# Advanced Gene Mapping Course

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Lectures

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# Genome-wide association studies (GWAS) - Part 1

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# Association testing: case/control studies

- Collect sample of affected individuals (cases) and unaffected individuals (controls)
  - Or a else a sample of random "population" controls
    - Most of whom will not have the disease of interest
- Examine the association (correlation) between alleles present at a genetic locus and presence/absence of disease
  - By comparing the distribution of genotypes in affected individuals with that seen in controls

# Genome-wide association studies (GWAS)

- Popular (and highly successful) approach over past 12 years
- Enabled by advances in high-throughput (microarray-based) genotyping technologies
- Idea is to measure the genotype at a set of single nucleotide polymorphisms (SNPs) across the genome, in a large set of unrelated cases and controls
  - Or related individuals (family data) but need to analyse differently

### Two individuals

Person 1 ACCTGTGTGCCCAATGGCGTCCCATACTATCGG ACCTGTGCGCCCAATGGCGTCCCATACTATCGG

Person 2 ACCTGTGCGCCCAGTGGCGTCCCATACTATCGG ACCTGTGCGCCCAGTGGCGTCCCATAGTATCGG

• Test each SNP for association/correlation with disease phenotype

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# Case/control studies

• Each person can have one of 3 possible genotypes at a SNP (with alleles coded 1 and 2)

Genotype	Cases	Controls
2 2	500 $(= a)$	200 (= b)
1 2	$1100 \ (= c)$	820 (= d)
1 1	400 $(=e)$	980 $(= f)$
Total	2000	2000

- $\bullet$  Test for association (correlation) between genotype and presence/ absence of disease using standard  $\chi^2$  test for independence on 2 df
- Two odds ratios can be estimated
  - OR  $(2|2:1|1) = \frac{af}{be}$
  - OR  $(1|2:1|1) = \frac{cf}{de}$

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## Odds ratios

- Odds of disease are defined as P(diseased)/P(not diseased)
  - Odds ratio OR (2|2:1|1) repesents the factor by which your odds of disease must be multiplied, if you have genotype 2|2 as opposed to 1|1
    - i.e. the 'effect' of genotype 2|2
- Similarly, we can define the OR for 1|2 vs 1|1
  - As the factor by which your odds of disease must be multiplied, if you have genotype 1|2 as opposed to 1|1
    - ullet i.e. the 'effect' of genotype 1|2
- ORs are closely related (often  $\approx$ ) genotype relative risks
  - The factor by which your probability of disease must be multiplied, if you have genotype 1|2 as opposed to 1|1 (say)
- If your genotype has no effect on your probability (and therefore on your odds) of disease, then the ORs=1.
  - $\bullet$  So the association test can be thought of as a test of the null hypothess that the ORs=1

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# Genotype relative risks

• If a disease is reasonably rare, the odds ratio approximates the genotype relative risk (GRR, RR)

Genotype	Penetrance	GRR	Odds	OR
1/1	0.01	1.0	0.01/0.99 = 0.0101	1.00
1/2	0.02	2.0	0.02/0.98 = 0.0204	2.02
2/2	0.05	5.0	0.05/0.95 = 0.0526	5.21

• If your genotype has no effect on your probability (and therefore your RR) of disease, then both the ORs and the GRRs=1.

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# Dominant/recessive effects

### Dominant:

Genotype	Cases	Controls	Total
2 2 and 1 2	500+1100	200+820	700+1920
1 1	400	980	1380
Total	2000	2000	4000

### Recessive:

Genotype	Cases	Controls	Total
2 2	500	200	700
1 2 and 1 1	1100+400	820+980	1920+1380
Total	2000	2000	4000

• Can also rearrange table to examine effects of alleles (1 df tests):

Counting alleles

		Counts in			
	Allele	Cases	Controls		
	2	2100 (=a)	1220 (=b)		
	1	1900 (= $c$ )	$2780 \ (=d)$		
•	Total	400	400		

Allelic OR = ad/bc

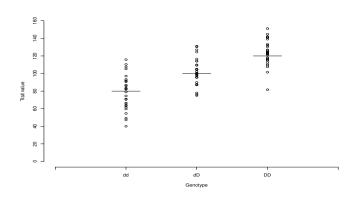
- $\chi^2$  test statistic on 1 df =  $\sum_i (O_i E_i)^2 / E_i$  where  $O_i$  and  $E_i$  are the observed and expected values in cell i.
  - Assumes HWE under null and multiplicative allelic effects under alternative: considers chromosomes as independent units
  - Better approach: use counts in previous genotype table to perform a Cochran-Armitage trend test
  - Even better approach: use linear or logistic regression

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# Testing for association: quantitative traits

- Linear regression provides a natural test for quantitative traits
  - Testing the null hypothesis that the slope = 0



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# Logistic regression

- Used in case/control studies
  - Outcome is affected or unaffected
  - Model probability (and thus odds) of disease p as function of variable x coding for genotype:

$$\ln \frac{p}{1-p} = \beta_0 + \beta_1 x \quad \equiv c + mx$$

- Use observed genotypes in cases and controls to estimate the values of regression coefficients  $\beta_0$  and  $\beta_1$ 
  - And to test whether  $\beta_1 = 0$

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# Logistic regression

- Standard method used in standard epidemiological studies e.g. of risk factors such as smoking in lung cancer
- Main advantage is you can include more than one predictor in the regression equation e.g.

$$\ln \frac{p}{1-p} = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3$$

where  $x_1$ ,  $x_2$ ,  $x_3$  code for

- genotypes at 3 loci
- measured environmental covariates (e.g. age, sex, smoking etc),
- genetic principal component scores (to adjust for population substructure),
- interactions between loci etc. etc.

# Testing for association

- All methods produce a test statistic and a p value at each SNP, indicating how significant the association/correlation observed appears to be
  - i.e. how likely it was to have occurred by chance
- At any location showing 'significant' association, we expect to see several SNPs in the same region showing association/correlation with phenotype
  - Due to the correlation or linkage disequilibrium (LD) between neighbouring SNPs

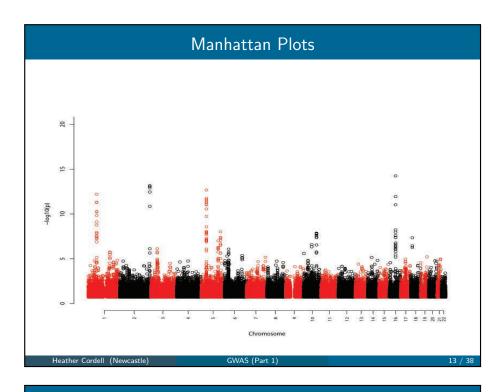
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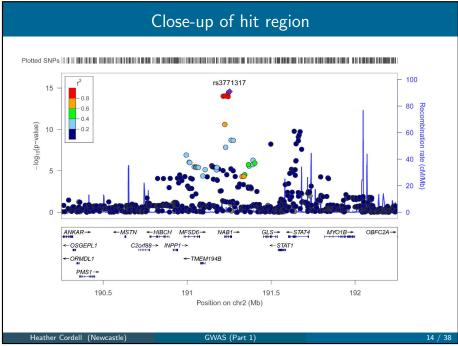
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# Historical Perspective: Complement Factor H in AMD

- First (?) GWAS was by Klein et al. (2005) Science 308:385-389
- Typed 116,204 SNPs in 96 cases (with age-related macular degeneration, AMD) and 50 controls
  - Very small sample size they were very lucky to find anything!
  - $\bullet$  Luck was due to the fact the polymorphism has a very large effect (recessive OR=7.4)
- Klein et al. followed up on two SNPs passing threshold  $(p < 4.8 \times 10^{-7})$ 
  - Plus a third SNP that just failed to pass significance threshold, but lay in same region as first SNP

# Complement Factor H in AMD

- Of the 3 SNPs followed up:
  - One appeared to be due to genotyping errors: significance disappeared on filling in some missing genotypes
  - First and third SNP lie in intron of Complement Factor H (CFH) gene
    - Lies in region previously implicated by family-based linkage studies
- Resequencing of the region identified a polymorphism of plausible functional effect
- Immunofluorescence experiments in the eyes of AMD patients supported the involvement of *CFH* in disease pathogenesis.

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## **GWAS**

- GWAS really got going about 12 or 13 years ago
  - See Visscher et al. (2012) AJHG 90:7-24 "Five Years of GWAS Discovery"
  - And Visscher et al. (2017) AJHG 101:5-22 "10 Years of GWAS Discovery: Biology, Function and Translation"
- 2007/2008 saw a slew of high-profile GWAS publications
  - Breast cancer (Easton et al. 2007)
  - Rheumatoid Arthritis (Plenge et al. 2007)
  - Type 1 and Type 2 diabetes (Todd et al. 2007; Zeggini et al. 2008)
- Arguably the most influential was the Wellcome Trust Case Control Consortium (WTCCC) study of 7 different diseases
  - http://www.wtccc.org.uk/

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## WTCCC

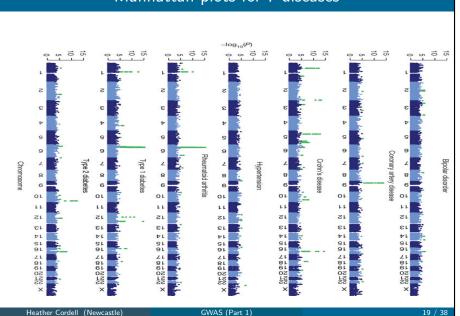
- Nature 447: 661-678 (2007)
- Considered 2000 cases for each of the following diseases:
  - Bipolar disorder, coronary artery disease, Crohn's disease, hypertension, rheumatoid arthritis, type 1 diabetes, type 2 diabetes
- Compared each disease cohort to common control panel
  - 3000 population-based controls
  - From 1958 birth cohort and National Blood Service
- Highly successful
  - WTCCC found 24 separate association signals
  - Including highly convincing signals in 5 out of the 7 diseases studied
  - All were replicated in subsequent independent follow-up studies

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# Manhattan plots for 7 diseases



# Lessons from WTCCC (and others)

- Typically used rather standard statistical/epidemiological methods  $(\chi^2 \text{ tests}, t \text{ tests}, \log \text{istic regression etc.})$
- Success largely due to:
  - An appreciation of the importance of large sample size (> 2000 cases, similar or greater number of controls)
  - Stringent quality control procedures for discarding low-quality SNPs and/or samples
  - Stringent significance thresholds ( $p=5\times10^{-8}$ ) to account for multiple testing and/or low prior prob of true effect
  - Importance of replication in an independent data set

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# **Quality Control**

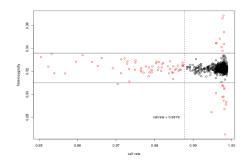
- Stringent QC checks are required for GWAS data
- Discard samples (people) deemed unreliable
  - Low genotype call rates, excess heterozygosity etc.
  - X chromosomal markers useful for checking gender
    - Males should 'appear' homozygous at all X markers
  - Genome-wide SNP data useful for checking relationships and ethnicity
- Discard data from SNPs deemed unreliable
  - On basis of genotype call rates, Mendelian misinheritances, Hardy-Weinberg disequilibrium
  - Exclude SNPs with low minor allele frequency (MAF)

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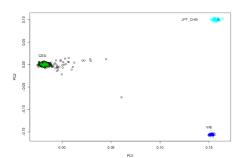
- 61 sample exclusions (low call-rate); 23 exclusions (heterozygosity)
- SNP exclusions also made based on call-rates, MAF and Hardy-Weinburg equilibrium (HWE)

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# QC: ethnicity tests



- Multidimensional scaling (with 210 HapMap individuals) identifies 33 samples with non-Caucasian ancestry
- Similar methods can be used to model more subtle population differences between samples

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# Multivariate Analysis

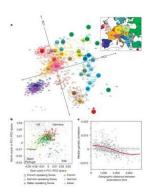
- Several related multivariate analysis techniques have been proposed for detecting population structure in genome-wide association studies
  - Principal components analysis (PCA)
  - Principal coordinates analysis (PCoA)
  - Multidimensional scaling (MDS)
- If population differences can be detected (and adjusted for) in association analysis, this offers a way to deal with the problem of population stratification
  - Population sampled actually consists of several 'sub-populations' that do not really intermix
  - Can lead to spurious false positives (type 1 errors) in case/control studies
- These techniques can also be used in quality control (QC) procedures, to check for (and discard) population outliers

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# Principal components analysis (PCA)

### Genes mirror geography within Europe



J Novembre et al. (2008) Nature 456(7218):98-101, doi:10.1038/nature07331

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# Principal Components Analysis

- Price et al. (2006) Nature Genetics 38:904-909; Patterson et al. (2006) PLoS Genetics 2(12):e190
  - Based on popn genetics ideas from Cavalli-Sforza (1978)
- Idea is to form a large matrix M of SNP counts (0,1,2) corresponding to the genotype at a L loci (=rows) for n individuals (=columns)

$$\mathsf{M} = \left( \begin{array}{cccc} g_{11} & g_{12} & \cdot & g_{1n} \\ g_{21} & g_{22} & \cdot & g_{2n} \\ g_{31} & g_{32} & \cdot & g_{3n} \\ \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot \\ g_{L1} & g_{L2} & \cdot & g_{Ln} \end{array} \right)$$

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# Principal Components Analysis

• Subtract row means and normalise by function of row allele frequency  $\sqrt{f_l(1-f_l)}$  to give matrix X

$$X = \begin{pmatrix} x_{11} & x_{12} & . & x_{1n} \\ x_{21} & x_{22} & . & x_{2n} \\ x_{31} & x_{32} & . & x_{3n} \\ . & . & . & . \\ . & . & . & . \\ x_{L1} & x_{L2} & . & x_{Ln} \end{pmatrix}$$

- This matrix will be used as starting point for PCA
  - In principal we could start with a different matrix in particular not all PCA approaches would normalise by  $\sqrt{f_l(1-f_l)}$

# Multivariate Analysis

- Estimate covariance matrix  $\Psi = X^T X$  between all pairs of individuals, with entries  $\psi_{ij}$  defined as the covariance (summing over SNPs) between column i and j of X
  - Represents average genome-wide IBD (estimated from IBS)
  - ullet Compute the eigenvectors  $ec{v}_j$  and eigenvalues  $\lambda_j$  of matrix  $\Psi$ 
    - ullet Co-ordinate j of the kth eigenvector represents the ancestry of individual j along 'axis' k
- For technical details, see McVean (2009) PLoS Genetics 5;10:e1000686
- Many genetics packages e.g. (PLINK) will allow you to calculate the top 10 (or more) PCs
  - Different geographic populations can often be well separated by just the first two or three PCs
    - Useful for outlier detection
  - For more subtle differences, you may need to calculate more PCs
    - And include them as covariates in the regression equation
    - Post-GWAS QC can determine whether you have included 'enough'

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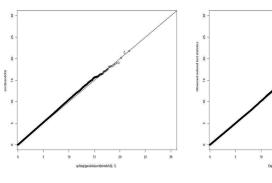
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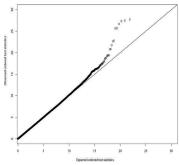
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# Post GWAS QC: Q-Q Plots (good)

• Plot ordered test statistics (y axis) against their expected values (x axis)

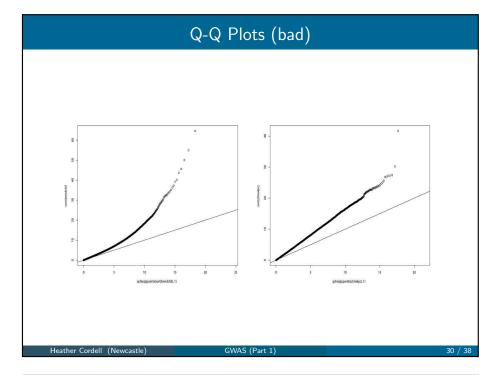




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# Population stratification

- $\bullet$  A QQ plot showing constant inflation (straight line with slope >1) can indicate population stratification/population substructure
- Simple solution: Genomic Control (Devlin and Roeder 1999)
  - Use your observed test statistics to estimate the slope (=inflation factor  $\lambda$ )
  - $\bullet$  Divide each test statistic by  $\lambda$  to get an adjusted (deflated) test statistic
- More complicated solution: use PCA/MDS or similar
- Even more complicated solution: use linear mixed models

# Relatedness

- With genome-wide data, can also infer relationships based on average identity by descent (IBD)  $\Psi = X^T X$  or identity by state (IBS)
  - Using 'thinned' subset of markers with high minor allele frequency (MAF) and in approximate linkage equilibrium
  - Simple relationships (PO, FS, MZ/duplicates) can identified with only a few hundred markers
  - More complicated relationships require 10,000-50,000 SNPs
- Various software packages, including PLINK, KING and TRUFFLE

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# Expected IBD sharing

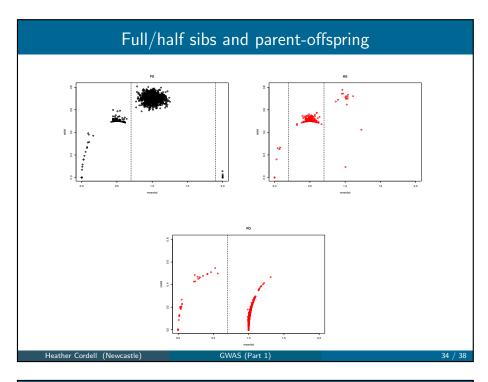
• Assuming no inbreeding, the IBD state probabilities are:

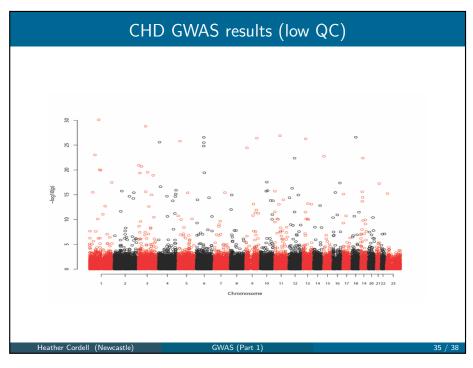
	Number of alleles shared IBD				
Relationship	2	1	0		
MZ twins	1	0	0		
Parent–Offspring	0	1	0		
Full siblings	1/4	1/2	1/4		
Half siblings	0	1/2	1/2		
Grandchild-grandparent	0	1/2	1/2		
Uncle/aunt-nephew/niece	0	1/2	1/2		
First cousins	0	1/4	3/4		
Second cousins	0	1/16	15/16		
Double 1st cousins	1/16	6/16	9/16		

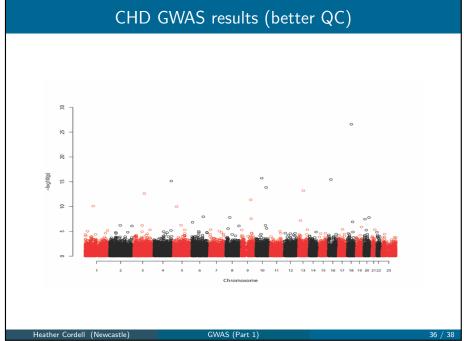
• A useful visualisation tool is to plot SE(IBD) vs mean(IBD)

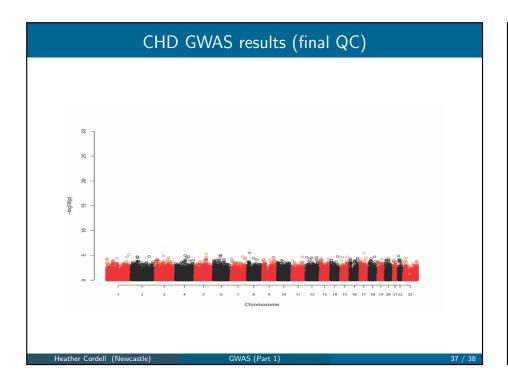
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# Genome-wide meta-analysis

- Puts together data (or results) from a number of different studies
  - Could analyse as one big study
  - But preferable to analyse using meta-analytic techniques
    - At each SNP construct an overall test based on the results (log ORs and standard errors) from the individual studies
- Meta-analysis is often made easier by using imputation
  - Inferring (probabilistically) the genotypes at SNPs which have not actually been genotyped
    - On the basis of their known correlations with nearby SNPs that have been genotyped
    - Using a reference panel of people (e.g. 1000 Genomes) who have been genotyped at all SNPs
- Enables meta-analysis of studies that used different genotyping platforms
  - By imputing to generate data at a common set of SNPs
    - Ideally while accounting for the imputation uncertainty in the downstream statistical analysis
    - In practice often don't bother use post-imputation QC to remove poorly-imputed SNPS

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# **Data Quality Control**

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# Genotype SNPs (~20-96) before Exome or Whole Genome Sequencing

- Genotype markers which can be used as DNA fingerprint
- Allows for Assessment of DNA quality
- Determines the sex of the individual
  - To aid in identification of sample swaps
- Detects cryptic duplicates
- · For family data
  - Aids in determining close familial relationships
    - Non-paternity
    - Sample swaps
    - Cryptic relationships

# **DNA Collection**

- Blood samples
  - For unlimited supply of DNA
    - · Transformed cell lines
      - Is expensive
    - · Whole genome amplification
    - Allows for the creation of large amounts of DNA from initial small DNA sample
      - » Perform WGA on each sample three or more times and use pooled samples
      - Can experience lower call rates and higher genotyping error rates
      - Not recommend to use WGS samples for Copy Number Variant analysis
- Buccal Swabs
  - · Small amounts of DNA
  - DNA not stable
- Saliva (Origene collection kit)

# **Measurement of DNA Concentrations**

- Nanodrop
- Picogreen

# **Detecting Genotyping Errors**

- Duplicate samples genotyped to detect inconsistencies
  - Can use duplicate samples that are inconsistent to adjust clusters to improve allele calls
    - Will not detect systematic errors
- Usually not performed for exome and whole genome sequencing studies

# **Effects of Genotyping Error**

- If there is no bias in genotyping error between cases and controls
  - Same rates of genotyping errors in case and control data
- For family based association studies Trios
  - Can increase both type I and II error
- Population based studies
  - Increases type II error only
- Cases and controls are genotyped
  - At different times
  - Different institutions
  - Or one group, case or control, is predominately genotyped at one time/same batch
- Can lead to different genotyping error rates in cases and controls
  - In this situation both type I and II error can be increased
- If genotyping cases and controls
  - Randomize cases and controls so they are spread evenly across genotyping runs.

# **Convenience Controls—Sequence Data**

- Obtain BAM files and recall cases and control together
  - Can still have differential errors between cases and controls
  - Check variant frequency by variant types in cases and control
    - Synonymous variants should have the same frequencies
    - Would not expect large differences in numbers of variants between cases and controls
- For single variants can compare difference in frequencies with gnomAD but is problematic
  - Differences in frequencies can be due to differences in populations and errors
  - Can not adjust for confounders
    - e.g. sex, population substructure/admixture
- Don't perform an aggregate test using frequency information from gnomAD

# **Convenience Controls**

- Can reduce the cost of a study
- Genotype data
- Type I error can be increased
  - Ascertainment from different population
  - Differential genotyping error
    - Even if performed at the same facility
- Proper QC can reduce or remove biases

# **Genotype Data QC – Population Based Studies**

- Remove DNA samples from individuals who are missing >3% or their genotype data
  - May choose to use an even more stringent criteria
- Low DNA quality can lead to higher genotypes error rates at markers with available genotype data
- Lower call rates in individuals may be due to DNA contamination with another DNA sample
- To avoid markers with higher genotyping error rates
  - For markers with a minor allele frequency (MAF)>0.05
    - Remove markers missing >5% of their genotype data
  - For makers with a MAF<5%</li>
    - Remove markers missing > 1% of their genotype data

# **Additional QC Family based studies**

- Detect double recombination events over small distances
  - Can be an indication of genotyping error
    - Merlin
- Detect non-Mendelian errors of segregation
  - Can be due to genotyping errors\*
  - If a larger number are observed
    - Could be due to incorrect specification of pedigree structure
      - e.g. non-paternity
    - Pedcheck

\*Many genotyping errors will not be detected for single nucleotide variants (SNVs). The probability of detecting non-Mendelian segregation due genotyping errors decreases with increasing MAF

# **Data Clean – Accessing Sex**

- Males mislabeled as females and females mislabeled as males
- Can be observed due to sample mix-ups
- Samples for which the sex is incorrect
  - Should be removed from the analysis
- Probably not the person you think it is

# **Data Clean – Accessing Sex**

- Males with an excess of heterozygous SNPs on the X chromosome can denote
  - Males mislabeled as females
  - Males with Klinefelter syndrome
  - Note: Males will be heterozygous for markers in the pseudoautosomal regions
- Females with an excess of homozygous genotypes on the X chromosome can denote
  - Females mislabeled as males
  - Females with Turner Syndrome

# **Checking for Potential DNA Contamination**

- DNA samples which have been contaminated by another DNA sample will have a larger proportion of their genotypes being heterozygous\*
- If cross contamination of samples within the same study will observe "relatedness" amongst study subjects
- Can also be observed from principal components analysis (PCA)/multidimensional scaling (MDS)
  - Samples which are cross contaminated will cluster together and not cluster with other samples

\*Higher levels of heterozygous markers will be observed in individuals of sub-Saharan African ancestry compared to those of European and Asian ancestry.

# **Checking for Duplicate and Related Individuals**

- Duplicate samples are sometimes included in a study as part of quality control
  - These can easily removed before data quality control
- Cryptic duplicates (unintentional)
  - DNA sample aliquoted more than once
  - Individual ascertained more than once for a study
    - e.g. The same individual undergoes the same operation more than once and is ascertained each time
- Individuals who are related to each other may participate in the same study
  - Unknown to the investigator

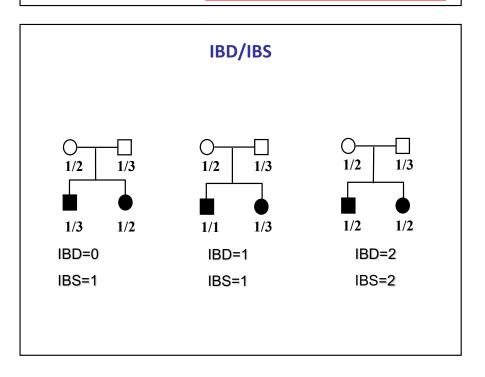
# **Identifying Duplicate and Related Individuals**

- Duplicate and related individuals can be detected by examining identify by state (IBS) adjusted for allele frequencies (p-hat) between all pairs of individuals within a sample
  - To estimate IBD sharing

# **Identifying Duplicate and Related Individuals**

- Genotype data from one of the duplicates needs to be removed from the dataset
- Only one related individual should be retained in the data set
  - If related individuals remain in the data set mixed-models need to be used to analyze the data\*
    - Case-Control
      - Generalized linear mixed models
    - Quantitative traits
      - Linear mixed models
  - If not type I error rates can be increased

\*If only a few related individuals in sample, may wish to remove them or use mixed-models to control type I errors. Must use mixed models if many related individuals in dataset. Due to the construction of the generalized relationship matrix (GRM) can be problematic to apply for large samples sizes, e.g. UKbiobank.



# **Identifying Duplicate and Related Individuals**

- IBS is the number of alleles of alleles which are shared between a pair of individuals
  - Can either share 0, 1, and 2 alleles
- Duplicate individuals will have IBS measures of 1 or close to 1
  - If there is genotyping error could make IBS< 1
- IBS measures are adjusted for by allele frequencies p-hat
  - Approximates IBD sharing

# King Graphical Output Known Relatives Cryptic Relatives 0.000 0.000 0.002 0.004 0.006 0.008 Pr(IBS=0)

# **Identifying Duplicate and Related Individuals**

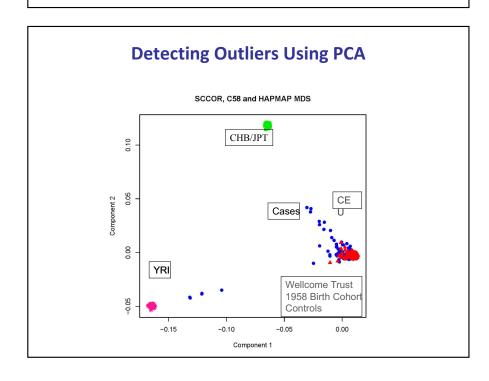
- Siblings and child-parent pairs will share 0.50 of their alleles IBD
  - For parent-child IBD=1 is ~1.0
  - For sibs IBD=1 is ~0.50
    - For more distantly related individuals the IBD measure will be lower
- Can use whole genome scan data to check IBD
  - Should "trim" markers so that they are not in LD
  - Caution should be used if using candidate genes are being studied since many markers will be in LD which can inflate the IBD measure
- PLINK or KING can be used to identify duplicate and related individuals

# Observing Low Levels of IBD Sharing for Multiple Individuals

- P-hat is calculated using the "population" allele frequency
- If individuals in sample come from different populations
  - Individuals from the same population within the sample will have inflated p-hat values due to incorrect allele frequencies
    - Appear incorrectly to be related to each other
- "Relatedness" amongst many individuals can also be observed when batches are combined if they have different error rates
  - Individuals from the same batch appear to be related
- DNA contamination can cause "relatedness" between multiple individuals

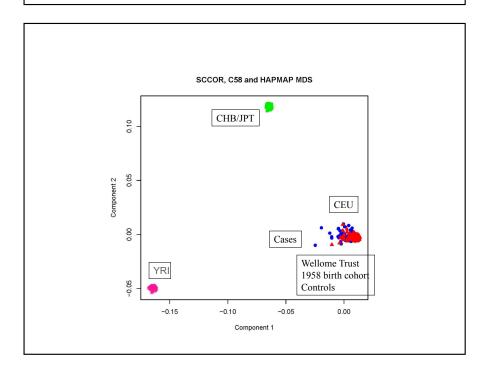
# **PCA/MDS**

- Can be used to find outliers
- Individuals from different ethnic backgrounds
  - African American Samples included in samples of European Americans
- Use a subset of markers which have been LD pruned
  - So there is only very low levels of LD between marker loci
- Plot 1<sup>st</sup> component vs. 2<sup>nd</sup> component
  - Additional components should also be plotted to determine potential biases in the data



# **PCA/MDS**

- Used to identify outliers
  - Individuals from different ancestries
    - e.g. African American samples included with European Americans samples
      - Can use samples from HapMap to help to determine what ethnic group outliers belong to.
        - » Should not include HapMap samples when calculating components to control for population substructure/admixture
  - Related individuals
  - Problems with genotype quality
    - Batch effects



# **Detecting Genotyping Error – Examining HWE**

- Testing for deviations from Hardy-Weinberg Equilibrium (HWE) not very powerful to detect genotyping errors
- The power to detect deviations from HWE is dependent on
  - Error rates
  - Underlying Error Model
    - Random
    - Heterozygous genotypes -> homozygous genotypes
    - Homozygous genotypes ->Heterozygous genotype
  - MAFs

# **Detecting Genotyping Error**

- Quantitative Traits
  - Caution should be used removing markers which deviate from HWE may be due to an association
    - Remove markers with extreme deviations from HWE and Flag markers with less extreme deviations from HWE
- In the presents of genotyping error
  - Random error and equal allele frequencies
  - Power to detect deviation from HWE is α
- Pseudo SNPs lend themselves to readily be detected through testing for deviation from HWE

# **Detecting Genotyping Error – Examining HWE**

- Controls and Cases are evaluated separately
  - Deviation found only in cases can be due to an association
- Test for deviation from HWE only in a sample of the same ancestry
  - Population substructure can introduce deviations from HWE
- Do not include related individuals when testing for deviations from HWE
  - Can cause deviation from HWE
- Quantitative Traits
  - Caution should be used removing markers which deviate from HWE may be due to an association
    - Remove markers with extreme deviations from HWE and Flag markers with less extreme deviations from HWE

# Testing for Deviations in HWE $-\alpha$ value

- ullet For different studies a variety of  $\alpha$  values are used
  - Need to consider that multiple testing is being performed
- WTCCC used a criterion p<5 X 10<sup>-7</sup> to remove SNPs
- A large variety of criterion are used to reject the null hypothesis of HWE
  - A criterion of 1.0 x 10<sup>-4</sup> is often used in published studies
- Deviations from HWE can be used to flag SNPs
  - e.g. Remove those SNPs with deviations from HWE with p<5.0 x  $10^{-8}$ 
    - Note should be more conservative if performing quality control for imputation
  - SNPs can then be investigated in more detail later for reasons for the observation of deviation from HWE
    - If there are significant association results
- A significant result with a large deviations from HWE in cases and controls is probably due to genotyping error or a pseudoSNP

# **Deviation from HWE**

• HWD coefficient (Weir 1996)

$$D = P_{11} - p^{2}$$

- For SNPs (2 allele system)
- The proportion observed for N genotypes G<sub>11</sub>, G<sub>12</sub> and G<sub>22</sub>
  - Is P<sub>11</sub>, P<sub>12</sub> and P<sub>12</sub> respectively
- p is the allele frequency which is estimated by

$$(2*G_{11} + G_{22})/2N$$

# **Detecting Genotyping Error**

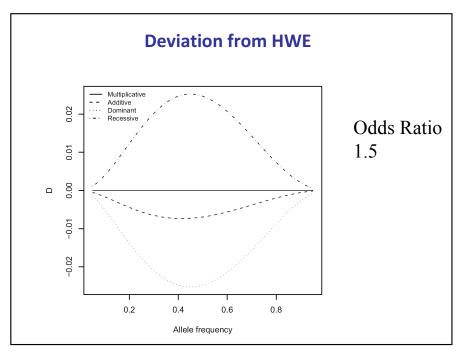
- Chance
  - Either an excess of heterozygous (-D) or homozygous genotypes (+D)
- Deviation from HWE due to genotyping error
  - Either an excess of heterozygous (-D) or homozygous genotypes (+D)
- Deviation from HWE due to pseudo SNPs
  - Excess of heterozygous (-D) genotypes
- Indication that deviation from HWE due to genotyping error
  - Higher genotype drop out rates for specific markers
- Pseudo SNPs
  - Primers map to multiple genomic regions

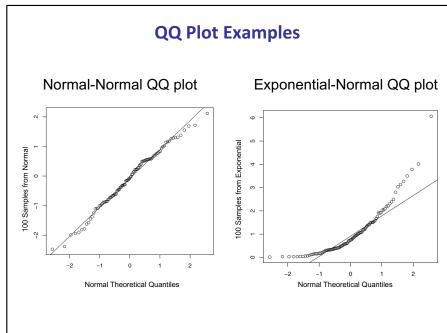
### **Deviation from HWE**

- Under HWE D=0
- Negative values of D indicate an excess of heterozygote genotypes
- Positive values of D indicate an excess of homozygote genotypes
- For a diallelic system
  - D can range from -0.25 to 0.25
- Markers not in HWE
  - May be due to population admixture
    - Excess of heterozygous genotypes (-D)
  - Copy number repeats (CNVs)
    - Either an excess of heterozygous (-D) or homozygous genotypes (+D)
- Heterozygous Advantage
  - Excess of heterozygous genotypes (-D)

# **Deviation from HWE**

- Genotype data from cases deviate from HWE when the SNP which is being tested is functional or in LD with a functional variant
  - Additive genetic model (D- excess heterozygous genotypes)
  - Dominant genetic model (D- excess heterozygous genotypes)
  - Recessive genetic model (D+ excess homozygous genotypes)
  - Multiplicative genetic model there is no deviation from HWE (D=0.0)
- Controls unaffected individuals
  - Display an extremely small deviation from HWE
  - Deviation from HWE is higher with higher disease prevalence
- Only unascertained samples have no deviation from HWE at the functional locus





# QQ plot

- QQ (quantile-quantile) plot is a graphical method for diagnosing differences between a random sample and a probability distribution
- Assume there are n points, ordered as x(1)<...<x(n). Then for i=1,...,n, we plot x(i) against the ith quantile (qi) of the specified distribution (e.g., normal).
- If the random sample is from the specified distribution, the QQ plot will be a straight line
- Let F() be the cumulative distribution function of a random variable, e.g., F(z)=P(x<z).
- The ordered n samples, x(1)<...<x(n), are treated as n empirical quantiles and the ith theoretical quantile, qi, corresponding to x(i) can be calculated as qi=F-1((i-0.5)/n)
- Plot qi on x axis and x(i) on y axis

# **Genome Wide Association Diagnosis**

- Thousands of markers are tested simultaneously
- The p values of neutral markers follow the uniform distribution
- If there are systematic biases, e.g., population substructure, genotyping errors, there will be a deviation from the uniform distribution
- QQ plots offers a intuitive way to visually detect biases

# All associations under the null except one

Phenotype	Covariate	Mean Chi-Square	GIF (λ)
BP		1.23829	1.16932
BP	Age	1.24119	1.18025
<u>BP</u>	Age-EV1	1.09471	<u>1</u>
BP	Age-EV2	1.0881	1
<u>BP</u>	Age-EV4	1.08385	1
BP	Age-EV10	1.09582	1.00402
BPI		1.14931	1.08921
BPI	Age	1.15139	1.08113
BPI	Age-EV1	1.05079	1.01148
BPI	Age-EV2	1.0428	<u>1</u>
<u>BPI</u>	Age-EV4	1.04204	1
BPI	Age-EV10	1.05421	1.01724
BPII		1.17283	1.25664
BPII	Age	1.17583	1.26996
BPII	Age-EV1	1.09874	1.15065
BPII	Age-EV2	1.09904	1.16425
BPII	Age-EV4	1.09502	1.14609
BPII	Age-EV10	1.10046	1.1418
BPII	Sex,Age-EV1	1.05958	1.06424
<u>BPII</u>	Sex,Age-EV4	1.05817	1.05323
BPII	Sex,Age-EV10	1.06338	1.05581

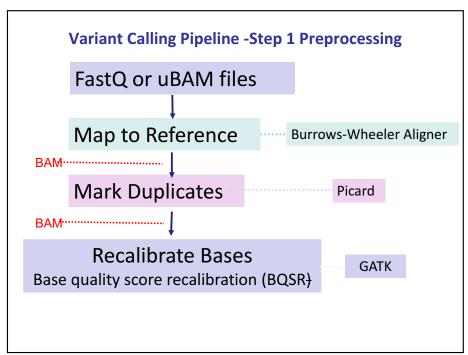
# Genomic Inflation Factor to Evaluate Inflation of the Test Statistic

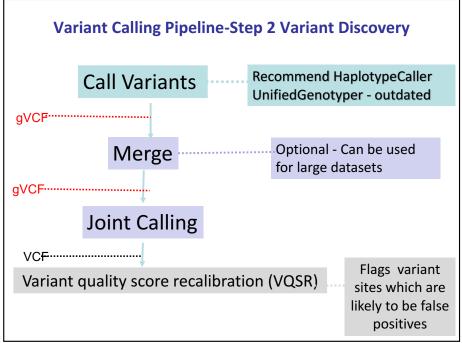
- Genomic Inflation Factor (GIF): ratio of the median of the test statistics to expected median and is usually represented as  $\lambda$ 
  - No inflation of the test statistic  $\lambda=1$
  - Inflation λ>1
  - Deflation λ<1</li>
- Problematic to examine the mean of the test statistic
  - If for a number of variants the null can be rejected
    - Particularly if they have very small p-values
      - The mean test statistic will be inflated

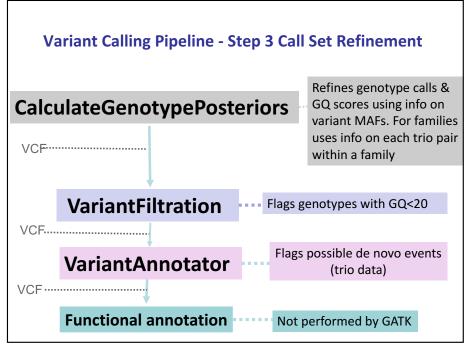
# **Significance Results**

- For those SNPs with strong associations
- Cluster plots should be examined
- Poor clustering overlap between clusters
  - Could be the reason for the strong association
- Cluster caller should be adjusted when possible and data reanalyzed









# **Variant Calling**

- BAM files are large and take considerable resources
  - Storage is expensive
  - One 30x whole genome is ~80-90 gigabytes
  - A small study of 1,000 samples will consume 80 terabytes of disk space
- The cost of cloud computing to call variants
  - (Souilmi et al. 2015)
  - \$5 per exome
  - \$50 per genome
    - For 1,000 samples
      - \$5,000 exome
      - \$50,000 genome

# Working with gVCF

- Instead of obtaining VCF files
- Can obtain gVCF files to perform joint calling and the rest of the GATK pipeline
  - A whole genome gVCF
    - ~1 Gigabyte
      - 1/100th the size of a BAM file for one individual
- Need additional information on how variants were called
  - e.g. HaplotypeCaller or UnifiedGenotyper
    - · Not valid to use Unified Genotyper

# **Influences on Sequence Quality**

- DNA quality
  - Age of sample
  - Extract method
  - Source of sample
- Sequencing machines (read length)
- Median sequencing depth
- Alignment
- · Variant calling method used
  - SNVs and Indels

# **NGS Data Quality Control**

- Extremely important to perform before data analysis
  - Poor data quality can increase type I and II errors
  - Due to inclusion of false positive variant sites or incorrect genotype calls
- Sequence quality can be influenced by
  - DNA quality
  - Sequencing machines (read length)
  - Sequencing depth
  - Alignment
  - Variant Calling
    - SNVs and Indels
- Protocols for data QC are still in their infancy
  - No set protocols for QC
- QC which has to be performed is data specific
  - Dependent on read depth
  - Batch effects
  - Availability of duplicate samples
  - etc

# NGS Data Quality - Removal of Genotype Calls and Samples

- Sequence read genotype depth (GD)
  - Concerned if GD is too low or too high\*
    - GD too low insufficient reads to call a variant site
    - GD too high can be an indication of copy number variants which can introduce false positive variant calls
      - \*Due to down sampling in GATK maximum GD is 250
    - Remove genotypes with low read depth, e.g. GD<8
  - Genotype quality (GQ) score
    - Removal of sites with low genotype quality core, e.g. GQ< 20
- Remove individuals who are missing genotype calls/variant sites, e.g.
   > 10%
  - To remove individuals with bad quality data who can potentially have incorrect genotype calls
- If using different capture arrays use the intersect of the arrays

# NGS Data Quality - Removal of Genotype Calls and Samples

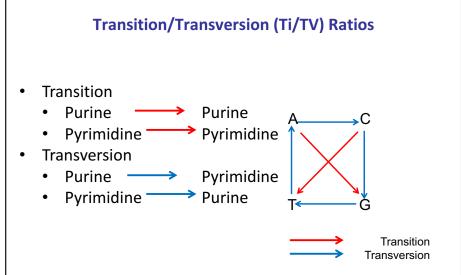
- · Removal of sites with missing data
  - e.g. missing > 10% of genotypes
- Removal of "novel" variant sites which only occur in one batch and the alternative allele is observed multiple times or the minor allele frequency (MAF) is high in overall sample
- Removal of sites that deviate from Hardy-Weinberg Equilibrium (HWE)
  - Must be performed by population if the study consists of more than one ancestry group, e.g. African American and European American
  - Related individuals should also be removed from the sample before testing for deviations from HWE

# **NGS Data Quality Control**

- Variant Quality Score Recalibration (VQSR) or
  - GATK
- Used to determine variant sites of bad quality
- However even after this step
  - Concordance of duplicates (when available) and
  - and Ti/Tv ratios are often low
- Additional QC steps needs to be performed

# **NGS Data Quality Control**

- Values which are used for GD, GQ, and missing data cut offs are based upon
  - Concordance rates
    - if there duplicate samples are available
  - Ti/Tv ratios
    - For individuals
    - Entire sample
  - Removal of batch effects
    - · As evaluated by multidimensional scaling (MDS) or
    - Principal components analysis (PCA)
  - Amount of data removed
    - QCI can remove substantial amounts of data which should be avoided
      - e.g. >15% of variant sites



# Transition/Transversion (Ti/TV) Ratios

- Ti/Ty Ratios
  - Whole genome ~2.0
  - Exome novel ~2.7
  - Exome known ~3.5



- Ti/Tv ratios can be calculated by
  - · Sample or
  - Dataset



- Ti/Tv ratios can be evaluated for subsets of data
  - e.g. by batch

# **Example -Project Description**

- 1,667 Samples
- Seven cohorts
- Two sequencing centers
  - Center 1
    - Two capture arrays
      - NimbleGen V2Refseg 2010 (CA1): 1082
        - » Batch 1 and 3
      - NimbleGen bigexome 2011 (CA2): 234
        - » Batch 2
  - Center 2
    - One capture array
      - Agilent SureSelect
        - » Batch 4
- Four batches
- No intentional duplicate samples

# **Example Project Description**

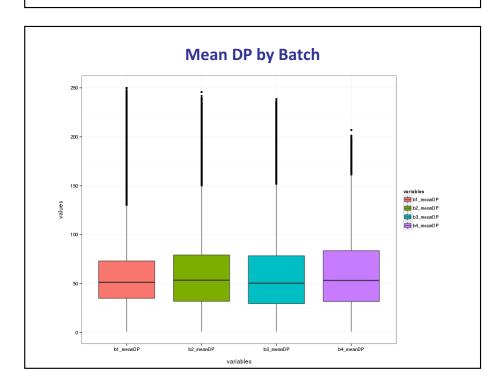
- Intersection of the three capture arrays used
  - NimbleGen V2Refseq 2010
    - Batch 1 and 3
  - NimbleGen bigexome 2011
    - Batch 2
  - Agilent Sure Select
    - Batch 4
- Sequencing machine
  - Illumina HiSeq
- Sequence alignment
  - BWA
- Multi-sample variant calling
  - GATK

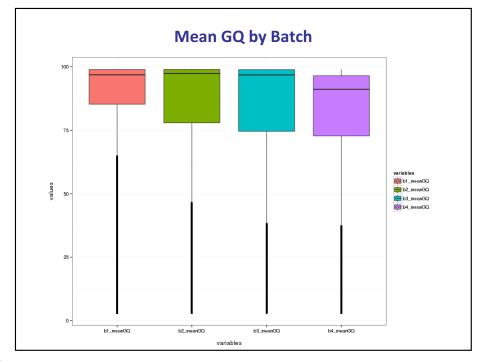
# **Sequence Data QC Overview**

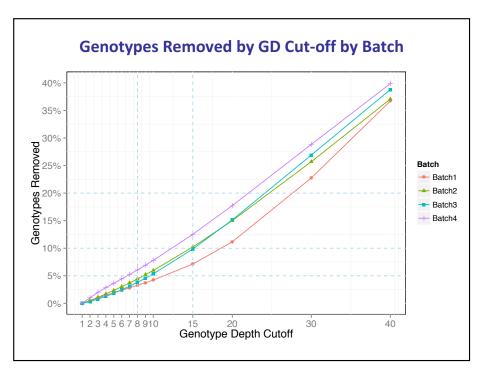
- Variant and genotype call level
  - Evaluation of batch effects
- Genotype call level Removal of genotype calls
  - Low or high depth of coverage GD < 8
  - Low genotype quality score GQ < 20</li>
- Removal of individual samples
  - >20% missing data
    - After taking the intersect of capture arrays
  - Samples without phenotype information
- Variant level removal of variant sites
  - Low call rate
    - i.e., missing call rate > 10%
  - "Novel" variant sites observed ≥2 only in a single batch
  - Deviation from Hardy-Weinberg-Equilibrium
    - · Population specific
    - Unrelated individuals
      - p<5 x 10<sup>-8</sup>

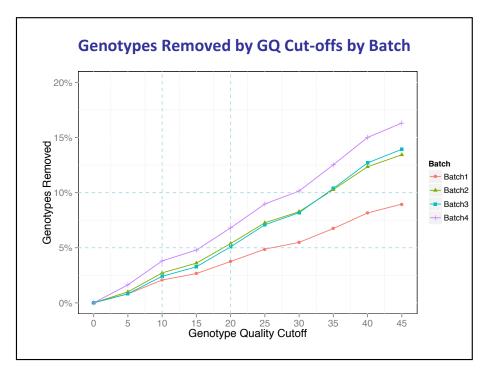
# **Sequence Data QC Overview**

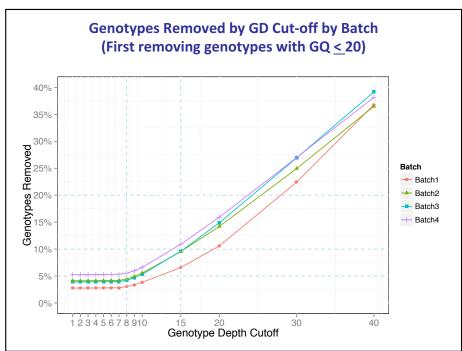
- Detection of sample outliers
  - Perform multidimensional scaling (MDS) to detect outliers
    - Due to population substructure/admixture and batch effects
    - · Remove effects by
      - Additional QC
      - Removal of outliers and\or
      - Inclusion of MDS or PCA components in the association analysis
- Evaluate sex of individuals based upon X and Y chromosomal data
  - Sample mix-ups
  - Individuals with Turner or Klinefelter Syndrome
- Evaluate samples for cryptically related individuals and duplicates
  - King or Plink algorithm
    - Retain one duplicate of a pair
    - Retain only one individual of a relative group or control for relatedness in the analysis, i.e. mixed models
- Post Analysis Quantile-Quantile (QQ)plots
  - To evaluate uncontrolled batch effects and population substructure/admixture

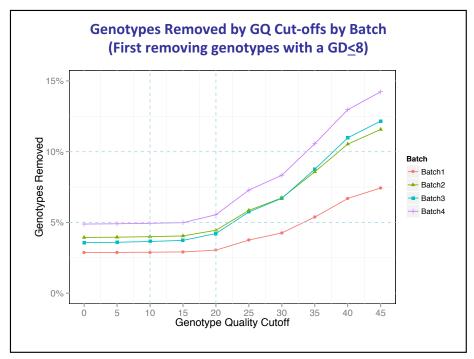












# **Missing Rate Criteria & Sites Removed**

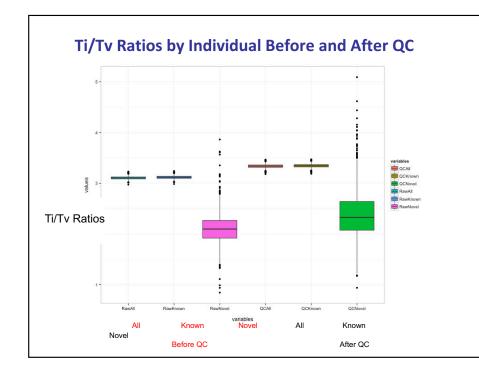
	10%	5%
Before QC*	2.5%	3.9%
After QC	12.9%	18.3%

<sup>\*</sup>After VQSR

Variant sites missing >10% of their data were removed

# Ti/Tv Ratios during QC Process

	Known	Novel	All
Before VQSR	2.95 ± 0.05	1.18 ± 0.29	2.86 ± 0.07
Before QC	3.12 ± 0.03	2.01 ± 0.32	3.11 ± 0.03
Genotype QC GD<8, GQ <20	3.18 ± 0.04	2.10 ±0.32	3.16 ± 0.03
Remove sites missing >10% genotypes	3.39 ± 0.04	2.42 ± 0.52	3.39 ± 0.04
Remove batch specific novel sites ≥ 2 N=17,835	3.39 ± 0.04	2.41 ± 0.53	3.39 ± 0.04
Remove sites deviating from HWE p<5x10 <sup>-8</sup> N=4,414	3.41 ± 0.04	2.39 ± 0.54	3.40 ± 0.04

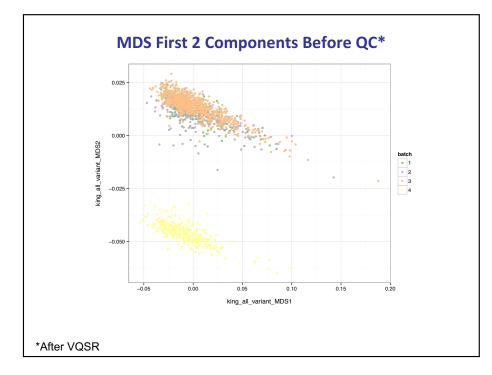


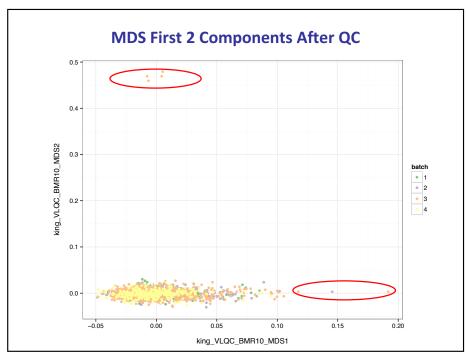
# **Detecting Outliers Using Multidimensional Scaling (MDS)**

- Multidimensional Scaling (MDS) and principal components analysis (PCA) are frequently used to detect outliers
  - MDS & PCA can also be used to control for substructure in the analysis
- Outliers can be cause by
  - Population stratification
  - Population substructure
  - Batch Effects

# **Sequence Data QC**

- Batch effects can sometimes be removed with additional QC
- Extreme outliers should be removed
- Additionally MDS or PCA components can be included in the analysis to control for population substructure\admixture and batch effects
  - Unless correlated with the outcome (phenotype)
- Batch effects (dummy coding) may be included as a covariate in the analysis
  - Unless correlated with the outcome (phenotype)





# **Order of Data Cleaning**

- Remove samples missing >10% genotype data
- Remove SNPs with missing genotype data
  - If MAF >5%
    - Remove markers with >5% missing genotypes
  - If MAF <5%</li>
    - Remove markers with >1% missing genotypes
- Remove samples missing >3% genotype calls
- Check for sex of individuals based on X-chromosome markers
  - Remove individual whose reported sex is inconsistent with genetic data
    - Could be due to a sample mix-up
- Check for cryptic duplicates and related individuals
  - Used "trimmed data set of markers which are not in LD
    - E.g.  $r^2 < 0.5$
  - Retain duplicate with best genotyping quality

# **Order of Data Cleaning**

- Perform principal components analysis to check for outliers
  - Use trimmed data set of markers which are not in LD
    - E.g.  $r^2 < 0.5$
  - Remove outliers from data
- Check for deviations from Hardy Weinberg Equilibrium
  - Separately in cases and controls
  - If more than one ethnic group
    - Separately for each ethnic group
- Examine QQ plots for potential problems with the data
  - e.g. not controlling adequately for population admixture

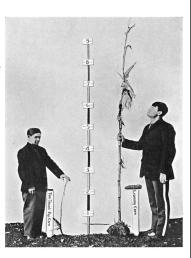
# Complex Trait Association Analysis of Rare Variants Obtained from Sequence Data: Population-Based Data

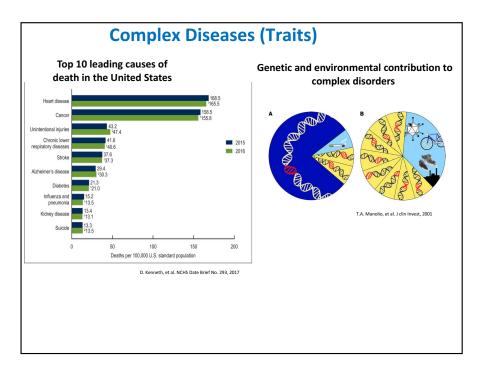
© 2020 Suzanne M. Leal, suzannemleall@gmail.com

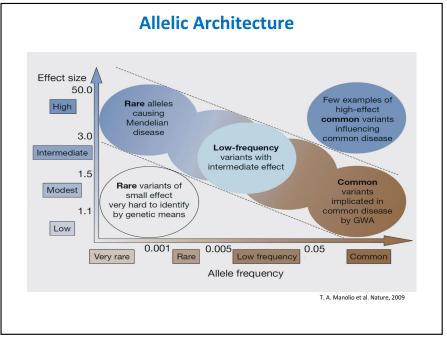
# **Heritability for Common Traits**

# Human height heritability is ~80%

- Strongly associated common variation explain 21—29%
- All common variation explains 60% of height heritability





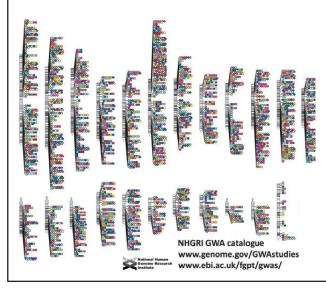


# Complex Disease – Common Variant Associations

- Disease susceptibility is conferred by variants which are common within populations
  - Variants are old and widespread
- These variants have modest phenotypic effect
- This model is supported by a large number of replicated examples
  - Age Related Macular Degeneration (Klein et al. 2005)
    - Complement factor H (CFH) gene



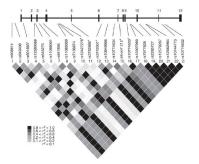
# **Complex Trait – Common Variant Associations**



- Although highly successful in identifying thousands of complex trait loci
- Usually pathogenic susceptibility variant(s) not identified

# Studying Complex Traits – Common Variant Associations

- Hundreds of thousands of Single nucleotide polymorphism (SNPs) genotyped and analyzed
  - Indirect mapping
    - Markers usually had a minor allele frequency (MAF) > 0.05
    - Usually not pathogenic tag SNPs
    - In linkage disequilibrium with disease susceptibility variant

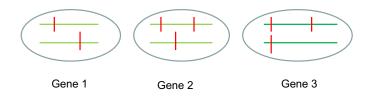


# **Complex Disease – Rare Variant Associations**

- Complex traits are the result of multiple rare variants
  - Although first thought to large effects, there effect sizes are usually small
- Although these variants are rare, e.g. MAF<0.005
  - Collectively they may be guite common
- Direct tests of this hypothesis where first reported >10 years ago
  - Dallas Heart Study
    - Small sample ~1,200 indiviuals
      - Multi-ethnic
      - Used "extreme" sampling
    - Plasma low density lipoprotein levels (Cohen et al. 2004)
      - NPC1L1

# Rationale for Rare Variant Aggregate Association Tests

- Testing individual variants with low effect sizes and minor allele frequencies (MAFs)
  - Underpowered to detect associations
- Testing variants in aggregate increases MAFs
  - Improving the power to detect associations



# **A Few Rare Variant Association Tests**

- Combined Multivariate Collapsing (CMC)
  - Li and Leal AJHG 2008
- Burden of Rare Variants (BRV)
  - Auer, Wang, Leal Genet Epidemiol 2013
- Weighted Sum Statistic (WSS)
  - Madsen and Browning PloS Genet 2009
- Kernel based adaptive cluster (KBAC)
  - Liu and Leal PloS Genet 2010
- Variable Threshold (VT)
  - Price et al. AJHG 2010
- Sequence Kernel Association Test (SKAT)
  - Wu et al. AJHG 2011
- SKAT-0
  - Lee et al. AJHG 2012

Fixed Effect Tests

Random Effect Test Optimal test

# **Caveats - Aggregate Rare Variant Association Tests**

- Misclassification of variants can reduce power
  - Inclusion of non-causal variants
  - Exclusion of causal variants
- · Analysis is limited to
  - Genes
  - Genes within pathways
- Analysis outside of exonic regions is problematic
  - Unlikely a sliding window approach will work
    - · Size of window unknown and will differ across the genome
  - A better understanding of functionality outside the coding regions is necessary
    - Predicted functional regions, enhancer regions, transcription factors, DNase I hypersensitivity sites, etc.

# **Types of Aggregate Analyses**

- Frequency cut offs used to determine which variants to include in the analysis
  - Rare Variants (e.g. <1% frequency)</li>
  - Rare and low (1-5%) frequency variants
- Maximization approaches
- Tests developed to detection associations when variants effects are bidirectional
  - e.g. protective and detrimental
- Incorporate weights based upon annotation
  - Frequency
    - e.g. gnomAD
  - Functionality
    - CADD c-scores

# Methods to Detect Rare Variant Associations Using Variant Frequency Cut-offs

- Combined multivariate & collapsing (CMC)
  - Li & Leal, AJHG 2008
- Collapsing scheme which can be used in the regression framework
  - Can use various criteria to determine which variants to collapse into subgroups
    - Variant frequency
    - · Predicted functionality

### **CMC**

- Example of coding used in regression framework:
  - Binary coding  $\chi_j = \begin{cases} 1 & \text{if rare variants present} \\ 0 & \text{otherwise} \end{cases}$
  - Gene region with 5 variant sites

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•			
•			
		+ + -	

1	1
2	1
3	0

Coding

Individual

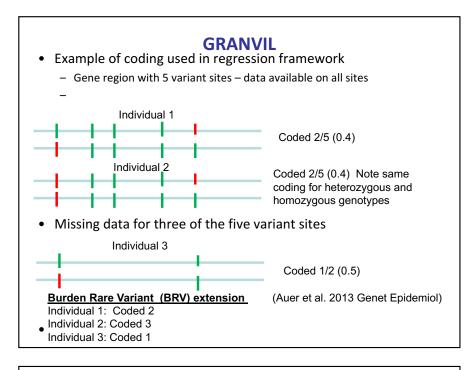
### Rare Variant Sites

Green bars: Major allele is observed in the study subject Red bars: Minor allele has been observed

**CMC** • Define covariate Xj for individual j as  $\chi_{j} = \begin{cases} 1 & \text{if rare variants present} \\ 0 & \text{otherwise} \end{cases}$ • Compute Fisher exact test for 2x2 table Number of cases for which one or more rare Number of cases variants are observed without a rare X=1X=0 e.g. nonsynonymous variants variants freq. <1% cases controls Number of controls Number of for which one or more controls without rare variants are a rare variants observed Can also use same coding in a regression framework

# Methods to Detect Rare Variant Associations Using Variant Frequency Cut-offs

- Gene-or Region-based Analysis of Variants of Intermediate and Low frequency (GRANVIL)
  - Aggregate number of rare variants used as regressors in a linear regression model
  - Can be extended to case-control studies
    - Morris & Zeggini 2010 Genet. Epidemiol
  - Test also referred to as MZ



# Methods to Detect Rare Variant Associations Maximization Approaches

- Variable Threshold (VT) method
  - Uses variable allele frequency thresholds and maximizes the test statistic
  - Also can incorporate weighting based on functional information
    - Price et al. AJHG 2010
- RareCover
  - Maximizes the test statistic over all variants with a region using a greedy heuristic algorithm
    - Bhatia et al. 2010 PLoS Computational Biology

# Methods to Detect Rare Variant Associations Weighted Approaches

- Group-wise association test for rare variants using the Weighted Sum Statistic (WSS)
  - Variants are weighted inversely by their frequency in controls (rare variants are up-weighted)
    - Madsen & Browning, PLoS Genet 2009
- Kernel based adaptive cluster (KBAC)
  - Adaptive weighting based on multilocus genotype
    - Liu & Leal, PLoS Genet 2010

# Methods to Detect Associations with Protective & Detrimental Variants within a Region

- C-alpha
  - Detects variants counts in cases and controls that deviate from the expected binomial distribution
    - For qualitative traits only
      - Neale et al. 2011 PLoS Genet
- Sequence Kernel Association Test (SKAT)
  - Variance components score test performed in a regression framework
    - Can also incorporate weighting
  - Wu et al. 2011 AJHG

### **Optimal Test**

- SKAT-O
  - Maximizes power by adaptively using the data to combine an aggregate test and the sequence kernel association tests
    - Lee et al. 2012 AJHG

# Determine MAF Cut-offs for Aggregate Rare Variant Association Tests

- MAF cut-offs are frequently used to determine which variants to analyze in aggregate rare variant association tests
- MAF from controls should not be used
  - Increases in type I error rates
- Determine variant frequency cut-offs from databases
  - ExAC
    - http://exac.broadinstitute.org/
  - gnomAD
    - http://gnomad.broadinstitute.org/

# Significance Level for Rare Variant Association Tests

- For exome data where individual genes are analyzed usually a Bonferroni correction for the number of genes tested is used.
  - There is very little to no linkage disequilibrium between genes
- Often a Bonferroni correction for testing 20,000 genes is often used as the significance level cut-off
  - $-2.5 \times 10^{-6}$

# Problem of Missing Genotypes for Aggregate Rare Variant Association Tests

- Same frequency of missing variant calls in cases and controls
  - Decrease in power
- More variant calls missing for either cases or controls
  - Increase in Type I error
  - Decrease in power
- Remove variant sites which are missing genotypes, e.g. >10%
- Impute missing genotypes using observed allele frequencies
  - For the entire sample
    - Not based on case or control status
- Analyze imputed data using dosages



### National Heart Lung and Blood Institute Exome Sequencing Project (NHLBI-ESP)

### Selection for the 12 Primary Traits

### Extreme quantitative trait values

Low-density lipoprotein (N=657) Blood pressure (N=812)

### Disease severity

Asthma (N=190)

Chronic obstructive pulmonary disease (N=623)

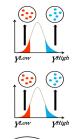
### Disease endpoints

Stroke (N=551)

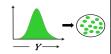
Early onset myocardial infarction (N=1007)

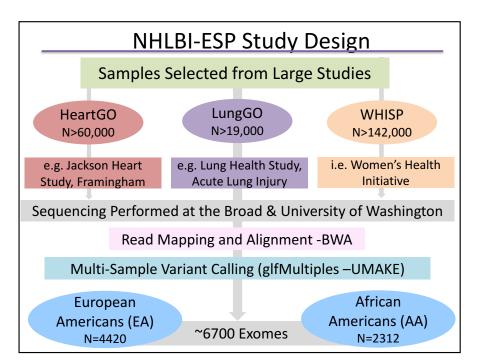
### Deeply phenotyped individuals

Randomly selected to be used as controls (N=964)









### Extensive Secondary Phenotypic Data

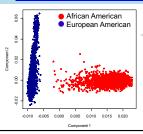
- C-reactive protein (N=3379)
- Red blood cell count (N=1103)
- ➤ EKG measurements(N<sub>EKG-OT</sub>= 3442)
- Systolic blood pressure (N=4423)
- > Fasting blood glucose (N=2470)
- Triglycerides (N=3728)

Fibrinogen (N=2915)

- ➤ Uric acid (N=2169)
- ➤ High-density lipoprotein (N=3770)
  - Waist-to-hip ratio (N=3853)
- ➤ Intima-media thickness (N=2079 )
- White blood cell count (N=3792)
- ➤ Low-density lipoprotein (N=2685)
- von Willebrand factor (N=1587)
- 59 Secondary phenotypes\*
  - > 48 quantitative traits
- > 11 qualitative traits
- \*Some traits are both primary and secondary
  - i.e. asthma, blood pressure, BMI, COPD, LDL, T2D

# Association Analysis Very different for rare variant sequence data than for common variants obtained from genotyping arrays Exom

Analysis performed using Variant
Association Tools
http://varianttools.sourceforge.net/VAT



### **Exome Data Quality Control**

### **Variant Site Removal**

**Support Vector Machine** 

### **Variant Call Removal**

Read Depth <10X

### **Variant Site Removal**

>500X mean depth, Missing >10% genotypes

Sex Check

### **Duplicates & Related Sample Check**

### Designate EAs & AAs

Multidimensionality scaling (MDS)

### Variant Site Removal

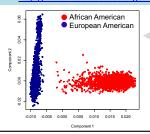
Deviation from HWE

# Data Quality Control & Association Analysis

Very different for rare variant sequence data than for common variants obtained from genotyping arrays

Analysis performed using Variant Association Tools

http://varianttools.sourceforge.net/VAT



### **Exome Data Quality Control**

### **Variant Site Removal**

Support Vector Machine

### Variant Call Removal

Read Depth <10X

### Variant Site Removal

>500X mean depth, Missing >10% genotypes

**Sex Check** 

### **Duplicates & Related Sample Check**

### Designate EAs & AAs

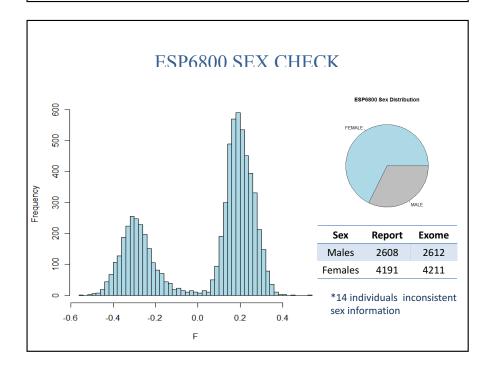
Multidimensionality scaling (MDS)

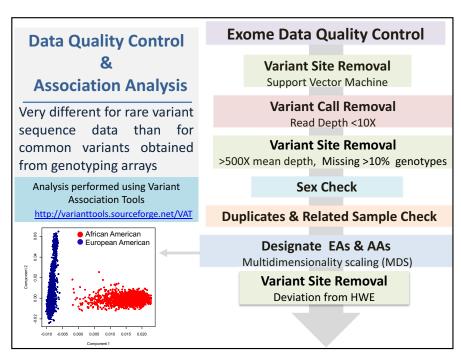
### **Variant Site Removal**

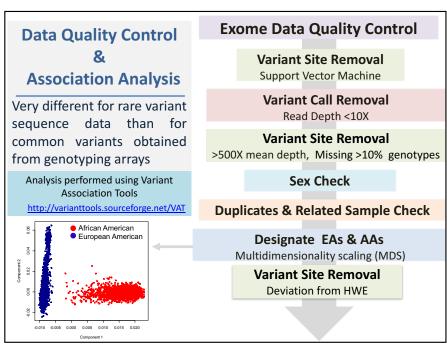
**Deviation from HWE** 

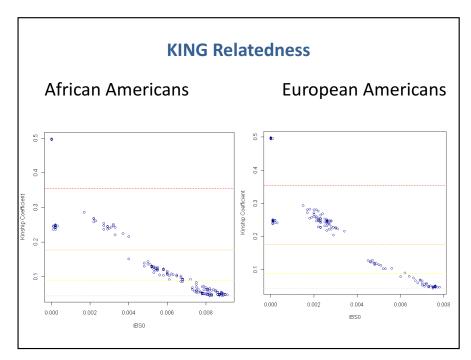
### Support Vector Machine (SVM)

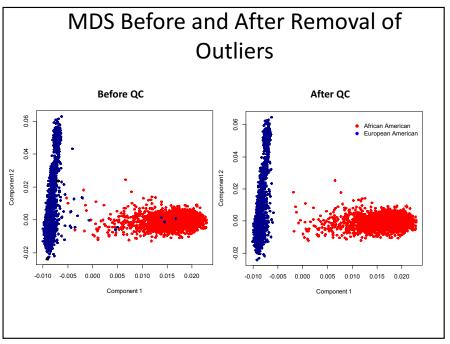
- A machine-learning algorithm, to separate likely true positive and false-positive variant sites.
- Uses VCF annotation related to quality of each SNV, including
  - Overall depth
  - Fraction of samples with coverage
  - Fraction of reference bases in heterozygous individuals (allele balance)
  - Inbreeding coefficient
  - In all 16 parameters were used
- Training set
  - False positives
    - SNVs that deviated significantly from expected values in three or more annotation categories
  - True positives
  - SNVs at HapMap polymorphic sites and Omni 2.5 array polymorphic sites in the 1000 Genomes project data
- The SVM classifier was used to identify all likely false positive sites
- Those variant sites which fail the support vector machine (SVM) (Likely false positive variant sites)
  - Are flagged and removed from further analysis



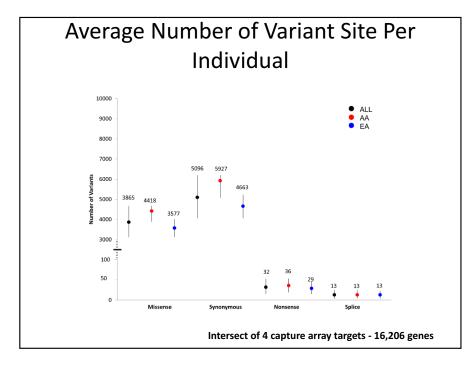






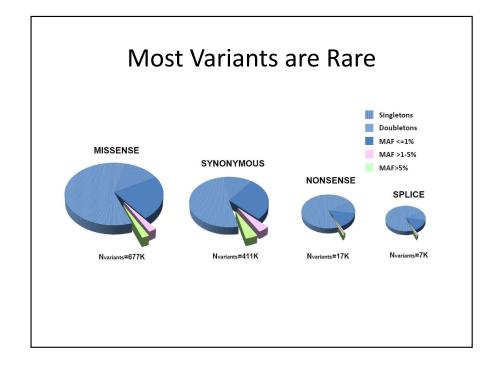


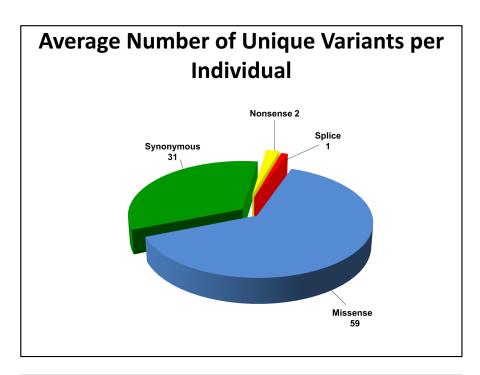
### **Exome Data Quality Control Data Quality Control Variant Site Removal Association Analysis** Support Vector Machine Variant Call Removal Very different for rare variant Read Depth <10X sequence data than for **Variant Site Removal** common variants obtained >500X mean depth, Missing >10% genotypes from genotyping arrays Analysis performed using Variant **Sex Check Association Tools** http://varianttools.sourceforge.net/VAT **Duplicates & Related Sample Check** African American European American Designate EAs & AAs Multidimensionality scaling (MDS) Variant Site Removal **Deviation from HWE**

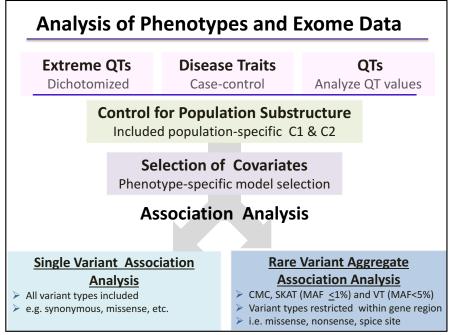


### Removal of Additional Variant Sites

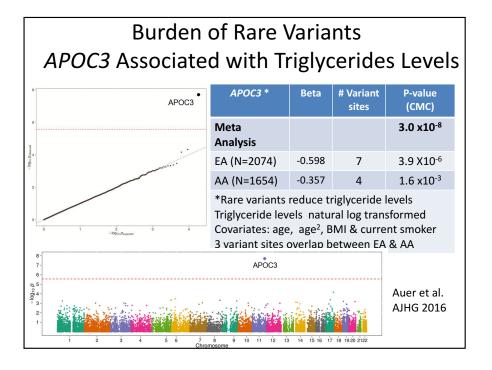
- Variant sites which deviate from HWE
  - − Using a p-value <1x10<sup>-7</sup> criterion
    - Number of variant sites which deviate from HWE expectations:
      - EA: 2332
      - AA: 2663







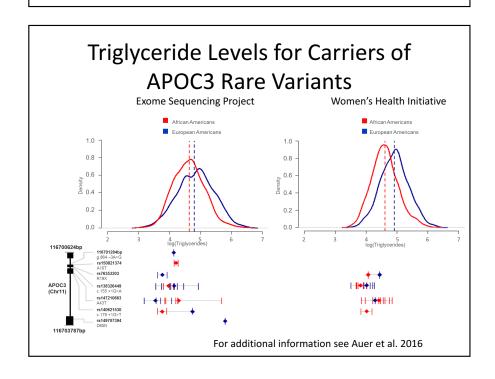
### **Analysis of Phenotypes and Exome Data Extreme QTs Disease Traits** QTs Dichotomized Case-control Analyze QT values **Control for Population Substructure** Included population-specific C1 & C2 Selection of Covariates Phenotype-specific model selection **Association Analysis** Rare Variant Aggregate **Single Variant Association Analysis Association Analysis** All variant types included CMC, SKAT (MAF <1%) and VT (MAF<5%).</p> Variant types restricted within gene region e.g. synonymous, missense, etc. i.e. missense, nonsense, spice site



### The Exome Chip

NHLBI-ESP the largest contributor of sequence data for the development of the exome chip

- > ~240,000 missense, nonsense and splice site variants
- NHLBI-ESP findings are being followed up using the exome chip
- Novel findings are also being pursed
- More than 100,000 exome chips being genotyped and analyzed using samples from the ESP cohorts



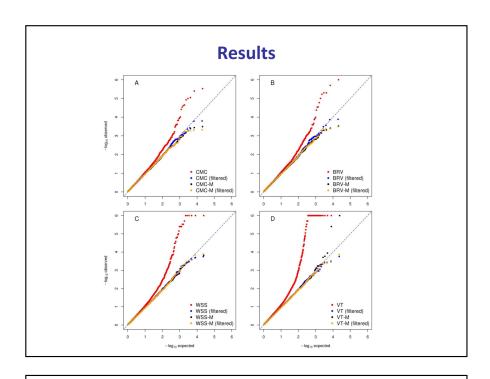
# Replication with the Exome Chip *APOC3* Associated with Triglycerides Levels

APOC3 *	Sample Size	# Variant Sites	P-value	
Meta Analysis	8,069		1.7 x 10 <sup>-18</sup>	
Women's Health Initiative (WHI) Exome Chip				
Meta Analysis	4,341		9.4 x 10 <sup>-12</sup>	
European Americans	2,301	3	1.3 x 10 <sup>-6</sup>	
African Americans	2,041	4	1.6 x 10 <sup>-6</sup>	
Exome Sequencing Project				
Meta Analysis	3,728		3.0 x 10 <sup>-8</sup>	
European Americans	2,074	7	3.9 x 10 <sup>-6</sup>	
African Americans	1,654	4	1.6 x 10 <sup>-3</sup>	
*Deduces trichuseride levels				

<sup>\*</sup>Reduces triglyceride levels

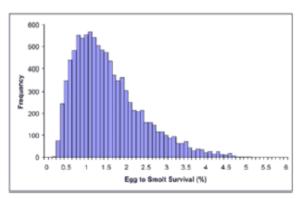
Triglyceride levels natural log transformed

Covariates: age, age<sup>2</sup>, sex, BMI & current smoker



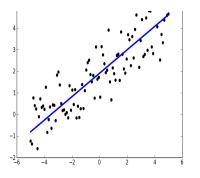
### **Analyzing Quantitative Variants**

- Most rare variant aggregate analysis methods can be performed on quantitative traits
- If phenotype data includes outliers or deviates from normality
  - Can increase type I errors



### **Rare Variant Aggregate Methods**

- Ideally should be performed in a regression framework
  - Logistic
  - Linear regression



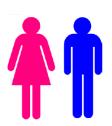
• Almost all methods have been extended to be implemented within a regression framework

### **Analyzing Quantitative Variants**

- For data that deviates from normality
  - Quantile-quantile normalization
- For data that includes outliers
  - Winsorize
- Don't winsorize and then normalize
- Instead of analyzing quantitative trait values
- Residual can be generated
  - If their our confounders which need to be controlled
    - Residuals are generated were confounders have been adjusted

### **Rare Variant Aggregate Methods**

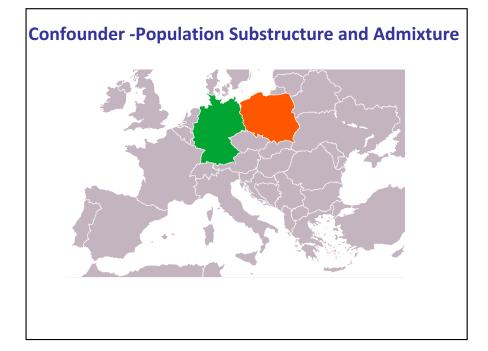
- Can control for covariates in the analysis which are potential confounders
  - Age
  - Sex
  - Body Mass Index (BMI)
  - Smoking pack years





### **Rare Variant Aggregate Methods**

- If proportion of cases and controls sampled from each populations is different
  - Can occur due to
    - Disease frequency is different between populations
    - Sloppy sampling
- Population substructure\admixture can cause detection of differences in variant frequencies within a gene which is due to sampling and not disease status
  - False positive findings can be increased

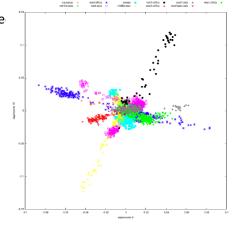


### **Example Pima Indians**



### **Rare Variant Aggregate Methods**

- Currently PCA or MDS are use to control for population substructure\admixture
  - Controls on the global level
  - May not be sufficient in particular for admixed populations



# Linear Mixed Models and Generalized linear Mixed Models

- Linear mixed models and their extension Generalized linear mixed models for binary traits
  - Can offer better control of type I error than linear and logistic regression
    - When observations are not independent
      - Related or cryptically related individuals are included in the sample
      - Population structure
- Models both fixed and random effects

### **Rare Variant Aggregate Methods**

- Best to obtain components to include in the regression model
  - using variants which are not in LD e.g. r<sup>2</sup><0.5 (prunned)</li>
  - covering a wide range of the allelic frequency spectrum e.g. >0.1%
- Success of PCA\MDS in controlling for population substructure\admixture can be evaluated through lambda and examining Quantile-Quantile (QQ) plots





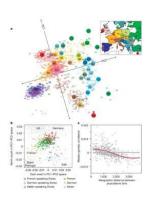
Genome-wide association studies (GWAS) - Part 2 More advanced topics: Linear Mixed Models and  $G \times G$  or  $G \times E$  interactions

### Heather J. Cordell

Population Health Sciences Institute Faculty of Medical Sciences Newcastle University, UK heather.cordell@ncl.ac.uk

### Population stratification and relatedness

Genes mirror geography within Europe



J Novembre et al. (2008) Nature 456(7218):98-101, doi:10.1038/nature07331

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WAS (Part 2)

rt 2) 3 / 3

### Linear Mixed Models (LMMs)

- Linear Mixed Models have been used for many years in the plant and animal breeding communities
- In the mid 1990s they became popular in the human genetics field, mostly for performing linkage analysis and estimating heritability
  - Using family (pedigree) data i.e. related individuals
- In recent years they have become popular in the genetic association studies field for:
  - Testing for association while accounting for varying degrees of relatedness
    - Close family relationships
    - Distant relationships and population stratification/substructure
  - Estimating the heritability accounted for various partitions of SNPs:
    - All SNPs typed on a GWAS panel
    - All typed SNPs and others in LD with them
    - Partitions of SNPs in various functional categories
  - Investigating genetic correlations between different traits
  - Predicting trait values in a new individual

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### Linear Mixed Models (LMMs)

- A linear mixed model is a statistical model in which the dependent variable is a linear function of both fixed and random independent variables
  - Known respectively as fixed and random effects
  - Fixed effects are considered 'fixed' at their measured values
  - Random effects are considered to be sampled from a distribution
- Recall the usual linear regression model

$$y = mx + c$$
 or  $y = \beta_0 + \beta_1 x$ 

• This model may also be written

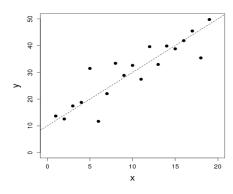
$$y_i = \beta_0 + \beta_1 x_i + \epsilon_i$$

- $y_i$  refers to the trait value of person i
- $x_i$  refers to the measured value of person i's predictor variable
- $\epsilon_i$  refers to the displacement from the regression line
  - i.e. the discrepency between the observed and the predicted y value

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### Linear Regression



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### Linear Mixed Models (LMMs)

- In linear regression we have  $y_i = \beta_0 + \beta_1 x_i + \epsilon_i$ 
  - Here  $\beta_0$  and  $\beta_1$  are fixed effects while  $\epsilon_i$  is a random error
- In matrix notation we can write this model:

$$\begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \end{bmatrix} = \begin{bmatrix} 1 & x_1 \\ 1 & x_2 \\ \vdots & \vdots \\ 1 & x_n \end{bmatrix} \begin{bmatrix} \beta_0 \\ \beta_1 \end{bmatrix} + \begin{bmatrix} \epsilon_1 \\ \epsilon_2 \\ \vdots \\ \epsilon_n \end{bmatrix}$$

$$ullet$$
 or  $\mathbf{y} = \mathbf{X}oldsymbol{eta} + oldsymbol{\epsilon}$ 

- ullet A LMM takes the form  ${f y}={f X}eta+{f Z}{f u}+{f \epsilon}$ 
  - ullet where ullet corresponds to a vector of random effects

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GWAS (Part 2

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### Linear Mixed Models (LMMs)

- E.g. suppose 2 fixed effects  $\beta_1$  and  $\beta_2$ , and 3 random effects
- Then  $\mathbf{y} = \mathbf{X}\boldsymbol{\beta} + \mathbf{Z}\mathbf{u} + \boldsymbol{\epsilon}$  corresponds to:

$$\begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \end{bmatrix} = \begin{bmatrix} x_{11} & x_{12} \\ x_{21} & x_{22} \\ \vdots & \vdots \\ x_{n1} & x_{n2} \end{bmatrix} \begin{bmatrix} \beta_1 \\ \beta_2 \end{bmatrix} + \begin{bmatrix} z_{11} & z_{12} & z_{13} \\ z_{21} & z_{22} & z_{23} \\ \vdots & \vdots & \vdots \\ z_{n1} & z_{n2} & z_{n3} \end{bmatrix} \begin{bmatrix} u_1 \\ u_2 \\ u_3 \end{bmatrix} + \begin{bmatrix} \epsilon_1 \\ \epsilon_2 \\ \vdots \\ \epsilon_n \end{bmatrix}$$

• or  $y_i = \beta_1 x_{i1} + \beta_2 x_{i2} + u_1 z_{i1} + u_2 z_{i2} + u_3 z_{i3} + \epsilon_i$ 

LMMs in genetics

- In genetics we generally work with two equivalent forms of LMM
- ullet One is:  $\mathbf{y} = \mathbf{X}oldsymbol{eta} + \mathbf{Z}\mathbf{u} + oldsymbol{\epsilon}$ 
  - The random effect u<sub>I</sub> corresponds to a scaled additive effect of causal variant (locus) I
    - Assuming many (m) such causal variants all across the genome
  - $\bullet$  The random effects  $u_{l}$  all have variance  $\sigma_{u}^{2}$  and are uncorrelated with each other
    - So  $\mathbf{u} = (u_1, u_2, \dots u_m) \sim N(0, \mathbf{I}\sigma_u^2)$
  - **Z** is a standardized genotype matrix i.e.  $z_{il}$  takes value

$$\left(\frac{-2f_l}{\sqrt{2f_l(1-f_l)}}, \frac{(1-2f_l)}{\sqrt{2f_l(1-f_l)}}, \frac{2(1-f_l)}{\sqrt{2f_l(1-f_l)}}\right)$$

if individual i has genotype (qq, Qq, QQ)

• where  $f_l$  is the frequency of allele Q at locus l

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### LMMs in genetics

ullet The other form is:  $oldsymbol{y} = oldsymbol{X}eta + oldsymbol{g} + oldsymbol{\epsilon}, \quad ext{or}$ 

$$y_i = \sum_{k} \beta_k x_{ik} + g_i + \epsilon_i$$

- Where the  $\beta_k$  are k fixed effects (e.g. covariates or SNPs to be tested for association), and random effect  $g_i = \sum_{l=1}^m z_{il} u_l$  is the total genetic effect in individual i, summed over all the causal loci
- Here,  $g_i$  is considered as a random effect operating in individual i
  - The vector of random effects **g** takes distribution  $\mathbf{g} \sim N(0, \mathbf{G}\sigma_a^2)$ 
    - Where G=ZZ'/m is the genetic relationship matrix (GRM) between individuals at the causal loci
    - $\sigma_a^2 = m\sigma_u^2$  is the total additive genetic variance
- For family data (close relatives), the expected values of the elements of  ${\bf G}$  are equal to twice the kinship coefficients  $\Phi_{ij}$  i.e.  ${\bf G}$  is equal to twice the kinship matrix  ${\bf \Phi}$ 
  - Models their relatedness at the causal loci (and elsewhere)

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### Use of LMMs in genetics

- The formulation  $\mathbf{y} = \mathbf{X}\boldsymbol{\beta} + \mathbf{g} + \boldsymbol{\epsilon}$  is known as the **Animal Model** and has been used extensively in plant and animal breeding
  - Mostly to predict the *breeding values*  $g_i$  in order to inform breeding strategies
    - E.g. to increase milk yield, meat production etc. etc.
  - Similar approaches could be used for prediction of trait values given genotype data
- In the mid 1990s it became popular in human genetics as the backbone of variance components linkage analysis
- Now commonly used in association analysis (GWAS)
  - To correct for relatedness, when testing for association

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### Testing for association using LMMs

- Idea is to test a fixed SNP effect  $\beta_1$ 
  - $\bullet$  While including a random effect  $\gamma_i$  that models relatedness
- Fit regression model:  $y_i = \beta_0 + \beta_1 x_i + \gamma_i$ 
  - y is the trait value
  - x is a variable coding for genotype at the test SNP (e.g. an allele count, coded 0, 1, 2 for genotypes 1/1, 1/2, 2/2)
  - $\gamma_i = g_i + \epsilon_i$
  - We assume  $\gamma \sim MVN(0, \mathbf{V})$  where variance/covariance matrix  $\mathbf{V}$  follows standard variance components model
    - Variance/covariance matrix structured as:

$$V_{ij} = \sigma_a^2 + \sigma_e^2 \quad (i = j)$$
  
 $V_{ij} = 2\Phi_{ij}\sigma_a^2 \quad (i \neq j)$ 

•  $\sigma_a^2$ ,  $\sigma_e^2$  represent the additive polygenic variance (due to all loci) and the environmental (=error) variance, respectively

### Testing for association using LMMs

- LMMs were first (?) applied in human genetics by Boerwinkle et al. (1986) and Abney et al. (2002)
- Chen and Abecasis (2007) implemented them via the "FAmily based Score Test Approximation" (FASTA) in the MERLIN software package
  - Closely related to earlier QTDT method (Abecasis et al. 2000a;b)
     which implements a slightly more general/complex model
  - FASTA was also implemented in GenABEL, along with a similar test called GRAMMAR (Aulchenko et al. 2007)

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### Estimating the genetic relationship matrix

- ullet These early implementations calculated the kinship matrix ullet on the basis of known (theoretical) kinships constructed from known pedigree relationships
- Amin et al. (2007) proposed instead estimating the kinships based on genome-wide SNP data
  - Ideally we want to use G=ZZ'/m, the genetic relationship matrix (GRM) between individuals at the causal loci
  - Since we don't know the causal loci, we approximate G by A, the overall GRM between individuals
    - Various different ways to estimate this, usually based on scaled (by allele frequency) matrix of identity-by-state (IBS) sharing

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### Software implementations

- Main difference between them is the precise computational tricks used to speed up the calculations
  - And the convenience/ease of use
    - See comparison in Eu-Ahsunthornwattana et al. (2014) PLoS Genetics 10(7):e1004445
- Association testing also implemented in some more general packages
  - GCTA

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- DISSECT
- EPACTS
- BOLT-LMM (Loh et al. 2016) uses a slightly different approach, based on a Bayesian implementation of LMM formulation 1:

$$y = X\beta + Zu + \epsilon$$

 Model can also be extended to bivariate traits (Korte et al. 2012, Nat Genet 44:1066-1071), implemented in MTMM/ASREML and DISSECT

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### Estimating the genetic relationship matrix

- Once you move to estimating the GRM, you are no longer limited to using family data
- Kang et al. (2010) and Zhang et al. (2010) suggested applying the approach to apparently unrelated individuals
  - As a way of accounting for population substructure/stratification
  - Also proposed applying to binary traits (case/control coded 1/0)
  - Implemented in EMMAX and TASSEL software, respectively
- Subsequently a number of other publications/software packages have implemented essentially the same model
  - FaST-LMM (Lippert et al. 2011)
  - GEMMA (Zhou and Stephens 2012)
  - GenABEL (GRAMMAR-Gamma) (Svishcheva et al. 2012)
  - MMM (Pirinen et al. 2013)
  - MENDEL (Zhou et al. 2014)
  - RAREMETALWORKER
     (http://genome.sph.umich.edu/wiki/RAREMETALWORKER)

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### Binary traits

- ullet For binary traits, coding cases and controls as a 1/0 quantitative trait is not optimal
  - Though in practice it seems to work reasonably well
- LTMLM (Hayeck et al. 2015) and LEAP (Weissbrod et al. 2015) instead use an underlying *liability model* to improve power
  - Assuming known disease prevalence
- Chen et al. (2016) [AJHG 98:653-66] showed that high levels of population stratification can invalidate the analysis, when applied to a case/control sample
  - Resulting in a mixture of **inflated** and **deflated** test statistics
  - Developed GMMAT software to address this problem
  - CARAT software (Jiang et al. 2016, AJHG 98:243-55) also appears to address this problem effectively
- SAIGE software (Zhou et al. 2018, AJHG 50(9):1335-1341)
   implements a mixed model association test that deals with large case-control imbalance

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### Elucidating genetic architecture

- Seminal paper by Yang et al. (2010) [Nat Genet 42(7):565-9]
- Showed that by framing the relationship between height and genetic factors as an LMM, 45% of variance could be explained by considering 294,831 SNPs simultaneously
  - So-called 'SNP heritability' or 'chip heritability'
  - $\bullet$  Demonstrated that modelling effects at all genotyped SNPs explained the 'known' heritability ( $\approx 80\%$ ) much better than just the top SNPs from GWAS
- Moreover, if you estimate effects of additional SNPs in LD with the genotyped SNPS, the variance explained goes up to 84% (s.e. 16%), consistent with 'known' value
- Subsequently many papers have shown similar results for a variety of complex traits

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### Partitioning variance

- The same formulation can be used to partition the variance explained by different subsets of SNPs
  - Yang et al. (2010) partitioned variance onto each of the 22 autosomes using formulation

$$\mathbf{y} = \mathbf{X}\boldsymbol{\beta} + \sum_{c=1}^{22} \mathbf{g_c} + \epsilon$$
 with  $\mathbf{V} = \sum_{c=1}^{22} \mathbf{A_c} \sigma_c^2 + \mathbf{I} \sigma_e^2$ ,

where  $\mathbf{g}_c$  is a vector of effects attributed to the cth chromosome, and  $\mathbf{A}_c$  is the GRM estimated from SNPs on the cth chromosome

- Slight adjustment is needed for estimating variance explained by SNPs on chromosome X
- Similar partitioning can be used to examine subsets of SNPs defined in other ways e.g. according to MAF or functional annotation

### Elucidating genetic architecture

Basic idea is to use formulation

$$y = X\beta + g + \epsilon$$

with  $\mathbf{g} \sim N(0, \mathbf{A}\sigma_a^2)$  and  $\epsilon \sim N(0, \mathbf{I}\sigma_e^2)$  so  $\mathbf{V} = \mathbf{A}\sigma_a^2 + \mathbf{I}\sigma_e^2$ 

- A is the GRM between individuals, estimated using all genotyped SNPs
- $\sigma_a^2$  and  $\sigma_e^2$  estimated using REML (or MLE)
- Thus we can estimate heritability accounted for by the genotyped SNPs as  $\sigma_a^2/(\sigma_a^2+\sigma_e^2)$
- Implemented in several software packages including GCTA and DISSECT
  - ALBI software (Schweiger et al. 2016, AJHG 98:1181-1192) can then be used to construct accurate confidence intervals for the heritability

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### Other approaches

- Some recent work has focussed on estimating (a) heritability explained by sets of SNPs, and (b) genetic correlations across traits, using summary statistics only
  - Bulik-Sullivan et al. (2015) [Nat Genet 47:291-295]
  - Bulik-Sullivan et al. (2015) [Nat Genet 47:1236-1241]
    - Clever idea that allows the variance component parameters to be estimated via a simple regression on 'LD Scores'

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### Gene-gene (and gene-environment) interactions

- GWAS have been extraordinarily successful at detecting genetic locations harboring genes associated with complex disease
  - But the SNPs identified do not account for the known (estimated) heritability for most disorders
  - Could G×G and G×E effects account for part of the 'missing heritability'?
    - Zuk et al. (2012) PNAS 109:1193-1198
- Effects operating through interactions may not be visible unless you stratify by or take account of the interacting genetic (or environmental) factors
  - By modelling interactions, we hope to increase our power to detect loci with weak marginal effects
- Phenomenon of biological interest?
  - Identifying genes that interact to cause disease could help us understand the mechanisms and pathways in disease progression

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### Interaction

Expected trait values (log odds of disease) take the form:

( )	,	
	Factor 2	
Factor 1	1	0
1	$\beta_0 + \beta_1 + \beta_2 + \beta_{12}$	$\beta_0 + \beta_1$
0	$\beta_0 + \beta_2$	$\beta_0$

- $\beta_0$ ,  $\beta_1$ ,  $\beta_2$ ,  $\beta_{12}$  are regression coefficients (numbers) that can be estimated from real data
  - Having factor 1 adds  $\beta_1$  to your trait value
  - Having factor 2 adds  $\beta_2$  to your trait value
  - Having both factors adds an additional  $\beta_{12}$  to your trait value ⇒ Implies that the overall effect of two variables is greater (or less) than the 'sum of the parts'
  - The 'effect' of factor 2 is different in the presence/absence of factor 1
- Suppose no main effects ( $\beta_1 = \beta_2 = 0$ )

	_ ,		
	Factor 2		
Factor 1	1	0	
1	$\beta_0 + \beta_{12}$	$\beta_0$	
0	$\beta_0$	$\beta_0$	

 Trait value only differs from baseline if both factors present GWAS (Part 2)

### Definition of (pairwise) interaction

- Statistical interaction most easily described in terms a of (logistic) regression framework
  - Supppose  $x_1$  and  $x_2$  are binary factors whose presence/absence (coded 1/0) may be associated with a disease outcome
  - Logistic regression models their effect on the log odds of disease as:

$$\log \frac{p}{1-p} = \beta_0 + \beta_1 x_1$$

 $\log \frac{p}{1-p} = \beta_0 + \beta_2 x_2$ 

Marginal effect of factor 1

Marginal effect of factor 2

$$\log \frac{p}{1-p} = \beta_0 + \beta_1 x_1 + \beta_2 x_2$$

 $\log \frac{p}{1-p} = \beta_0 + \beta_1 x_1 + \beta_2 x_2 \qquad \log \frac{p}{1-p} = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \frac{\beta_{12}}{\beta_{12}} x_1 x_2$ 

Main effects of factors 1 and 2

Main effects and interaction term

- For quantitative traits, use linear regression (replace  $\log \frac{p}{1-p}$  with y)
- For modelling as an LMM, add in a random effect  $\gamma$

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### Gene-gene interaction (epistasis)

- However SNPs are not binary, but rather take 3 levels according to the number of copies (0.1.2) of the susceptibility allele possessed
- Most general 'saturated' (9 parameter) genotype model allows all 9 penetrances to take different values
  - Via modelling log odds in terms of:
    - A baseline effect (β<sub>0</sub>)
    - Main effects of locus  $G(\beta_{G_1}, \beta_{G_2})$
    - Main effects of locus  $H(\beta_{H_1}, \beta_{H_2})$
    - 4 interaction terms

		Locus H	
Locus G	2	1	0
2	$\beta_0 + \beta_{G_2} + \beta_{H_2} + \beta_{22}$	$\beta_0 + \beta_{G_2} + \beta_{H_1} + \beta_{21}$	$\beta_0 + \beta_{G_2}$
1	$\beta_0 + \beta_{G_1} + \beta_{H_2} + \beta_{12}$	$\beta_0 + \beta_{G_1} + \beta_{H_1} + \beta_{11}$	$\beta_0 + \beta_{G_1}$
0	$\beta_0 + \beta_{H_2}$	$\beta_0 + \beta_{H_1}$	$\beta_0$

• Corresponds in statistical analysis packages to coding  $x_1$ ,  $x_2$  (0,1,2) as a "factor"

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### Gene-gene interaction

- Alternatively we can assume additive effects of each allele at each locus:
  - Corresponds to fitting

$$\log \frac{p}{1-p} = \beta_0 + \beta_G x_1 + \beta_H x_2 + \frac{\beta_{GH}}{\beta_{GH}} x_1 x_2$$

with  $x_1$ ,  $x_2$  coded (0,1,2)

		Locus H	
Locus G	2	1	0
2	$\beta_0 + 2\beta_G + 2\beta_H + 4\beta_{GH}$	$\beta_0 + 2\beta_G + \beta_H + 2\beta_{GH}$	$\beta_0 + 2\beta_G$
1	$\beta_0 + \beta_G + 2\beta_H + 2\beta_{GH}$	$\beta_0 + \beta_G + \beta_H + \beta_{GH}$	$\beta_0 + \beta_G$
0	$\beta_0 + 2\beta_H$	$\beta_0 + \beta_H$	$\beta_0$

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### Gene-environment (G×E) interactions

The same regression model

$$\log \frac{p}{1-p} = \beta_0 + \beta_G x_1 + \beta_H x_2 + \frac{\beta_{GH}}{\beta_{GH}} x_1 x_2$$

can be used to model interaction between a genetic factor  ${\it G}$  and an environmental factor  ${\it H}$ 

- With the environmental variable  $x_2$  coded in binary fashion (e.g. smoking) or quantitatively (e.g. age)
- Focus of analysis is often risk estimation
  - Estimating genetic risks in particular environments
  - Estimating effect of environmental factor on particular genetic background
    - Important for treatment/screening strategies and public health interventions
- For G×G, focus of interest is more related to
  - Increasing power to detect an effect (by taking into account the effects of other genetic loci)
  - Modelling the biology, especially related to the joint action of the loci

### Change of scale

- Transformations of outcome variable *y* can change whether or not the predictor variables interact
  - Due to definition of interaction as departure from a linear model for the effects of  $x_1$  and  $x_2$ , for predicting y
    - Two SNPs that interact on the log odds scale may not interact on the penetrance scale (and vice versa)
    - Makes biological interpretation of resulting interaction model difficult
- Much discussion in the literature
  - Siemiatycki and Thomas (1981) Int J Epidemiol 10:383-387; Thompson (1991) J Clin Epidemiol 44:221-232
  - Phillips (1998) Genetics 149:1167-1171; Cordell (2002) Hum Molec Genet 11:2463-2468
  - McClay and van den Oord (2006) J Theor Biol 240:149-159; Phillips (2008) Nat Rev Genet 9:855-867
  - Clayton DG (2009) PLoS Genet 5(7): e1000540; Wang, Elston and Zhu (2010) Hum Hered 70:269-277
- Bottom line is, little direct correspondence between statistical interaction and biological interaction
  - In terms of whether, for example, gene products physically interact
- However, existence of statistical interaction does imply both loci are "involved" in disease in some way
  - Good starting point for further investigation of their (joint) action

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### Testing association and/or interaction

• Go back to binary coding of genetic (and/or environmental) factors

$$\log \frac{p}{1-p} = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_{12} x_1 x_2$$

- 3df test of  $\beta_1 = \beta_2 = \beta_{12} = 0$  tests for association at both loci (or both variables), allowing for their possible interaction
- 2df test of  $\beta_2 = \dot{\beta}_{12} = 0$  tests for association at locus 2, while allowing for possible interaction with locus (or variable) 1
- 1df test of  $\beta_{12}=0$  tests the interaction term alone
- Depending on circumstances, any of these tests may be a sensible option
- Most tests of interaction/joint action can be thought of as a version of one or other of these tests
  - Although different tests vary in their precise details
  - And their relationship to the logistic regression formulation not always clearly described

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GWAS (Part 2

### $G \times G$ versus $G \times E$ in the context of GWAS

- Typically GWAS measure thousands if not millions of genetic variants
  - But only a few (tens or at most 100s) of environmental factors
- Feasible to consider all G×E combinations
- All pairwise G×G combinations possible, but much more time consuming
  - And leads to greater multiplicity of tests
  - Also, why stop at 2-way interactions?
    - Could look at all 3 way, 4 way etc. combinations
    - Scale of problem quickly gets out of hand
    - $\bullet$  Less obvious reason to do this for  $G{\times}E...$

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### Case-only analysis

- Piergorsh et al. 1994; Yang et al. 1999; Weinberg and Umbach 2000
- ullet Several authors have shown that, for binary predictor variables, a test of the interaction term  $eta_{12}$  in the logistic regresssion model

$$\log \frac{p}{1-p} = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_{12} x_1 x_2$$

can be obtained by testing for correlation (association) between the genotypes at two separate loci, within the sample of cases

- Gains power from making assumption that genotypes (alleles) at the two loci are uncorrelated in the population
  - So only really suitable for unlinked or loosely linked loci (since closely linked loci are likely to be in LD)
- Alternatively contrast the genotype correlations in cases with those seen in controls (--fast-epistasis in PLINK)

 $G \times G$  in the context of GWAS

- Many recent publications have focussed on finding clever computational tricks to speed up exhaustive search procedure
  - BOOST (Wan et al. (2010) AJHG 87:325-340)
  - SIXPAC (Prabhu and Pe'er (2012) Genome Res 22:2230-2240)
  - Kam-Thong et al. (2012) Hum Hered 73:220-236 (GPUs)
  - Fråanberg et al. (2015) PLOS Genetics 11(9):e1005502
     "Discovering genetic interactions in large-scale association studies by stage-wise likelihood ratio tests"
- Or have proposed filtering based on single-locus significance or other (biological or statistical) considerations
  - Reduces multiple testing burden, improves interpretability
- Or have proposed testing at the gene level rather than the SNP level
  - Ma et al. (2013) PLoS Genet 9(2): e1003321
    - Compared 4 different tests that combine P values from pairwise (SNP x SNP) interaction tests
    - Showed that the truncated tests did best
    - Presented an application only considering gene pairs known to exhibit protein-protein interactions

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### Testing correlation between loci

- A similar idea is implemented in EPIBLASTER (Kam-Thong et al. 2011; EJHG 19:465-571)
- Wu et al. (2010) (PLoS Genet 6:e1001131) also proposed a similar approach though needs adjustment to give correct type I error rates
- See also Joint Effects (JE) statistics (Ueki and Cordell 2012; PLoS Genetics 8(4):e1002625)
- All these methods test whether correlation exists (case-only) or is different in cases and controls (case/control), via testing a log OR for association between two loci
  - $\bullet$  However, the log OR for association ( $\lambda$ ) encapsulates a slightly different quantity between the different methods
- All implemented (along with standard logistic and linear regression) in CASSI
  - http://www.staff.ncl.ac.uk/richard.howey/cassi/

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### Empirical evidence for $G \times G$ interactions

- Epistasis among HLA-DRB1, HLA-DQA1, and HLA-DQB1 in multiple sclerosis (Lincoln et al. 2009 PNAS 106:7542-7547)
- HLA-C and ERAP1 in psoriasis (Strange et al. 2010)
- HLA-B27 and ERAP1 in ankylosing spondylitis (Evans et al. 2011)
- BANK1 and BLK in SLE (Castillejo-Lopez et al. 2012)
- Gusareva et al. (2014) found a reasonably convincing (partially replicating) interaction between SNPs on chromosome 6 (KHDRBS2) and 13 (CRYL1) in Alzheimer's disease
- Dai et al. (2016) [AJHG 99:352-365] identified 3 loci simultaneously interacting with established risk factors gastresophageal reflux, obesity and tobacco smoking, with respect to risk for Barrett's esophagus

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### Empirical evidence for G×G interactions

- Hemani et al. 2014 (Nature 508:249-253) found 501 instances of epistatic effects on gene expression, of which 30 could be replicated in two independent samples
  - Many SNPs are close together, could represent haplotype effects?
  - Or the effect of a single untyped variant?
  - See caveats in
    - Wood et al. (2014) Nature 514(7520):E3-5. PMID:25279928
    - Fish et al. (2016) Am J Hum Genet 99(4):817830. PMID:27640306

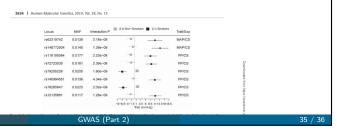
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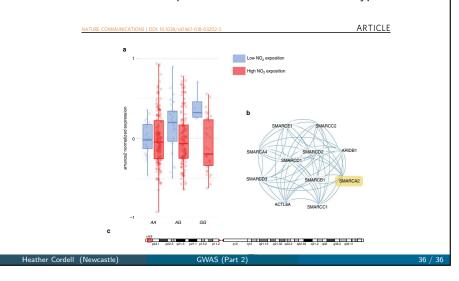
### Empirical evidence for $G \times E$ interactions

- Myers et al. (2014) Hum Mol Genet 23(19): 5251-9 "Genome-wide Interaction Studies Reveal Sex-Specific Asthma Risk Alleles"
- Small et al. (2018) Nat Genet 50(4): 572-580 "Regulatory Variants at KLF14 Influence Type 2 Diabetes Risk via a Female-Specific Effect on Adipocyte Size and Body Composition"
- Sung et al. (2019) Hum Molec Genet 28(15): 2615-2633 "A multi-ancestry genome-wide study incorporating gene-smoking interactions identifies multiple new loci for pulse pressure and mean arterial pressure."



### Empirical evidence for $G \times E$ interactions

• Favé et al. (2018) Nat Commun 9(1): 827 "Gene-by-environment Interactions in Urban Populations Modulate Risk Phenotypes"



# Power Analysis for Single and Rare Variant Aggregate Association Analyses

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### Power and Sample Size Estimation for Case-Control Data

- The correct  $\alpha$  must be use for sample size estimation/power analysis
- Type I ( $\alpha$ ) the probability of rejecting the null hypothesis of no association when it is true
- Due to multiple testing a more stringent value than  $\alpha$ =0.05 is used in order to control the Family Wise Error Rate

### Why Estimate Sample Sizes and/or Power?

- Not wasting your time and money
  - Carrying out a study for which you will never find a true association due to inadequate sample sizes
- Almost always necessary for grant proposals
  - Usually will be denied funding if cannot demonstrate planned study has adequate power

### Power and Sample Size Estimation for Case-Control Data

- GWAS of common variants where each variant is test separately
  - $-\alpha = 5 \times 10^{-8}$  (Bonferroni Correction for testing 1,000,000 variant sites)
  - Shown to be a good approximation for the effective number of tests
    - Valid even when more than 1.000,000 variant sites tested
  - Effective number of tests is dependent of the LD structure
- Analysis of individual variants for whole genome sequence data
  - More rare variants than common variants
    - Also have lower levels of LD than between common variants
  - The number of effective tests is higher than for analysis limited to common variants
  - $-\alpha$  yet to be determined

### **Determining Genome-wide Significance Levels**

- Using genotypes from the Wellcome Trust Case-Control Consortium
- Dudbridge and Gusnato, Genet Epidemiol 2008
- Estimated a genome wide significance threshold for the UK European population
- By sub-sampling the genotypes at increasing densities and using permutation to estimate the nominal p-value for 5% family-wise error
- Then extrapolating to infinite density
- The genome wide significance threshold was estimated to be ~7.2X10-8
- Estimate is based on LD structure for Europeans
  - Not sufficiently stringent for populations of African Ancestry

# Power and Sample Size for Aggregate Rare Variant Tests

- For gene based methods a Bonferroni correction for the number of genes/regions tested is used
  - e.g. 20,000 genes significance level  $\alpha = 2.5 \times 10^{-6}$ 
    - Can use a less stringent criteria
      - Not all genes have two or more variants
        - » Divide 0.05 by number of genes tested
    - If units other than genes used may have to use a more stringent
- Little LD between variants in separate genes
  - Little to no correlation between tests
    - Bonferroni correction is not overly stringent

### **Power and Sample Size for Replication Studies**

- For replication studies can base the significance level (α)
- On the number of genes/variants being brought from the discovery (stage I) study
- To replication (stage II)
- For example is hypothesized that 20 genes and 80 independent variants will be brought to stage II
  - A Bonferroni correct can be made for performing 100 tests
    - An  $\alpha = 5.0 \times 10^{-3}$  cab be used for a family wise error rate of 0.05

# Estimating Power/Sample Sizes For Individual Variants

- Can be obtained analytically
- Information necessary
  - Prevalence
  - Risk allele frequency
  - Effect size (odds ratio-for case control data)
  - Genetic model for the susceptibility variant
    - Recessive (γ<sub>1</sub>=1)
    - Dominant  $(\gamma_2 = \gamma_1)$
    - Additive  $(\gamma_2=2\gamma_1-1)$
    - Multiplicative (γ<sub>2</sub>=γ<sub>1</sub><sup>2</sup>)

# Estimating Power/Sample Sizes For Individual Variants

- Usually information on disease prevalence is known from epidemiological data
- A range of risk allele allele frequencies and effect sizes are used
- A variety of genetic models are also used
  - Dominant
  - Additive
  - Multiplicative

### **Armitage Trend Test**

- Power and Sample size
  - Calculated under different models
    - Where γ is the relative risk
      - Multiplicative
      - » γ<sub>2</sub>=γ<sub>1</sub><sup>2</sup>
      - Additive
        - $\nu \gamma_2 = 2\gamma_1 1$
      - Dominant
        - » γ<sub>2</sub>=γ<sub>1</sub>
      - Recessive
        - » γ<sub>1</sub>=1

### **Gamma is the Relative Risk**

- Many programs work with the relative risk (y)
- Relative risk only approximates odds ratio when disease is rare
  - Not appropriate for common trait
- Example risk variant and marker allele frequency 0.01
  - D' and  $r^2=1$

Disease Prevalence	1/2 RR=1.5	2/2 RR=1.5
0.01	1.51	1.51
0.10	1.59	1.59
0.20	1.71	1.71

Disease Prevalence	1/2 RR=1.5	2/2 RR=2.25
0.01	1.51	2.28
0.10	1.59	2.61
0.20	1.71	3.25

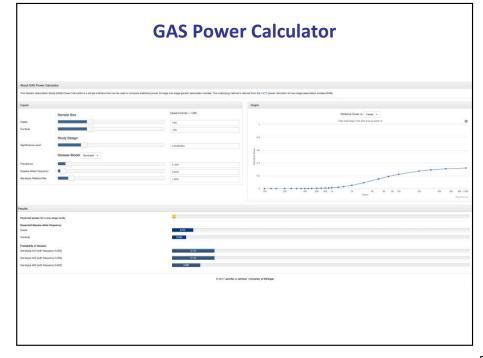
### **Armitage Trend Test - Power Calculations**

- Information need
  - Population prevalence
  - Genetic Model
  - Risk allele frequency
- Lools
  - http://ihg.gsf.de/cgi-bin/hw/power2.pl
  - Reference Slager and Schaid 2001

### **Armitage Test for Trend** sample size approximations for Armitage's test for trend: Disease prevalence High risk allele frequency 0.05 Type 1 error (alpha) 0.00000005 Power (1- beta) 0.8 Gamma 1 Cases / (cases + controls) 0.5 Cases necessary = 1502 Controls necessary = 1502 Cases and controls necessary = 3004 Gamma (genotypic relative risk): Under a multiplicative model, gamma2 = gamma1^2; under a additive model, gamma2 = 2 \* gamma1 - 1; under a dominant model, gamma2 = gamma1; under a recessive model, gamma1 = 1. Slager SL, Schaid DJ: Case-control studies of genetic markers: Power and sample size approximations for Armitage's test for trend. Hum Hered 52, 149-153 (2001). Freidlin B, Zheng G, Li Z, Gastwirth JL: Trend tests for case-control studies of genetic markers: Power, sample size and robustness. Hum Hered 53, 146-152 (2002). Tim M. Strom

### **Genetic Association Study (GAS) Power Calculator**

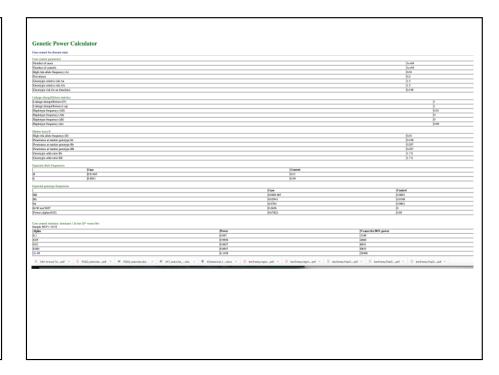
- <a href="http://csg.sph.umich.edu/abecasis/cats/gas\_power\_calculator/i">http://csg.sph.umich.edu/abecasis/cats/gas\_power\_calculator/i</a> ndex.html
- A one-stage study power calculator
  - Which was derived from CaTs
    - Which is to perform two-stage genome wide association studies
      - Skol et al. 2006
- Cochran Armitage Trend Test
- Displays Graphs of results



### **Genetic Power Calculator**

- http://zzz.bwh.harvard.edu/gpc/
- S Purcell & P Sham
- Uses the methods described in Sham PC et al. (2000) Am J Hum Genet 66:1616-1630
  - VC QTL linkage for sibships
  - VC QTL association for sibships
  - VC QTL linkage for sibships conditional on the trait
  - TDT for discrete traits
  - Case-Control for discrete traits
  - TDT for quantitative traits
  - Case-Control quantitative traits
- Although input is relative risk
  - Displays odds ratios

### **Genetic Power Calculator** Case - control for discrete traits High risk allele frequency (A) : 0.01 (0 - 1) : 0.2 (0.0001 - 0.9999)Prevalence Genotype relative risk Aa : 1.5 (>1) Genotype relative risk AA : 1.5 ( >1 ) (0 - 1)D-prime (0 - 1)Marker allele frequency (B) : 0.01 Number of cases (0 - 10000000)Control : case ratio : 1 (>0) ( 1 = equal number of cases and controls) ☑ Unselected controls? (\* see below) User-defined type I error rate : 0.00000005 (0.00000001 - 0.5) User-defined power: determine N : 0.80 (0 - 1) (1 - type II error rate) Process Reset Created by Shaun Purcell 24.Oct.2008



### **PAWE**

- Power Association With Errors
  - Will give same results for case-control studies of discrete traits as
     Genetic Power Calculator when calculations are done without errors
- Four different error models can be used
  - See online documentation for complete explanation
- Can either perform:
  - Power calculations for a fixed sample size
  - Sample size calculations for a fixed power
- The genotype frequencies can be generated either using a:
  - Genetic model free method or
  - Genetic model based method

### Quanto

- Provides sample size and power calculations for
- Genetic and environmental main effects
- Interactions
  - Gene x gene
  - Gene x environment
- Sample & power calculations can be carried for:
  - Case-control
    - Unmatched
    - Matched
  - Case-sibling
  - Case-parent (trios)
    - Quantitative
    - Qualitative
  - Independent sample of individuals
    - Quantitative traits
      - Assumption sampled from a random population

### Linkage Disequilibrium (LD)

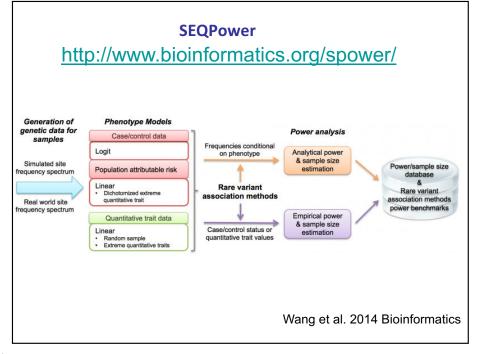
- Power will be reduced if causal variant is not in perfect LD (r<sup>2</sup>=1) with the tag SNP
- Can adjust sample size when r<sup>2</sup> <1 to increase power to the same level as when r<sup>2</sup>=1
- Can estimate sample size when r<sup>2</sup>≠1
  - $-N/r^2=N'$
  - Valid only for multiplicative model
  - (Pritchard and Przeworski, 2001)
- Power calculation almost always assume that r<sup>2</sup>=1

# Power Analysis for Rare Variant Aggregate Association Tests

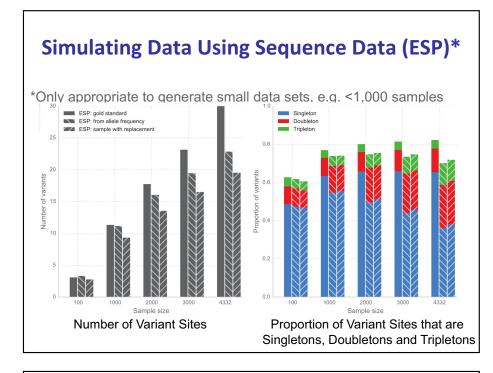
- Many unknown parameters must be modeled
  - Allelic architecture within a genetic region
    - Varied across genes and populations
  - Effects of variants within a region
    - Fixed or varied effect sizes of causal variants
    - Bidirectional effect of variants
    - Proportion of non-causal variants
- Power usually must be estimated empirically
- Simplified assumptions can be made to obtain analytical estimates
  - All variants have the same effect size
  - No non-causal variants

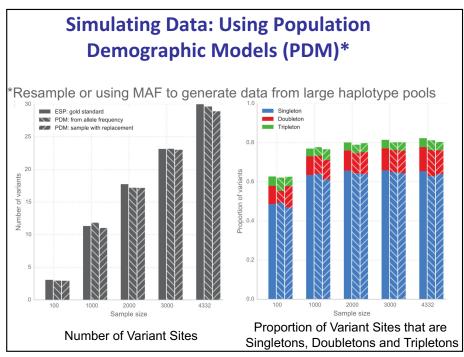
### **SKAT Power Calculator**

- R Library
- Provides a haplotype matrix
  - 10,000 haplotypes over 200kb region
  - Simulated using a calibrated coalescent model (cosi)
  - Mimicking linkage disequilibrium structure of European ancestry
  - User can also provide haplotype data
- Power and sample size calculations for binary and quantitative traits
- User specify proportion of variants that increase or lower risk



### **Does Generating Variant Data Using the European Population Demographic Model Perform Well?** Distribution of number of variants per gene Simulated Data **FSP Data** 1600 1600 1400 1400 1200 1000 1000 800 600 600 400 400 Simulated variant counts based on Simulated variant counts based haplotype pool down-sampled to ESP on the entire simulated population





## Simulation Studies to Evaluate Power for Rare Variant Association Studies

- It is unknown which genes are important in disease etiology
  - Correct allelic architecture is unknown
- Can get a better understanding of power to detect associations by generating variants for the entire exome
- Use a variety of disease models
  - Odds ratios
  - Proportion of pathogenic variants
- Analyze of all genes
  - e.g. those with 3 or more variant sites
- Determine power as the proportion of genes that meet exome-wide significance (alpha=2.5x10<sup>-6</sup>)

### **Power Analysis**

- For tests of individual variants
  - Power depended on sample size, disease prevalence, minor allele frequency, genetic model and variant effect size
- For rare variants (aggregate association tests)
  - Also dependent on the allelic architecture
    - Cumulative variant frequency within analyzed region
    - Proportion of causal variants
      - How much contamination by non-causal variants
    - Effect sizes the same the same or different across gene regions
      - Effects of variants in the same or different directions
        - » Protective and detrimental
        - » Increase and decrease quantitative trait values

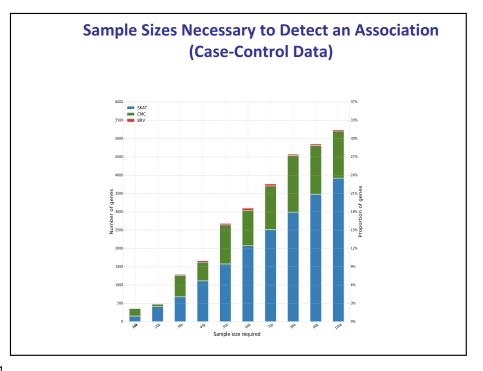
# Power Analysis Rare Variants (Aggregate Association Tests)

- Power will not only vary between traits greatly
- The power to detect an association will also vary drastically between genes
- For some genes even with hundreds of thousands of samples power will still be low, while for others a few thousand samples may be sufficient

# How Large of a Sample Size is Necessary to Detect Rare Variant Associations? Data generated on 18,397 genes Variant data simulated using a European population demographic model Gazave et al. 2013 Every missense, nonsense and splice with a MAF≤ 1% assigned an odds ratio of 1.5

• Sample sizes to detect X number of genes determined for

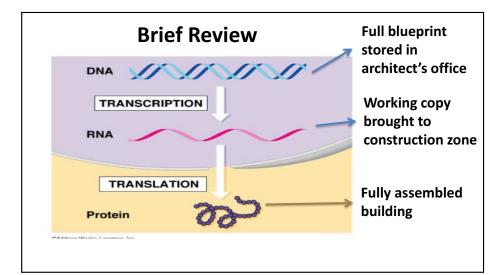
 $-\alpha = 2.5 \times 10^{-6}$ - power=0.8

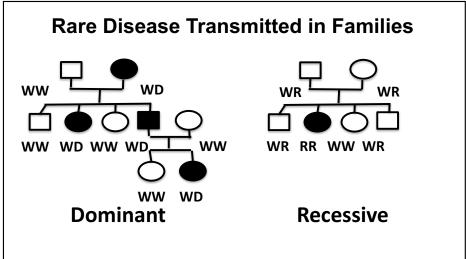


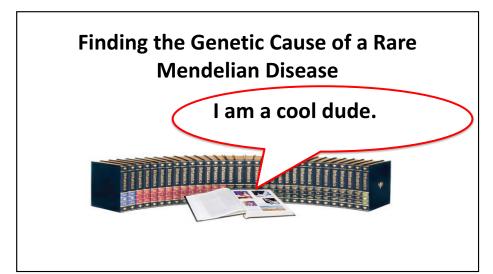
# Integrative Approaches in Biobanks : Getting to Biological Mechanisms of Disease

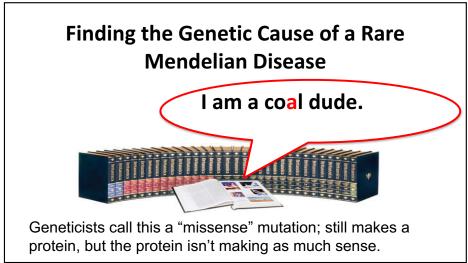
Nancy J. Cox, PhD Vanderbilt Genetics Institute Vanderbilt University Medical Center

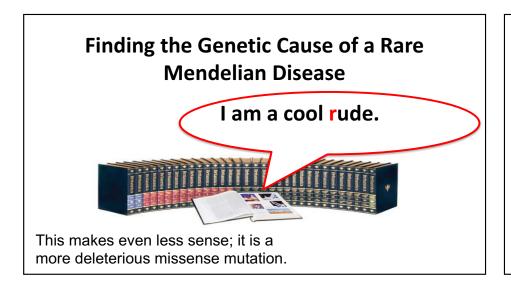
### **But First Some Review**

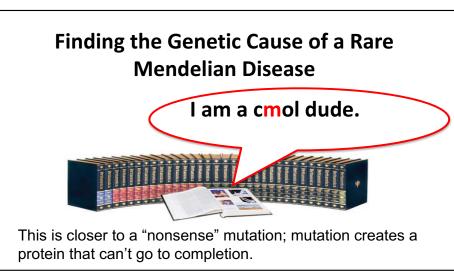












# Finding the Genetic Cause of a Rare Mendelian Disease

I am a fool dude.



This might be considered a "gain-of-function" mutation. The protein is active – but is doing something entirely new.

### **Common Diseases**

- Are familial, in that the risk of disease in a relative of an affected person is higher than the risk in the general population, but the transmission is not simple
- Many genetic and non-genetic risk factors contribute to common diseases
- Any disease that sends people to doctors or hospitals may have a genetic component

# Finding Genetic Factors Contributing to a Common Disease...

Eating lots of sugar and fat is good for increasing your risk of diabetes. Instead eat lots of fruits and vegetables.



# Finding Genetic Factors Contributing to a Common Disease...

Eating lots of sugar and fat is good! For increasing your risk of diabetes instead eat lots of fruits and vegetables.



# Genomic Discoveries for Rare Mendelian Disease



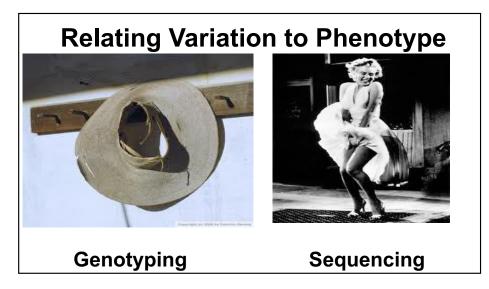


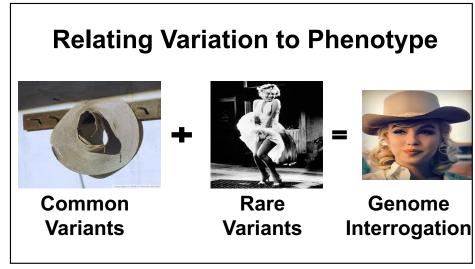
## Genomic Discoveries for Common Disease

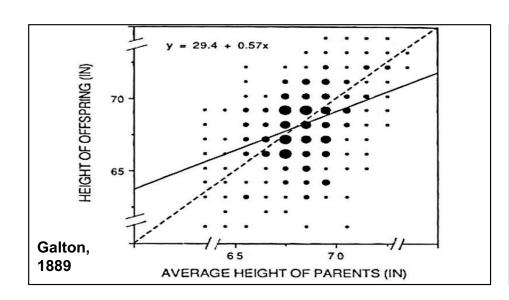


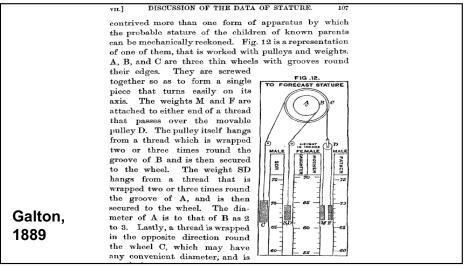












### **Estimating Heritability from SNPs**

### **REPORT**

GCTA: A Tool for Genome-wide Complex Trait Analysis

Jian Yang, 1,  $\star$  S. Hong Lee, 1 Michael E. Goddard, 2, 3 and Peter M. Visscher 1

### **ARTICLE**

Estimating Missing Heritability for Disease from Genome-wide Association Studies

Sang Hong Lee,¹ Naomi R. Wray,¹ Michael E. Goddard,²,³ and Peter M. Visscher¹,\*

### Table 2 Comparison of results of different polygenic methods across diseases

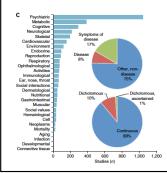
			Caused by common GWAS SNPs			
Pre			LMM-based _ heritability (s.e.)	Polygenic modeling and Bayesian inference		
	Prevalence (%)	Family based heritability <sup>a</sup>		Total variance explained (50% CI)	N SNPs (50% CI)	
Rheumatoid arthritis	1	0.53-0.68 (-0.13 MHC) <sup>b</sup>	0.32 (0.037)	0.18 (0.15–0.20) (+0.04 known non-MHC) <sup>b</sup>	2,231 (1,588–2,740)	
Celiac disease	1	0.5-0.87 (-0.35 MHC) <sup>b</sup>	0.33 (0.042)	0.44 (0.40-0.47)	2,550 (1,907–3,061)	
MI/CAD	6	0.3-0.63	0.41 (0.067)	0.48 (0.43-0.54)	1,766 (1,215–2,125)	
T2D mellitus	8	0.26-0.69	0.51 (0.065)	0.49 (0.46-0.53)	2,919 (2,335–3,442)	

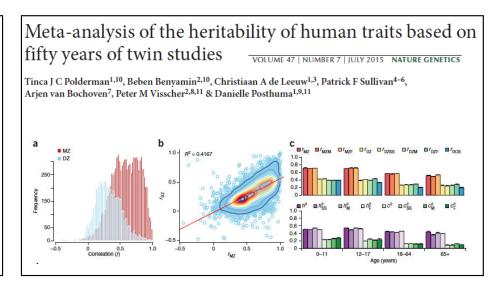
<sup>8</sup>Family based heritability estimates were taken from previous data for rheumatoid arthritis<sup>27,28</sup>, celiac diseasa<sup>18,30</sup>, MI/CAD<sup>31,32</sup> and T2D<sup>33,34</sup>. <sup>9</sup>We excluded some loci in certain analyses: although the family based heritability estimates are based on the whole genome, the extended MHC region was removed from the common GWAS SNP analyses for rheumatoid arthritis and celiac disease, and validated non-MHC loci were further removed from the polygenic modeling analysis of the rheumatoid arthritis GWAS data. 50% CI, 50% credible interval; s.e., standard error.

Stahl et al, Nat Gen

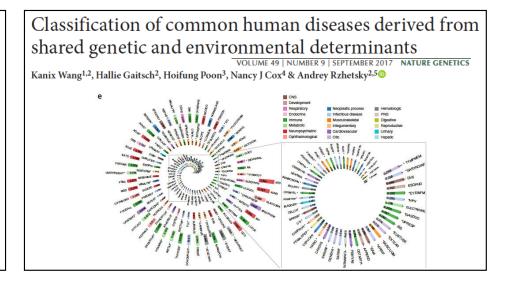
### Meta-analysis of the heritability of human traits based on fifty years of twin studies VOLUME 47 | NUMBER 7 | IULY 2015 NATURE GENETICS

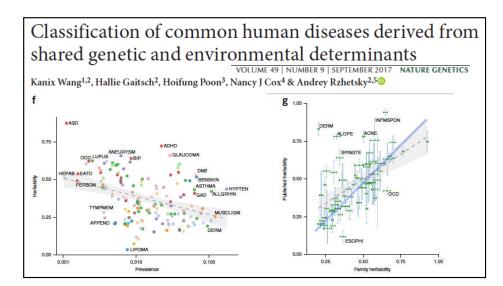
Tinca J C Polderman<sup>1,10</sup>, Beben Benyamin<sup>2,10</sup>, Christiaan A de Leeuw<sup>1,3</sup>, Patrick F Sullivan<sup>4-6</sup>, Arjen van Bochoven<sup>7</sup>, Peter M Visscher<sup>2,8,11</sup> & Danielle Posthuma<sup>1,9,11</sup>



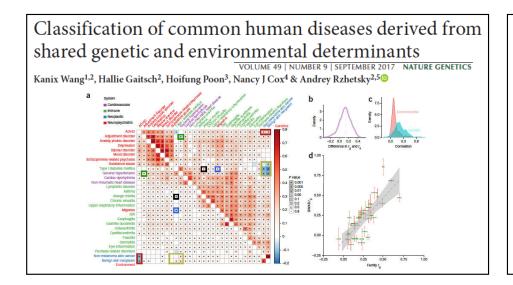


# Meta-analysis of the heritability of human traits based on fifty years of twin studies VOLUME 47 | NUMBER 7 | JULY 2015 NATURE GENETICS Tinca J C Polderman<sup>1,10</sup>, Beben Benyamin<sup>2,10</sup>, Christiaan A de Leeuw<sup>1,3</sup>, Patrick F Sullivan<sup>4-6</sup>, Arjen van Bochoven<sup>7</sup>, Peter M Visscher<sup>2,8,11</sup> & Danielle Posthuma<sup>1,9,11</sup>

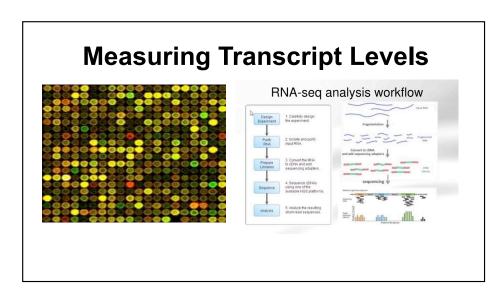


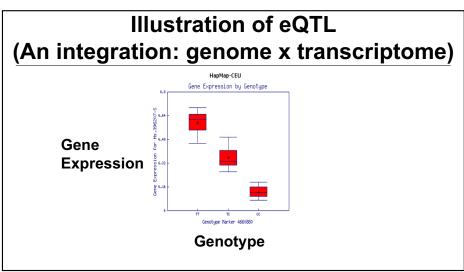


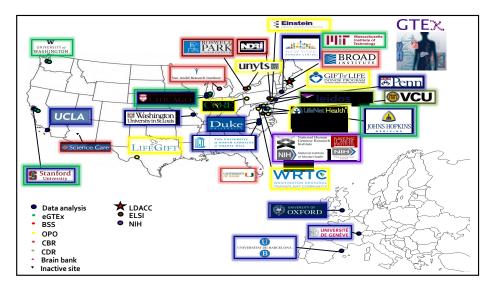


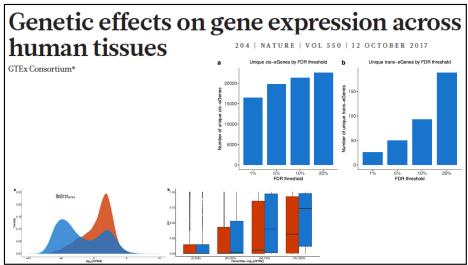


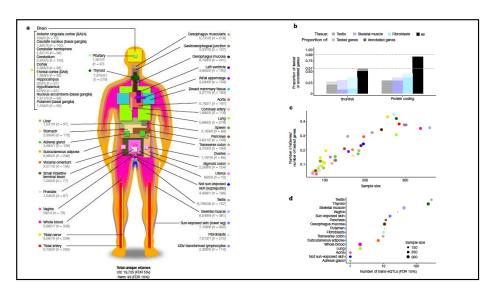
## Transcriptomics Review

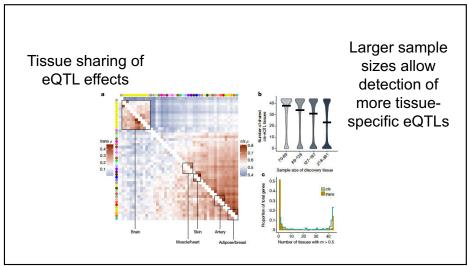


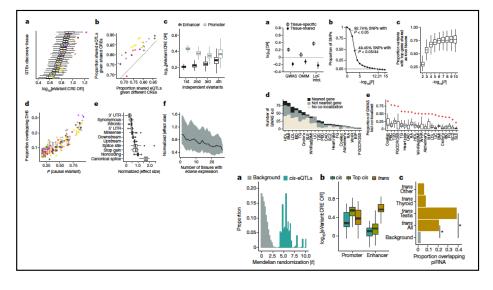


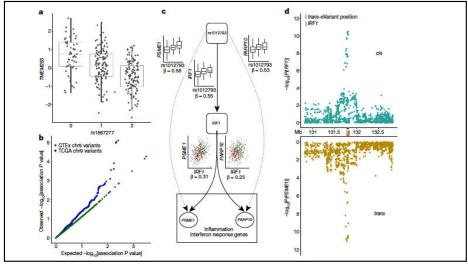






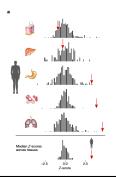






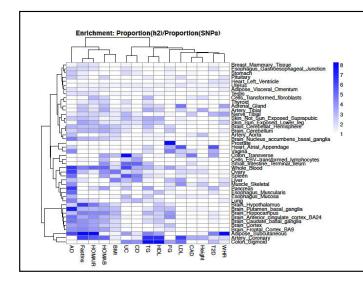
#### The impact of rare variation on gene expression across tissues 12 OCTOBER 2017 | VOL 550 | NATURE | 239

Xin Li<sup>1</sup>\*, Yungil Kim<sup>2</sup>\*, Emily K. Tsang<sup>1,3</sup>\*, Joe R. Davis<sup>1,4</sup>\*, Farhan N. Damani<sup>2</sup>, Colby Chiang<sup>5</sup>, Gaelen T. Hess<sup>4</sup>, Zachary Zappala<sup>1,4</sup>, Benjamin J. Strober<sup>6</sup>, Alexandra J. Scott<sup>5</sup>, Amy Li<sup>4</sup>, Andrea Ganna<sup>7,8,9</sup>, Michael C. Bassik<sup>4</sup>, Jason D. Merker<sup>1</sup>, GTEx Consortium†, Ira M. Hall<sup>5,10,11</sup>, Alexis Battle<sup>2</sup>§ & Stephen B. Montgomery<sup>1,4</sup>§

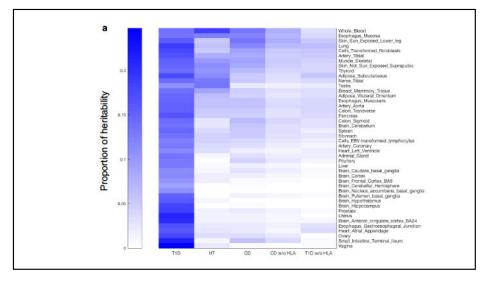


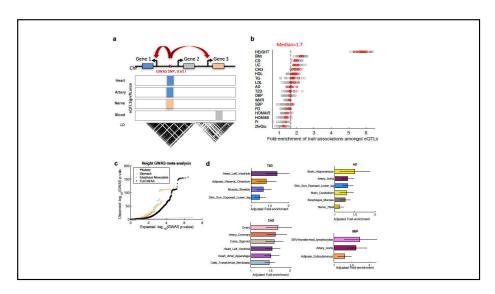
we observed that 58% of underexpression and 28% of overexpression outliers had rare variants near the relevant gene, compared to 8% for non-outliers (Fig. 3c).

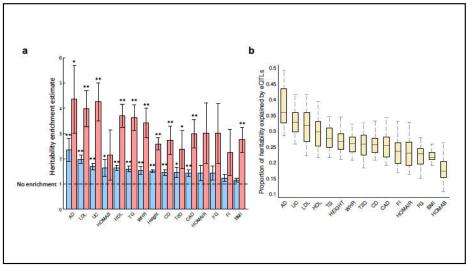
#### **GWAS** and **Transcriptomics**



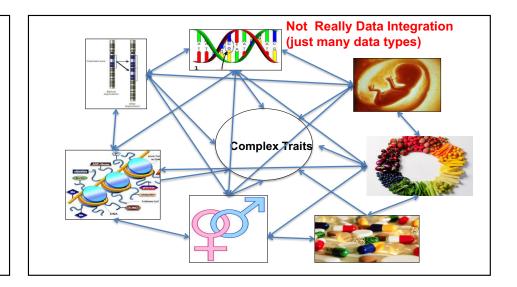
Fold enrichment (proportion of h<sup>2</sup> explained by eQTLs / proportion of total SNPs that were tissuespecific eQTLs)

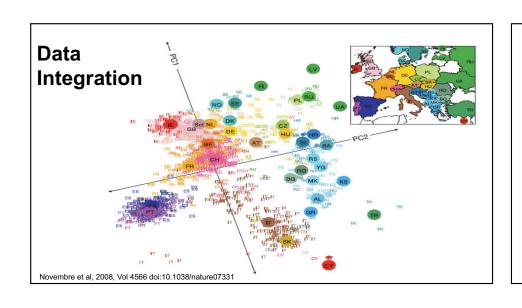






## What is Data Integration?

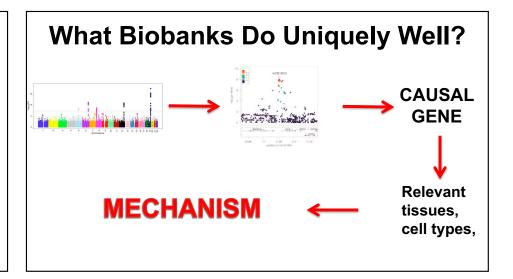


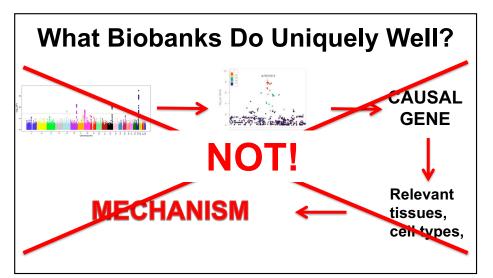


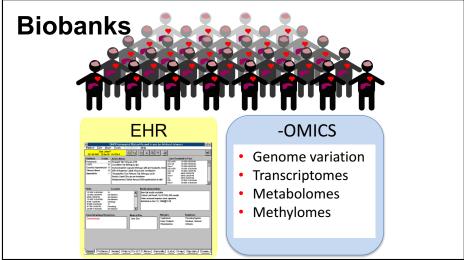
## Data Integration: Phenome X -OMICS

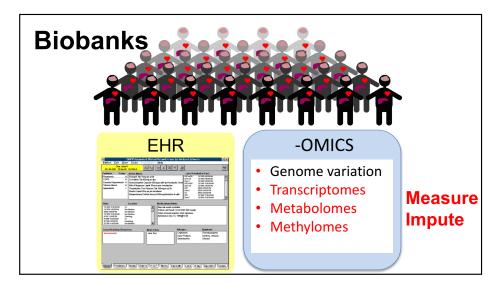
What can we do uniquely well in biobank data?

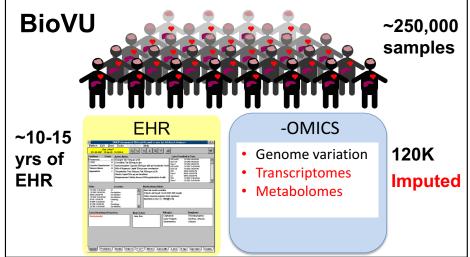
How can biobank strengths improve understanding of mechanisms of disease?

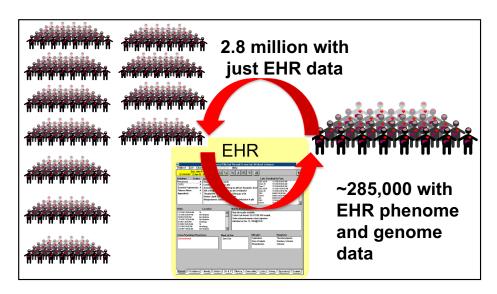


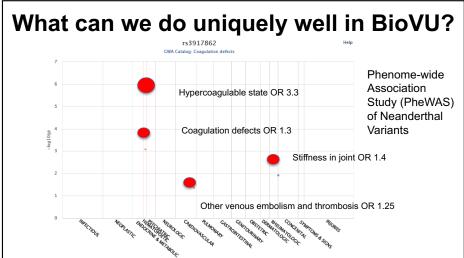






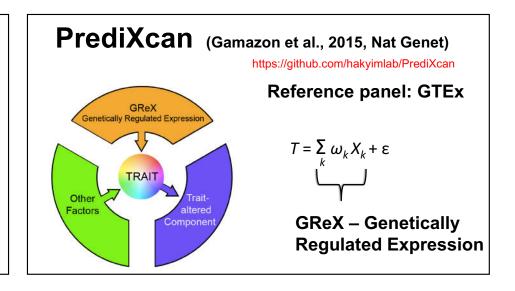


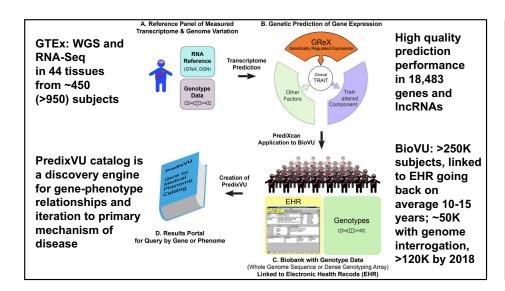




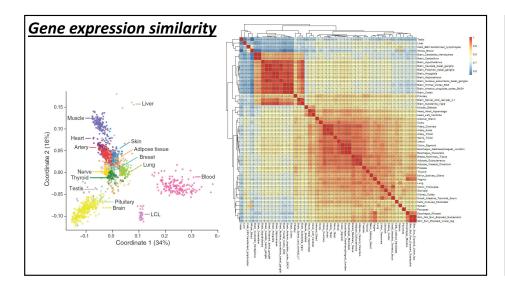
GWAS: What variants are associated with this phenotype?

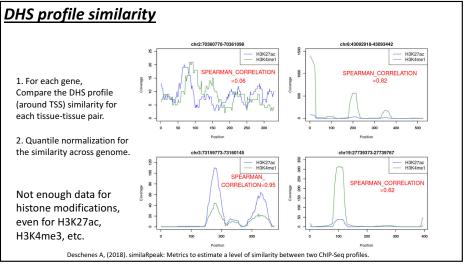
PheWAS: What phenome is associated with this variant?

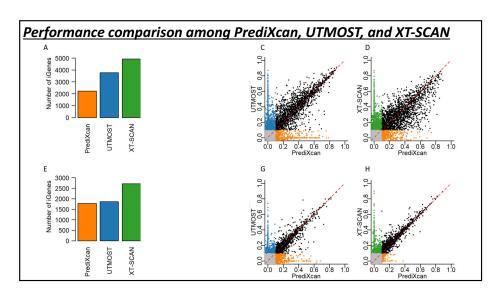




<u>Comparison</u>	PrediXcan	UTMOST	XT-SCAN
			Eric Gamazon
Cross-tissue	No	Yes	Yes
Prediction	Elastic Net	Sparse	Weighted
Model	Liastic ivet	Group LASSO	Elastic Net
Incorporate regulatory elements	No	No	Yes (DHS)
Incorporate expression similarity	No	No	Yes
			Dan Zhou



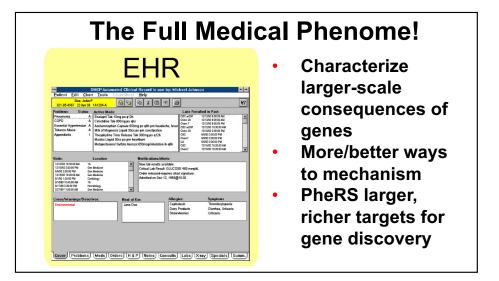


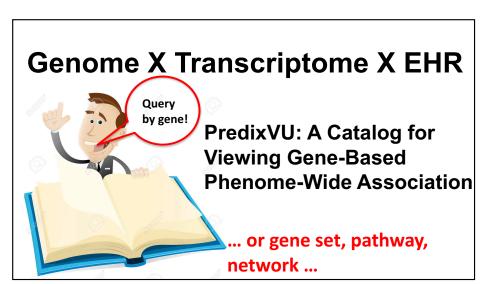




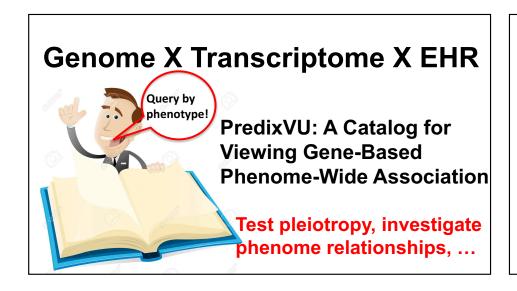
Gene-based PheWAS
What does this gene do?

What does the natural variation in the expression of this gene associate with across the medical phenome?





#### *ZNF577* P-value Cases Trait OR per unit SD Controls Viral hepatitis C 0.37 6.21E-07 0.84 808 20904 Viral hepatitis 0.37 0.86 4.38E-06 20904 267 Malignant neoplasm of liver, primary 0.37 0.81 1.61E-04 22080 Cancer of liver and intrahepatic bile duct 0.37 0.82 2.43E-04 318 22080 Precordial pain 0.37 1.22 4.34E-04 12283



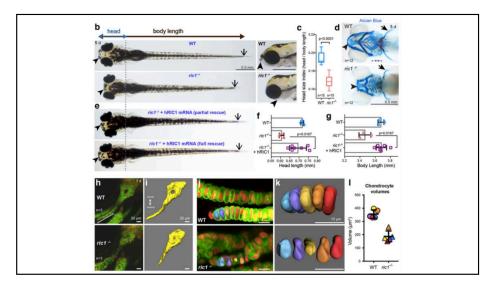
	virai Hepatitis C						
Gene	R <sup>2</sup>	OR per unit SD	P-value	Cases	Controls		
<u>ZNF577</u>	0.37	8.44E-01	6.21E-07	808	20904		
<u>ZNF649</u>	0.12	8.48E-01	1.85E-06	808	20904		
SPAG1	0.22	8.63E-01	2.98E-05	808	20904		
KLRC1	0.42	8.57E-01	4.31E-05	808	20904		
CST2	0.14	8.64E-01	4.42E-05	808	20904		

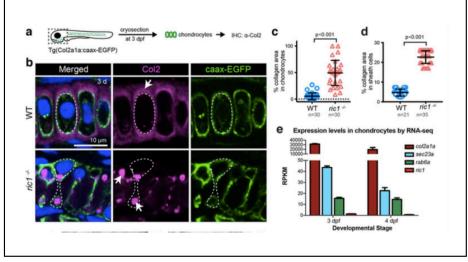
Wirel Henetitie C

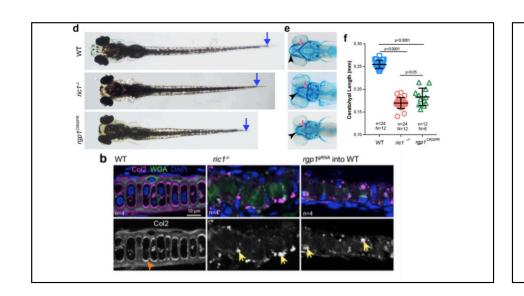
#### **Intestinal Infection**

Gene	R <sup>2</sup>	OR per unit SD	P-value	Cases	Controls
NDUFA4	0.03	1.16	1.83E-09	1608	24187
C10orf120	0.006	1.13	4.92E-08	1608	24187
TJP1	0.066	1.12	5.27E-06	1608	24187
YEATS2	0.012	0.89	6.33E-06	1608	24187
DGAT2	0.12	1.12	1.11E-05	1608	24187
GNA12	0.23	1.12	1.32E-05	1608	24187
ZNF525	0.13	0.89	1.96E-05	1608	24187
ALLC	0.15	0.89	2.08E-05	1608	24187
HDGFRP2	0.005	0.90	3.45E-05	1608	24187









#### BioVU Phenome for RIC1/RGP1

- Bone, fracture, and connective tissue disorders !
- Tooth development and eruption



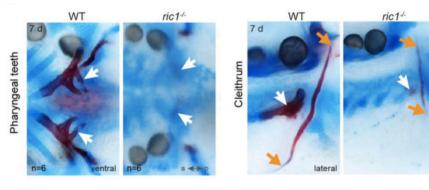
- Gait disorders
- Asthma, heart valve defects and replacement
- Esophageal, gut and digestive disorders



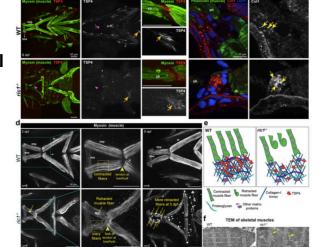
- Strabismus, amblyopia
- Neurological and neuropsychiatric disorders

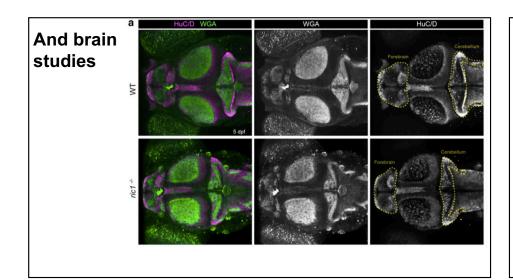


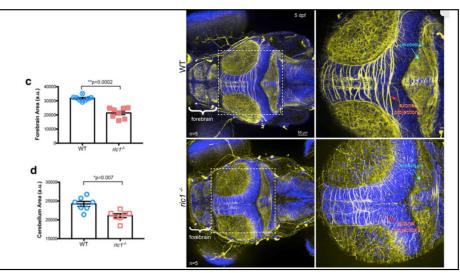
#### Results of BioVU studies prompted zebrafish studies of tooth development...

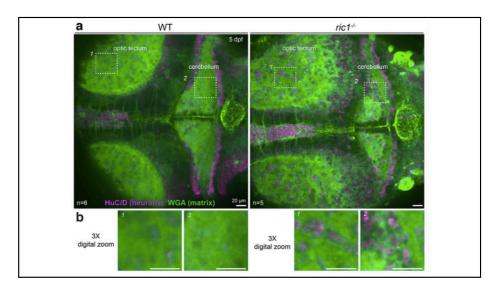


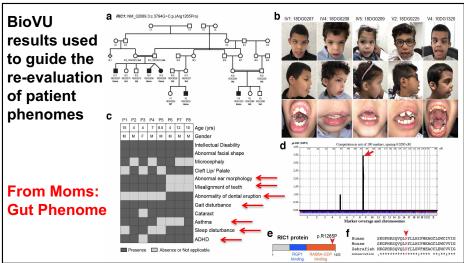
Muscle attachment studies in small (eye) and large muscles...

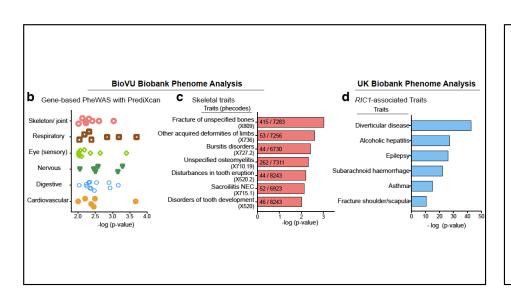


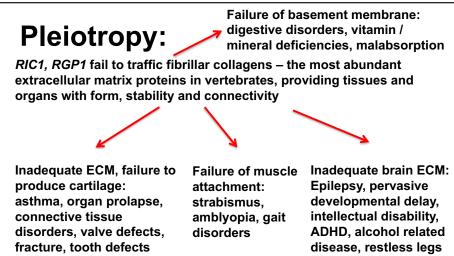


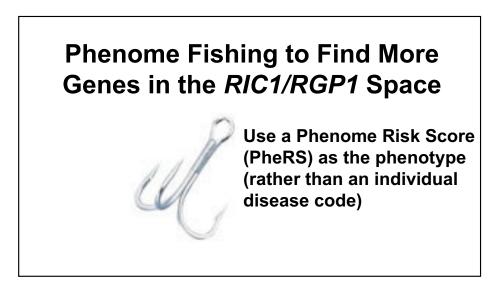


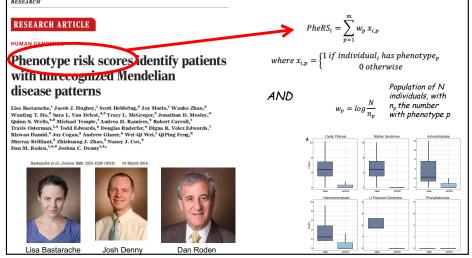












### Genes with Significant Association to *RIC1/RGP1* PheRS

COL14A1, COL3A1, COL5A2, COL9A3

Exchanges bound GDP for free GTP – a (Duh!)
key part of the *RIC1/RGP1* machine

for collagen transport

FAM124A, FGD6, EPC2, EPPK1, ADAMTSL4, ATP5H, EDEM2, CPT1A

ER-associated degradation of misfolded glycoproteins

Attaches to fibrillin and fibrillar collagens to stabilize extracellular matrix

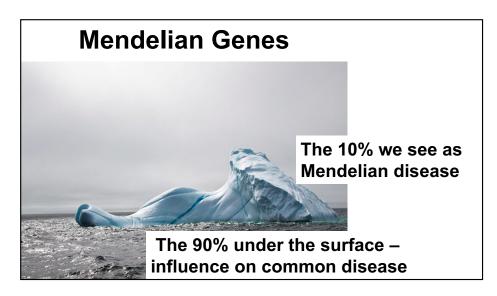
## Creating a Poly-gene Score for ECM Strength

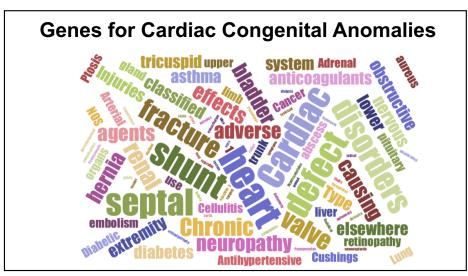
- Directions of effects consistent across the genes functioning to strengthen ECM
- Sum predicted expression across gene set to probe phenome associations to ECM strength

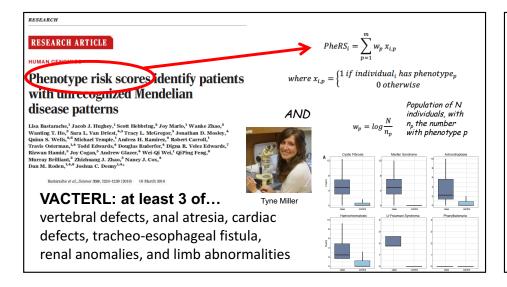
Pleiotropy is ubiquitous.

**Continuum from Mendelian to Complex** 

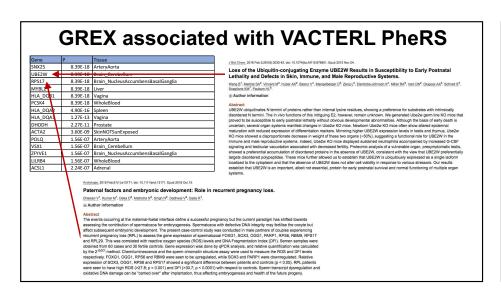
Continuum from LOF to eleterious to Lexpression

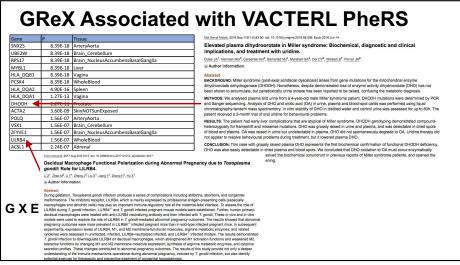


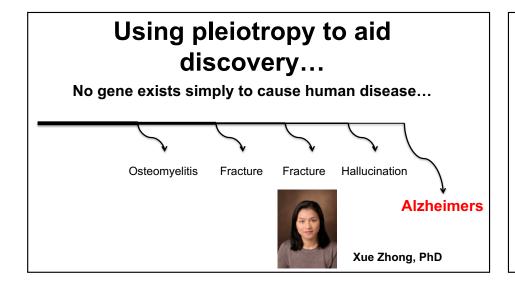




#### **GReX Associated with VACTERL PheRS** Gene SNX25 8.39E-18 ArteryAorta UBE2W 8.39E-18 Brain Cerebellum 8.39E-18 Brain\_NucleusAccumbensBasalGanglia MYRI 1 8 39F-18 Liver 8.39E-18 WholeBlood HLA\_DQA2 4.90E-16 Spleen HLA\_DQA1 1.27E-13 Vagina DHODH 2 27F-11 Prostate 3.60E-09 SkinNOTSunExposed POLQ 1.56E-07 ArteryAorta VSX1 1.56E-07 Brain\_Cerebellum 1.56E-07 Brain NucleusAccumbensBasalGanglia 1.56E-07 WholeBlood







#### Trait OR per unit SD p-value Cases Controls Unspecified osteomyelitis 8.38E-01 4.03E-05 524 19865 Fracture of upper limb 8.95E-01 6.03E-05 1355 21096 7.06E-05 231 19865 Acute osteomyelitis 7.79E-01 8.41E-01 7.18E-05 21096 Fracture of humerus 948 Fractures: patella, Bacterial enteritis 1.15E+00 7.67E-05 radius, ulna, Intestinal infection due to C. difficile 1.15E+00 1.10E-04 vertebral column Heart failure with reduced EF 9.15E-01 1.10E-04 2262 Brain: intracranial 735 hemorrhage, 8.70E-01 1.41E-04 Osteomyelitis subdural hemorrhage, Osteomyelitis, periostitis, and other 8.80E-01 2.14E-04 Congenital anomalies of limbs 6.75E-01 2.34E-04 76 cerebral aneurism. Alzheimers

Phenome Associations to GReX of PSEN1

#### TREM2 GReX Associations

#### Nasu-Hakola Disease

Alzheimers and other dementias

Trait	OR per unit SD	p-value	Cases	Controls
Chronic osteomyelitis	8.18E-01	1.40E-05	344	19865
Acute osteomyelitis	7.93E-01	1.97E-05	231	19865
Cerebral laceration and contusion	7.34E-01	5.55E-05		
Unspecified osteomyelitis	8.59E-01	1.17E-04	Brain: Delerium, psychogenic disorde	
Osteomyelitis	8.79E-01	1.51E-04		
Diverticulitis	8.47E-01	4.98E-04		
Hallucinations	7.44E-01	7.18E-04		tions
			degenera	tions

## Osteoclasts and microglia share a developmental lineage...

- Substantial overlap in genes expressed, and the genetic architecture of their gene regulation
- Additional of the genes implicated in Alzheimers show similar patterns of phenome association

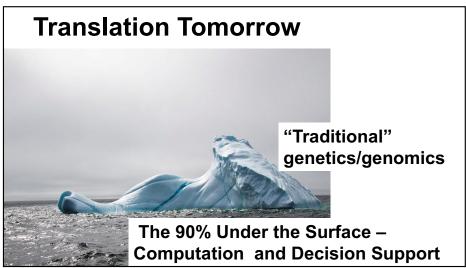
#### In 2.8M Subjects with EHR...

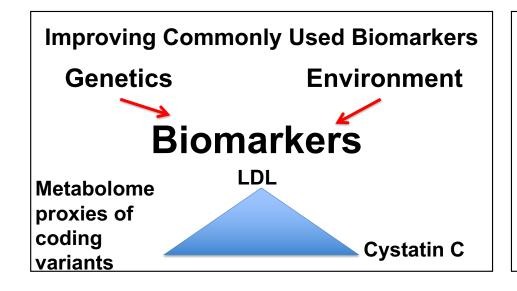
- Age at diagnosis for osteomyelitis is 15-20 years earlier than diagnosis of dementia
- Subjects with osteomyelitis diagnosed before 60 have 4-6 X increased risk of dementia diagnosis after age 70

#### In Silico Drug Trials

- Already conducting in silico drug trials: Do patients taking a drug for one indication have altered risk or age at onset for another disease (e.g. AD)? YES
- Pleiotropic phenome discovered through genetics creates a larger target for discovery and validation for in silico and later clinical trials







**New –Omics Biomarkers** 

Discovery of New Biomarker Relationships

#### Ranges and Thresholds

- Some biomarker measurements are adjusted for sex, age, race/ethnicity
- It is not about race/ethnicity! It is about DNA variation with frequency differences by historical geographic ancestry

#### **Predictive Modeling**

- Done extensively in learning healthcare systems now
- Where can we add genetics to the modeling and get improvement?
- For the most expensive conditions, even marginal improvements in prediction yield better care, lower costs

#### The IOTA Concept:

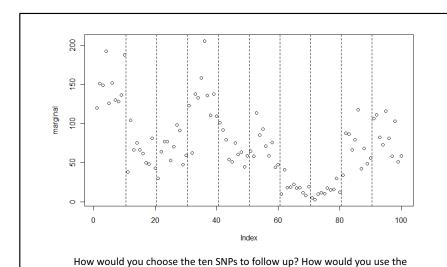
When we already have the genome information, even an iota of improvement over current practice (or existing predictive models) will have value for the most expensive and common conditions

## Statistical fine-mapping of GWAS signals

#### **Bogdan Pasaniuc**

Associate Professor Computational Medicine UCLA @bpasaniuc pasaniuc@ucla.edu

Advanced gene mapping course, January 2020

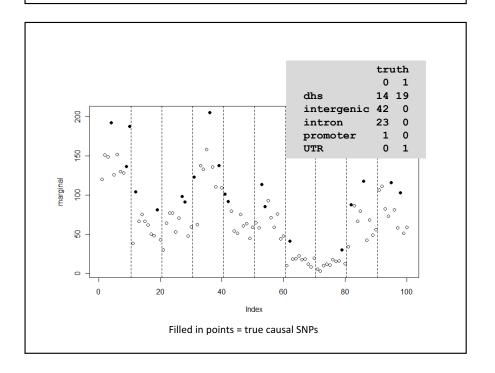


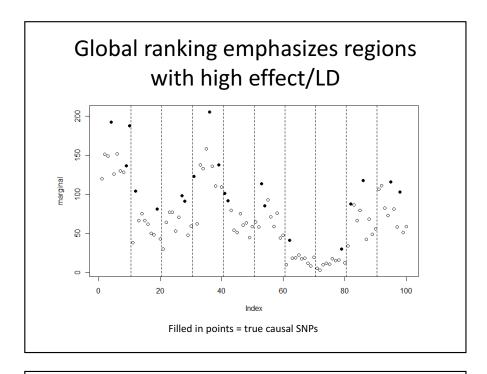
genetic association data? What other information could you use? How would

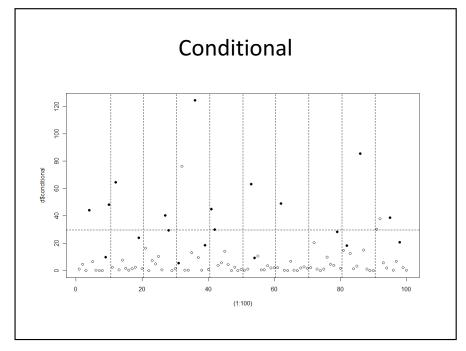
you combine the association results with this additional information?

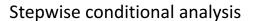
#### Motivating example:

- You've conducted a GWAS using in ~100,000 individuals.
- 10 regions are GWAS significant.
- You have resources to conduct follow-up studies of 10 SNPs.
- How do you chose the SNPs for functional follow-up?





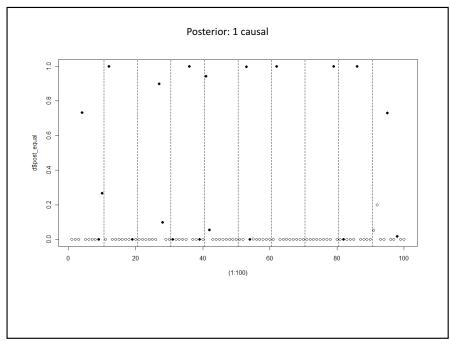


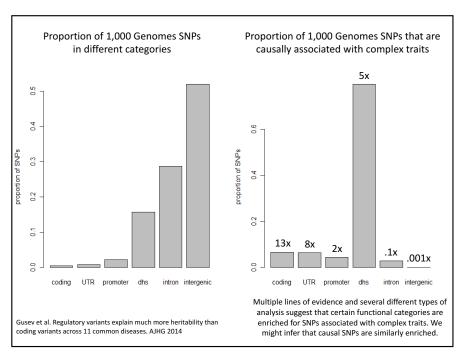


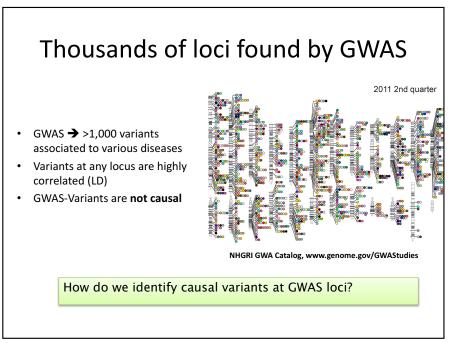
Does this analysis match the goal?

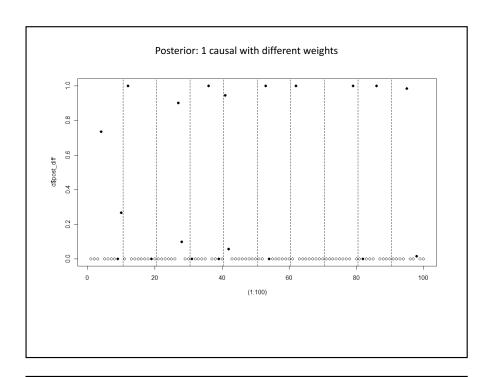
Maybe not: the more "LD friends" a causal variant has, the more likely the stepwise approach will pick one of its "friends"

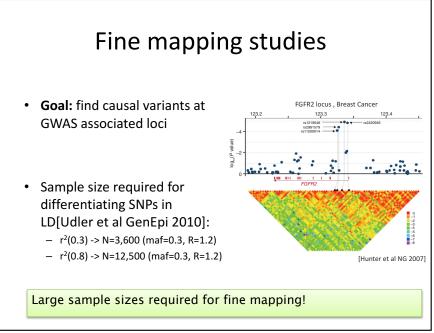
This is particularly concerning when power is modest (unlike in our well-powered example)



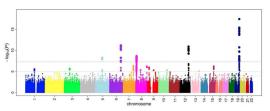








#### An optimization approach to fine-mapping



- Many GWAS associated loci
  - Height (>180), BC(~30), PC(~30)...
- 2-step approach:
  - 1. Select set of SNPs for functional validation from considered loci
  - 2. Test set of variants in functional assays
- Goal: find as many causals within fixed budget

Statistical model → causal SNP probabilities (statistical fine-mapping, see Schaid et al NRG 2018)

#### Methods for fine-mapping

- GOAL: prioritize variants for functional assays
- Prioritization approaches:
  - Marginal association statistics
    - Ignores LD → suboptimal performance
  - Conditioning approaches
    - No clear strategy for selecting variants to condition on
    - Stopping condition?
    - Does not correctly model LD for prioritizing causal variants
  - Probabilistic approach
    - Estimates probability of each variant to be causal
    - Can integrate ENCODE genomic features as priors

#### Pervasive Linkage Disequilibrium (LD) in the human genome

- Neighboring SNPs are inherited together on haplotypes
- Block-like correlation structure across the human genome



Barret et al. Bioinformatics 2005

#### Only need to measure a subset of the markers for effective GWAS!

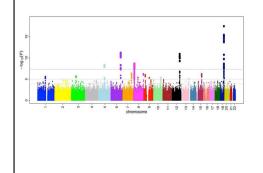
- Neighboring SNPs are inherited together on haplotypes
- Block-like correlation structure across the human genome
- Fill in the rest through imputation

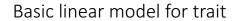


Marchini et al. Nat Rev Genet 2010

## 

#### Groups of neighboring variants will display significant associations due to LD





#### GWAS marginal effect is biased due to LD

GWAS effect size at SNP i:

$$\widehat{\boldsymbol{\beta}_{GWAS,i}} = \frac{1}{n} X_i y = \frac{1}{n} X_i ([X_1 \cdots X_p] \beta + \epsilon)$$

$$= \left[ \frac{1}{n} X_i X_1 \cdots \frac{1}{n} X_i X_p \right] \beta + \frac{1}{n} X_i \epsilon$$

$$= \boldsymbol{\Sigma}_{j=1}^{\mathbf{p}} \mathbf{r}_{ij} \boldsymbol{\beta}_j + \frac{1}{n} X_i \epsilon$$

Or in matrix notation:

$$\widehat{\boldsymbol{\beta}_{GWAS}} = MVN(\underline{V\boldsymbol{\beta}}, \frac{V(1-h_g^2)}{n})$$

Am. J. Haw. Genet. 69:1-14, 2001

#### REVIEW ARTICLE

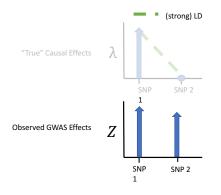
Linkage Disequilibrium in Humans: Models and Data

Jonathan K. Pritchard' and Molly Przeworski'

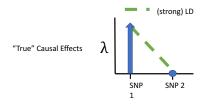
this review, we describe recont empirical and theoretical work on the extent of linkage florequiblemen (LDI) as beam an genume, comparing the predictions of majer populations general models to resultable Ala, Seward and beam and the production of the production of

Pritchard&Przeworski AJHG 2001, Shi et al, AJHG 2016,

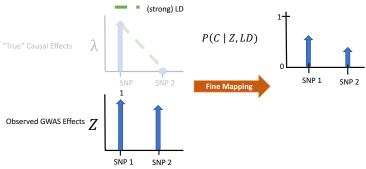
#### LD induces correlations between causal and non-causal SNPs



#### LD induces correlations between causal and non-causal SNPs



Given the correlation structure and association strength, quantify the probability that SNPs explain the signal



CAVIAR, CAVIARBF, FINEMAP, PAINTOR, Susie, etc... (nicely reviewed in Schaid et al NRG 2018)

Approximate estimation of posterior probabilities (1-causal assumption)

- Assumptions
  - one causal SNP per locus
  - causal variant is typed

$$P(c \mid \overline{s}) = \frac{P(\overline{s} \mid c)P(c)}{P(c)}$$

- Marginal association statistics are sufficient to estimate posterior [Maller et al Nat Gen 2012]
  - Can be extended to frequentist approach
  - Statistics at nearby SNPs are independent of phenotype conditional on causal variant
- "Robust to misspecifications"
- Can estimate confidence sets

Allowing for multiple causals improves accuracy 2 Causal 3 Causal ω ω Ö Ö. несан нате 0.4 0.6 несан нате 0.4 0.6 **CAVIAR** 0.2 Top K 1-Post 0.0 10 10 Number of selected SNPs Number of selected SNPs [Hormozdiari et al. Genetics 2014 Allowing for multiple causals improves accuracy

Causal status vector →

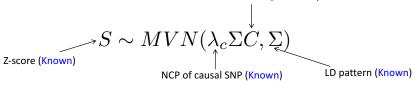
$$C = \{c_1, c_2, \cdots c_m\}$$

• Use Bayes to compute probability of each vector

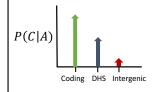
$$P(C|S) = \frac{P(S|C)P(C)}{P(S)}$$

Model for association statistics

Causal status (Unknown)



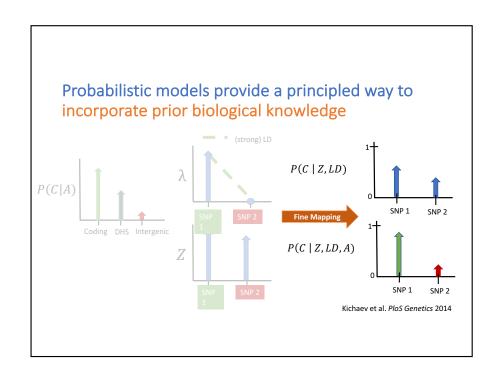
Probabilistic models provide a principled way to incorporate prior biological knowledge

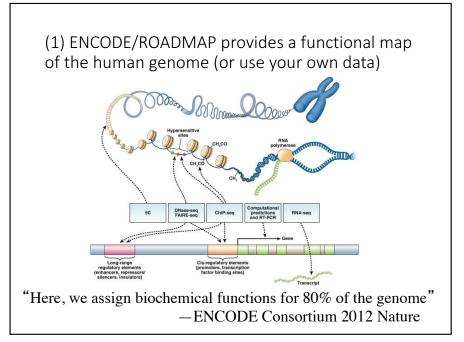


# Probabilistic models provide a principled way to incorporate prior biological knowledge P(C|A) A SNP1 SNP2 SNP2

- (1) Where to get external functional information?
  (e.g., classes of SNPs more likely to have function)
- (2) How to quantify which classes of SNPs more useful for our trait of interest?

  (e.g., regulatory in tissue X vs tissue Y)



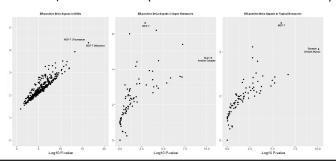


#### (2) Functional enrichment

- · Question:
  - Is GWAS signal concentrated in particular "functional" areas of the genome?
- Functional enrichment = GWAS Signal / proportion of genome covered by functional annotation

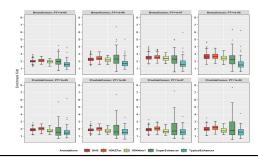
#### (2) Functional enrichment quantification Option 1: count of biofeatures with GWAS signal

- Question:
  - Is GWAS signal concentrated in particular "functional" areas of the genome?
- Functional enrichment = GWAS Signal / proportion of genome covered by functional annotation
- Example from Breast/Prostate Cancer (Chen..Linstroem Hum Genet 2019)

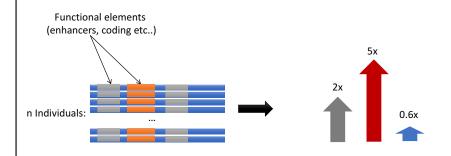


#### (2) Functional enrichment quantification Option 1: count of biofeatures with GWAS signal

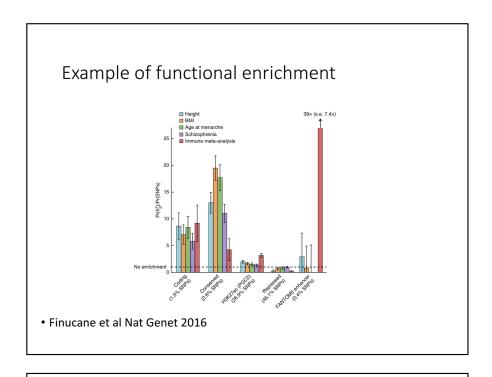
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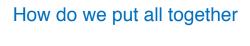


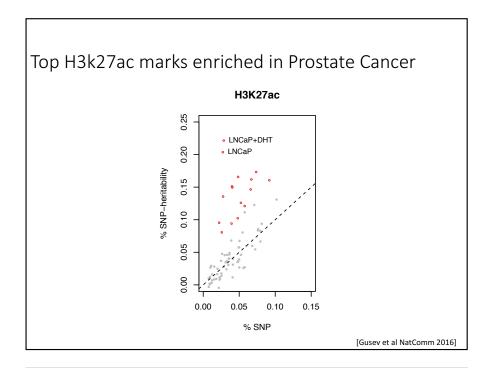
#### (2) Functional enrichment quantification Option 2: SNP-heritability enrichment

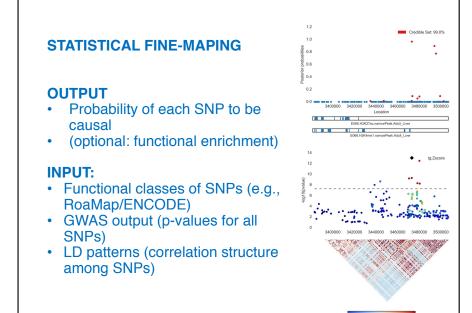


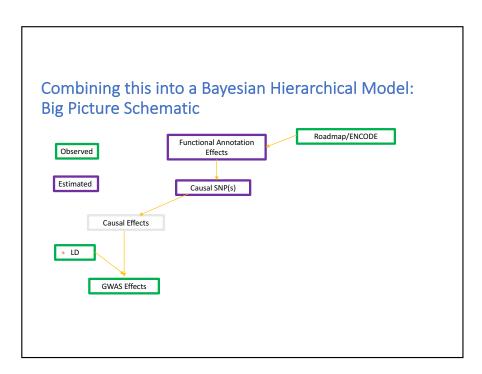
Can be estimated directly from summary GWAS (e.g., Finucane et al Nat Gen 2014)

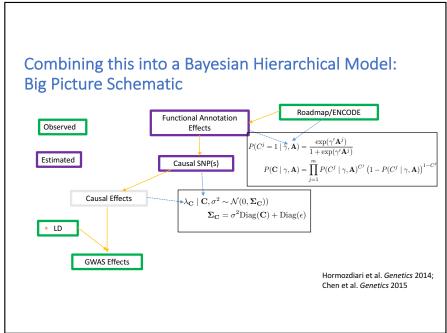


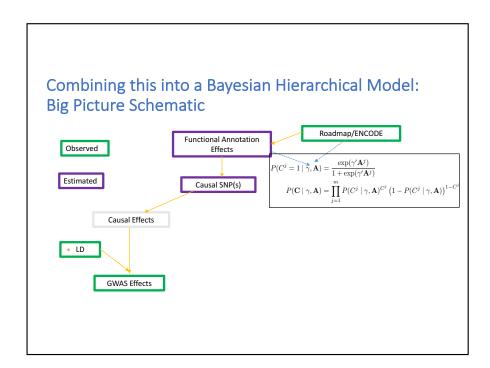


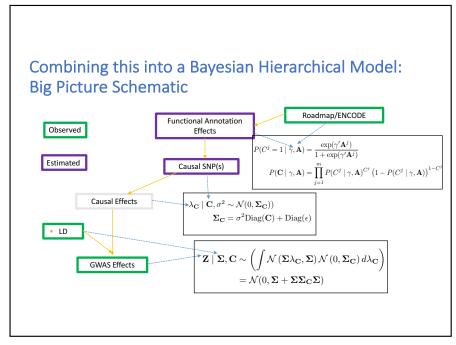


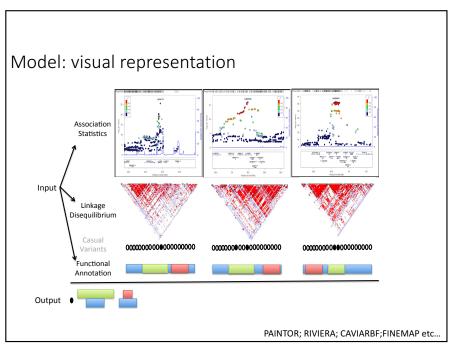


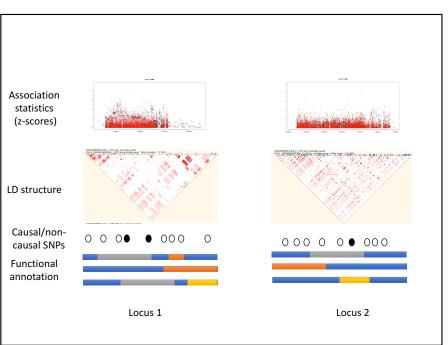


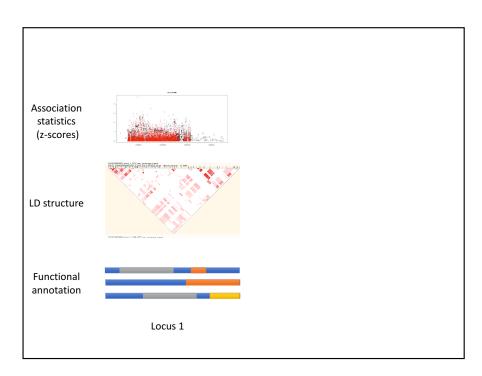


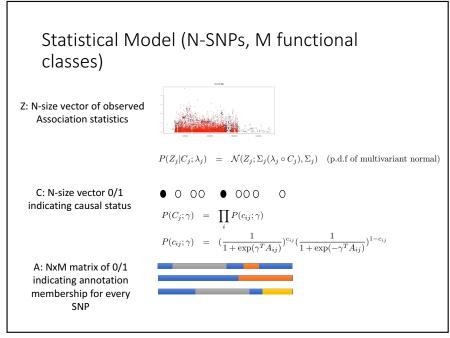












#### Statistical Model (N-SNPs, M functional classes) Z: N-size vector of observed Association statistics $\lambda_i$ : effect size of SNP j $P(Z_j|C_j;\lambda_j) = \mathcal{N}(Z_j;\Sigma_j(\lambda_j\circ C_j),\Sigma_j)$ (p.d.f of multivariant normal) Σ<sub>i</sub>: LD at locus i C: N-size vector 0/1 indicating causal status $P(C_j; \gamma) = \prod P(c_{ij}; \gamma)$ A: NxM matrix of 0/1 probability of SNP to be indicating annotation causal membership for every SNP

#### Practical considerations

#### Getting output from statistical model: Bayes

$$P(\mathbf{C} \mid \mathbf{Z}, \mathbf{\Sigma}, \mathbf{A}, \gamma) = \frac{\mathcal{N}(0, \mathbf{\Sigma} + \mathbf{\Sigma} \mathbf{\Sigma}_{\mathbf{C}} \mathbf{\Sigma}) P(\mathbf{C} \mid \mathbf{A}, \gamma)}{\sum_{C \in \mathcal{C}} \mathcal{N}(0, \mathbf{\Sigma} + \mathbf{\Sigma} \mathbf{\Sigma}_{\mathbf{C}} \mathbf{\Sigma}) P(\mathbf{C} \mid \mathbf{A}, \gamma)}$$

- Causal vector formulation gives the flexibility to model multiple causal variants at any risk locus
- Iterative procedure to estimate annotation effects across all fine mapping loci using Maximum Likelihood and EM.

Fine-mapping credible sets are miscalibrated when assuming a single causal variant.

Causal Assump.	Method	Functional Annotations	Causals Identified	90% Credible Set Size
Single	Maller et al.	None	64.2%	265.0
Multiple	CAVIAR	None	91.9%	510.3

90% credible set = set of SNPs that consume 90% of the total posterior probability mass

Maller et al. Nat Gen 2012; Hormozdiari et al. Genetics 2014:

#### Leveraging functional enrichment improves finemapping resolution

Causal Assump.	Method	Functional Annotations	Causals Identified	90% Credible Set Size	
Single	Maller et al.	None	64.2%	265.0	
Multiple	CAVIAR	None	91.9%	510.3	up to ~30%
Multiple	PAINTOR	Included	91.2%	393.7	improvem

90% credible set = set of SNPs that consume 90% of the total posterior probability mass

Maller et al. *Nat Gen* 2012; Hormozdiari et al. *Genetics* 2014; Kichaev et al. *Plos Genetics* 2014

What if we have multiple ancestries? Can we still perform statistical fine-mapping?

#### Statistical fine-mapping identifies bona-fide causal variants

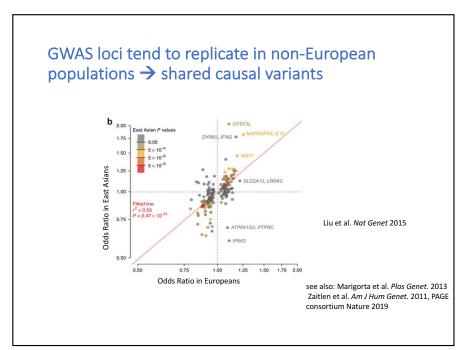
LETTERS

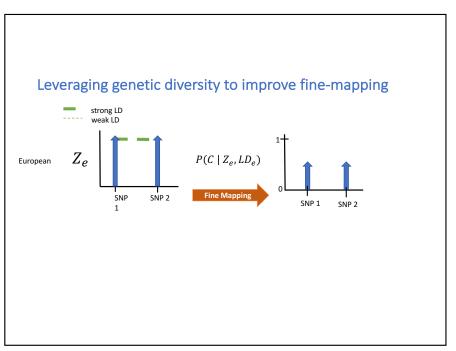
A thrifty variant in *CREBRF* strongly influences body mass index in Samoans

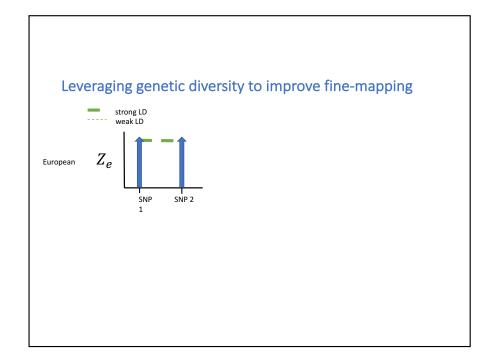
Ryan L Minster<sup>1,13</sup>, Nicola L Hawley<sup>2,13</sup>, Chi-Ting Sul-<sup>12,13</sup>, Guangyun Sun<sup>3,13</sup>, Erin E Kershaw<sup>4</sup>, Hong Cheng<sup>3</sup> Olive D Buhule<sup>2,12</sup>, Jerome Lin<sup>1</sup>, Muagututi'u Sefuiva Reupena<sup>6</sup>, Satupa'itea Viali<sup>7</sup>, John Tuitele<sup>8</sup>, Take Naseri<sup>9</sup>, Zsolt Urban-<sup>11</sup>, Banian Deka-<sup>11</sup>, Daniel E West<sup>1,2,14</sup> & Steben T McGarvey<sup>9</sup><sup>11,14</sup>

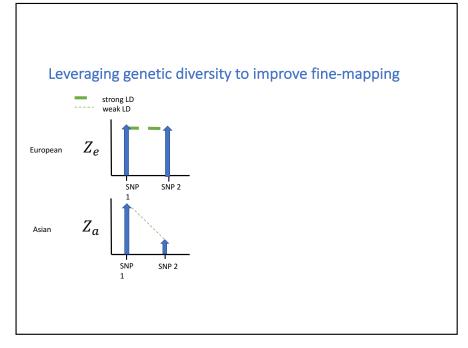
"Bayesian fine-mapping with PAINTOR strongly supported following up the missense variant. The two variants in the region with the highest posterior probability (PP) of being causal were rs373863828 (PP = 0.80) and rs150207780 (PP = 0.22); when Encyclopedia of DNA Elements (ENCODE) functional annotation was included, these probabilities increased to 0.92 and 0.34, respectively"

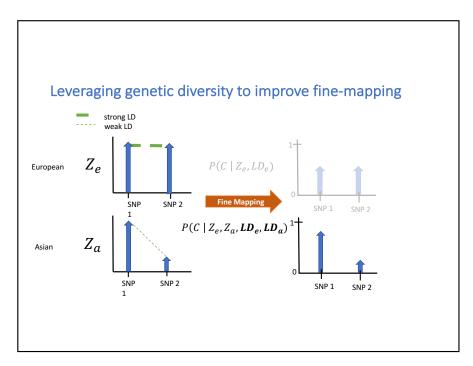
## Divergent population histories give rise to unique genetic backgrounds LD Patterns Allele Frequencies Cursulan Voruba

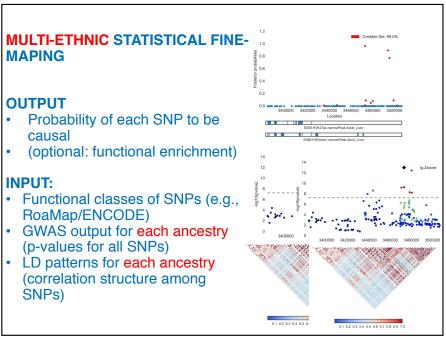


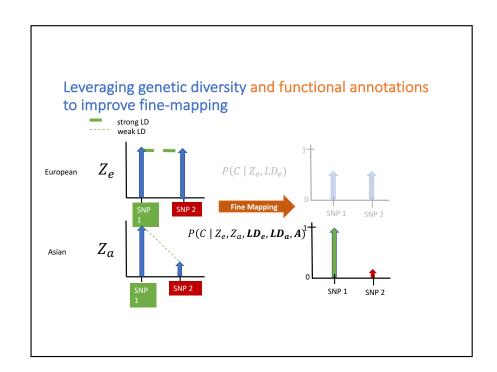


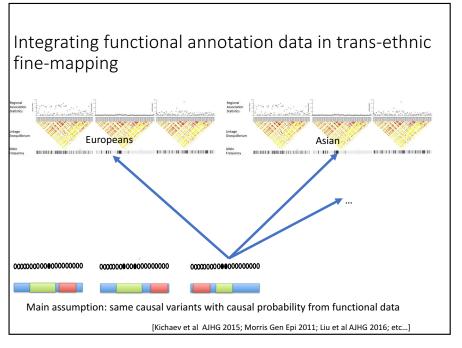


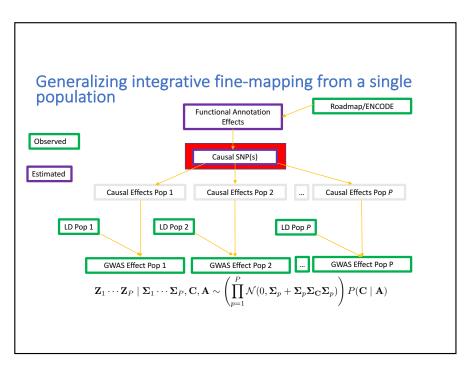


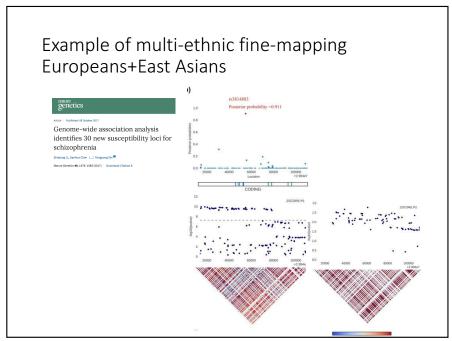


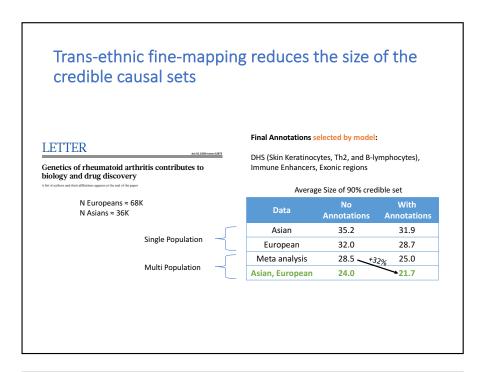


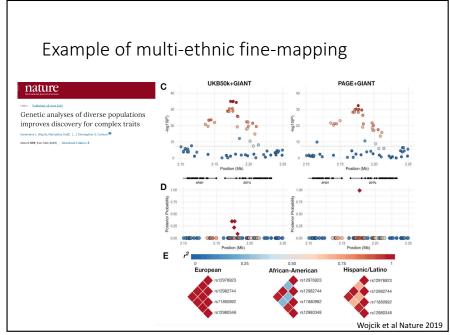


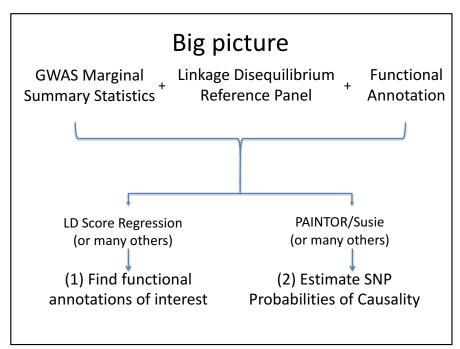


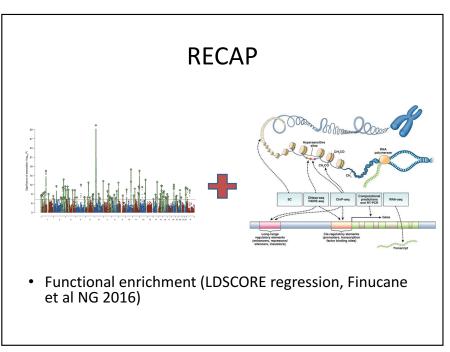


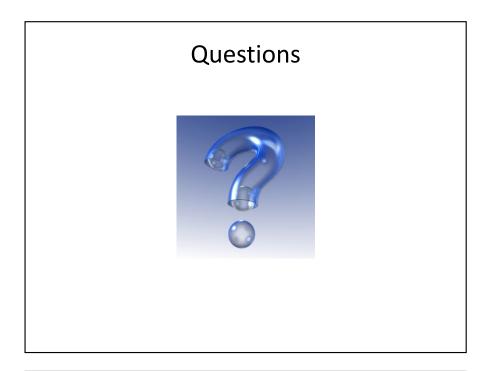


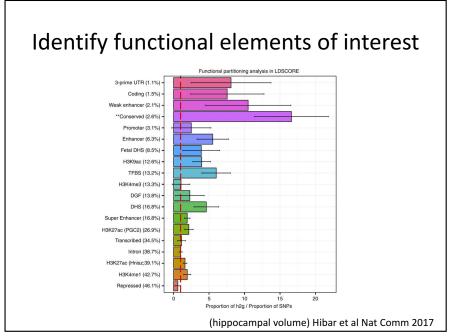




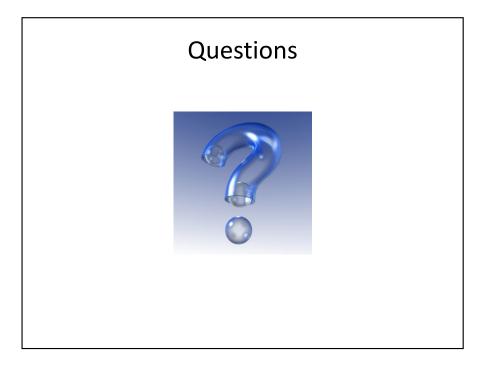




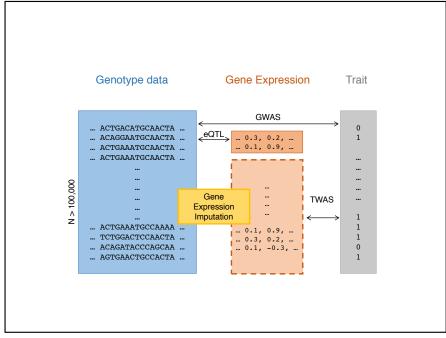


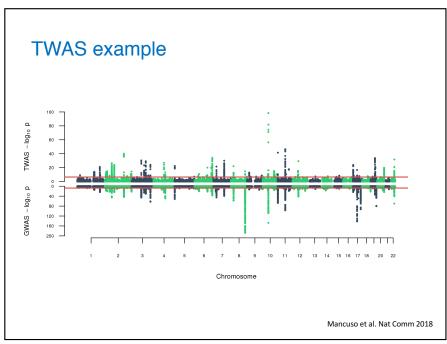


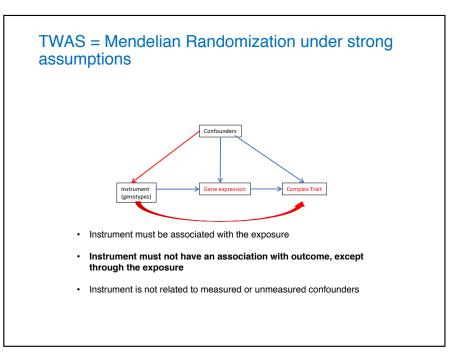
# Prioritize genetic variants likely to be biologically causal E Multi-region fine-mapping with annotation Ex Locus 1 | Execuse annotation enrichment | Borrow information across loci

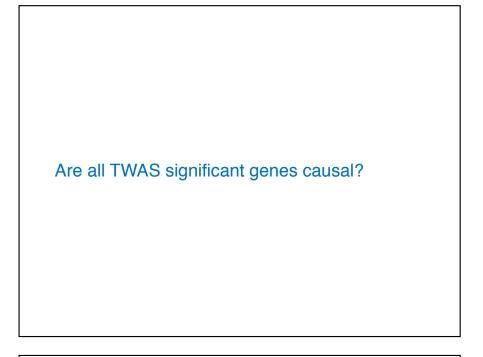


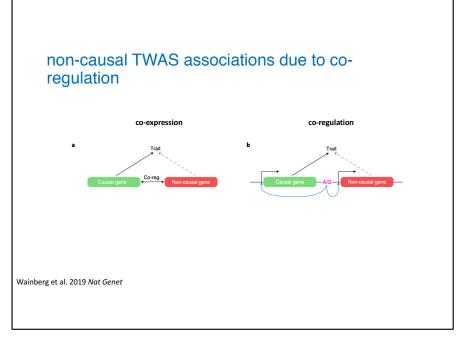
Statistical fine-mapping at gene-level in TWAS/PrediXscan/etc...

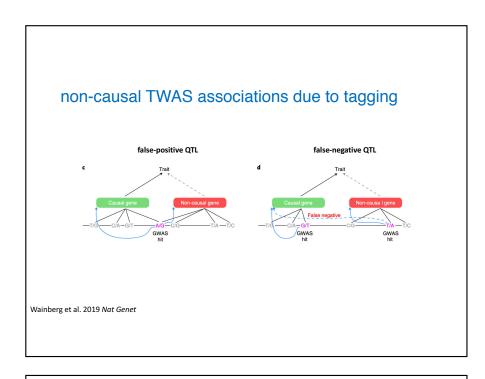












### But we really want causal genes...

### TWAS interpretation

- Two sample Mendelian Randomization test
  - Estimate mediating effect of gene expression under very strong assumptions!
  - Zhu et al. Nat Gen 2016; Barfield et al Gen Epi 2018, ...
- Test of association (genetic covariance) expression and trait
  - **Similarity** between trait / GE at local genetics
  - Gusev et al. Nat Gen 2016; Mancuso et al. AJHG 2017, Wainberg et al Nat Gen 2019; Mancuso et al Nat Genet 2019

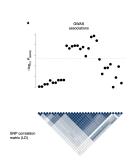


### Opportunities and challenges for transcriptomewide association studies

Michael Wainberg', Nasa Sinnott-Armstrong®², Nicholas Mancuso®², Alvaro N. Barbeira®⁴, David A. Knowles®⁴⁵, David Golan', Raili Ermel', Arno Ruusslepp³³, Thomas Quertermous®², KeHao®³, Johan L. M. Björkegren®³³, Hae Kyung Im®⁴\*, Bogdan Pasaniuc®³³³, Manuel A. Rivas®™ and Anshul Kundaje®¹²

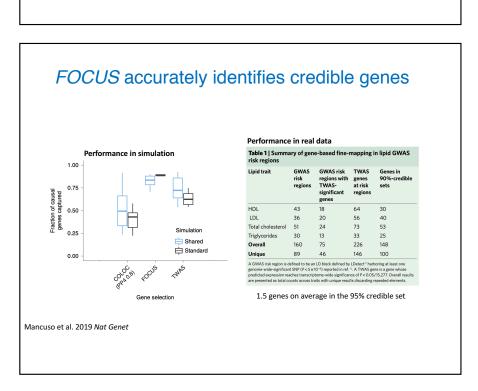
### Probabilistic fine-mapping of TWAS

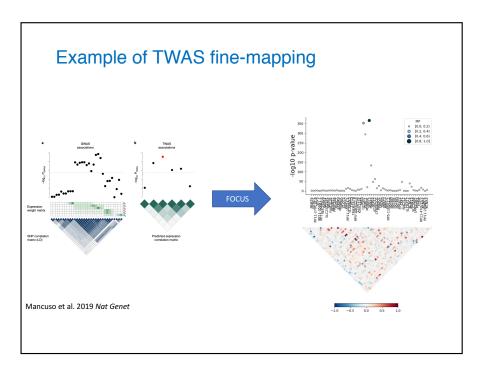
GWAS: Fine-mapping multiple associated SNPs in LD at a locus

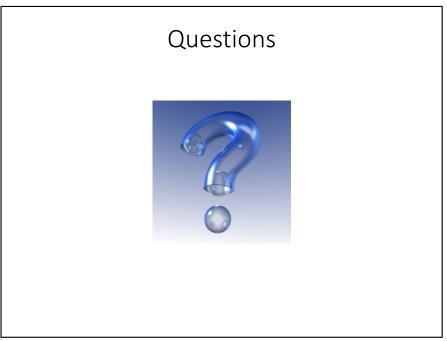


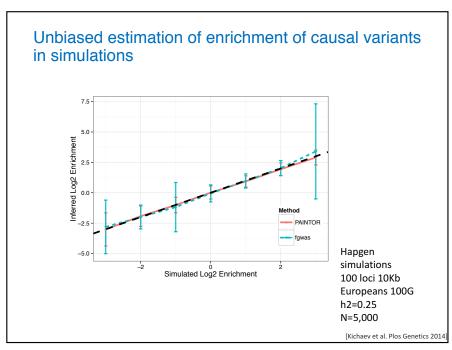
Mancuso et al. 2019 Nat Genet

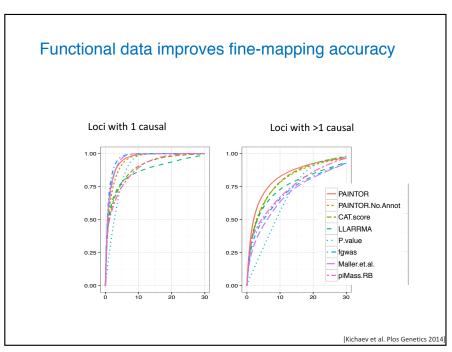
# Probabilistic fine-mapping of TWAS GWAS: Fine-mapping multiple associated SNPs in LD at a locus TWAS: Fine-mapping multiple gene models → posterior probability for each gene → credible sets (FOCUS) Mancuso et al. 2019 Nat Genet

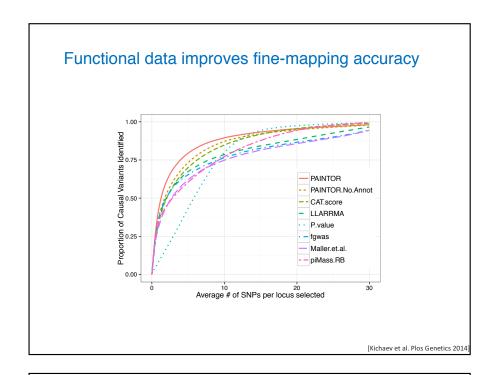


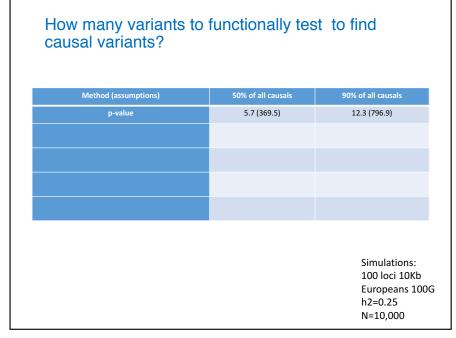












### How many variants to functionally test to find causal variants?

Method (assumptions)	50% of all causals	90% of all causals
p-value	5.7 (369.5)	12.3 (796.9)
Probabilities (single causal per locus) (Maller et al NG'12)	2.7 (172.4)	25.0 (1616.1)

Simulations: 100 loci 10Kb Europeans 100G h2=0.25 N=10,000

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PAINTOR (multiple causals)	1.7 (108.9)	11.4 (734.4)
PAINTOR (multiple causals; with ENCODE)	1.2 (78.7)	9.7 (625.6)

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PAINTOR (multiple causals; with ENCODE)	1.2 (78.7)	9.7 (625.6)
PAINTOR* (multiple causals; true ENCODE prior)	1.2 (77.9)	9.4 (610.6)

Simulations: 100 loci 10Kb Europeans 100G h2=0.25 N=10,000

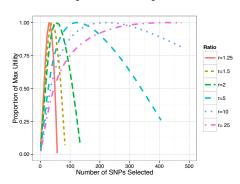
### Assuming 1 causal per locus yields miss-calibrated causal sets

Causal Set	Method	Annotations	# Causals	# SNPs
90%	Maller et al.	-	63.2	325.5
95%	Maller et al.	-	68.8	409.8
99%	Maller et al.	-	76.7	579.4

[Kichaev et al. Plos Genetics 2014]

### How many SNPs to follow-up?

- Depends on ratio of benefit of finding a causal variant to cost of testing a variant (r=B/C)
  - r=10 → the benefit of finding a causal outweighs 10 times the cost of testing 1 SNP



r=10,  $\sim$ 3.8 SNPs per locus to identify  $\sim$ 72.6% of all causals r=100,  $\sim$ 13.1 SNPs per locus to identify  $\sim$ 96.2% of all causals

[Kichaev et al. Plos Genetics 2014]

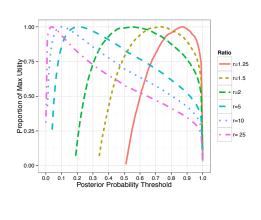
### Assuming 1 causal per locus yields miss-calibrated causal sets

Causal Set	Method	Annotations	# Causals	# SNPs
	Maller et al.	-	63.2	325.5
90%	PAINTOR	-	90.1	569.4
	PAINTOR	+	89.9	461.0
-	Maller et al.	-	68.8	409.8
95%	PAINTOR	-	95.8	741.4
	PAINTOR	+	95.6	628.8
	Maller et al.	-	76.7	579.4
99%	PAINTOR	-	101.5	1118.9
	PAINTOR	+	101.6	1001.8

[Kichaev et al. Plos Genetics 2014

### How many SNPs to follow-up?

 Thresholding on posterior probability of causality gives a principled way of maximizing utility.



[Kichaev et al. Plos Genetics 2014]

### Other considerations

- Locus size (function of LD):
  - Increasing locus size increases performance of PAINTOR vs existing methods
    - 10Kb: 27.4 vs 11.4 variants to follow-up to find 90% of causals
    - 50Kb: 110.7 vs 24.1 variants to follow-up to find 90% of causals
- Causal not in the data:
  - Median distance in Kb increases by ~6%
    - 21.6 vs 22.0 median Kb to the top 10 SNPs
    - 1.6 vs 4.0 minimum Kb to the top 10 SNPs
- Sample size
  - 19.0, 12.5, 10.8 variants per locus to find 90% of all causals for 2.5k, 5k and 10k samples

### Yale

# From cross-phenotype associations to pleiotropy in human genetic studies

### Andrew DeWan, PhD, MPH

Associate Professor of Epidemiology
Co-Director, Yale Center for Perinatal, Pediatric and Environmental Epidemiology
Yale School of Public Health

Work done in collaboration with Yasmmyn Salinas, PhD, MPH, Assistant Professor of Epidemiology, Yale School of Public Health

Yale school of public health

### **Pleiotropy**

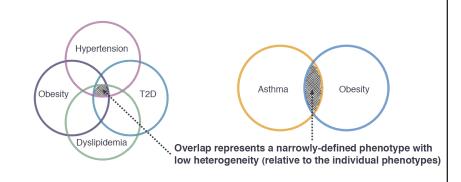
- Phenomenon in which a genetic locus affects more than one trait or disease
- Molecular level
  - Single gene with multiple physiological functions
  - Two domains of a single gene product with different functions and affecting multiple phenotypes
  - Gene product with a single function that affects multiple phenotypes be acting in multiple tissues
- Statistical level
  - A locus displaying cross-phenotype associations is often considered pleiotropic

2

### Pleiotropy and disease comorbidity

- Examples of correlated (comorbid) disease
  - Obesity, hypertension, dyslipidemia, type 2 diabetes (metabolic disorder)
  - Depression, anxiety, personality disorders (psychiatric disorder)
  - Asthma, obesity (pro-inflammatory conditions)
- Why do certain disease occur together
  - Causality
  - Shared environmental risk factors
  - Shared genetic risk factors

# Pleiotropy and disease comorbidity



### Pleiotropy and disease comorbidity

- Pleiotropy-informed analyses consider multiple phenotypes together and take into account the correlation between the phenotypes
  - Analyzing multiple correlated phenotype (e.g. comorbid diseases) is equivalent to analyzing a single narrowly-defined phenotype with low heterogeneity

### Pleiotropy and disease comorbidity

- Detecting shared genetics and/or molecular pathways between comorbid diseases can help us understand exactly how the etiology of the diseases overlap
- Etiologic overlaps:
  - provide opportunities for novel interventions that prevent or treat the comorbidity, rather than preventing/treating each disease separately
  - facilitate drug repurposing (that is, known drugs targeting a pleiotropic locus may be repurposed to treat other diseases controlled by that locus, precluding the need for the development and testing of a brand-new drug)

Expression of autism spectrum and schizophrenia in patients with a 22q11.2 deletion

Jacob A.S. Vorstman a,\*, Elemi J. Breetvelt a, Kirstin I. Thode b, Eva W.C. Chow c,d, Anne S. Bassett c,d

- <sup>a</sup> Rudolf Magnus Institute of Neuroscience, Department of Psychiatry, University Medical Center Utrecht, Utrecht, The Netherlands
- b Department of Psychiatry, Malcolm Grow Medical Center, Joint Base Andrews, Andrews AFB, MD, USA
- Clinical Genetics Research Program, Centre for Addiction and Mental Health, Toronto, Ontario, Canado Department of Psychiatry, University of Toronto, Toronto, Ontario, Canada

Schizophrenia Research 143 (2013) 55-59

Autistic symptoms and probable ASD during childhood, assessed in 77 adults with 22q11,2DS, comparing those with and without schizophrenia

	Total (n=77)	22q11,2DS-SZ (n=36)	22q11,2DS-Co (n=41)	p				
Mean SRS T-score (95% CI)	73.1 (69.7-76.6)	72,4 (67,3-78,0)	73.7 (68.9-78.6)	0,36				
Subjects categorized as probable ASD	n (%)	n (%)	n (%)	p	Uncorrected OR (95% CI)	p	Corrected OR (95% CI)	p
SRS T score cut-off 60 SCQ cut-off 15 SCQ cut-off 12	59 (76.6%) 13 (16.9%) 27 (35.1%)	27 (75.0%) 3 (8.3%) 13 (36.1%)	32 (78.0%) 10 (24.4%) 14 (34.1%)	0.75 <sup>b</sup> 0.06 <sup>b</sup> 0.86 <sup>b</sup>	0.84 (0.29-2.43) 0.28 (0.07-1.12) 1.10 (0.44-2.78)	0.75 0.07 0.86	0.36 (0.085-1.52) 0.20 (0.03-1.46) 1.53 (0.49-5.27)	0.17 <sup>c</sup> 0.11 <sup>d</sup> 0.49 <sup>d</sup>

- CI = confidence interval <sup>a</sup> Mann-Whitney-Wilcoxon,
- <sup>c</sup> Corrected for age and IO.

d Corrected for gender, age, IQ.

Background: Copy number variants (CNVs) associated with neuropsychiatric disorders are increasingly being identified. While the initial reports were relatively specific, i.e. implicating vulnerability for a particular neuropsychiatric disorder, subsequent studies suggested that most of these CNVs can increase the risk for more than one neuropsychiatric disorder. Possibly, the different neuropsychiatric phenotypes associated with a single genetic variant are really distinct phenomena, indicating pleiotropy. Alternatively, seemingly different disorders could represent the same phenotype observed at different developmental stages or the same underlying pathogenesis with different phenotypic expressions.

Aims: To examine the relation between autism and schizophrenia in patients sharing the same CNV. Method: We interviewed parents of 78 adult patients with the 22q11.2 deletion (22q11.2DS) to examine if autistic symptoms during childhood were associated with psychosis in adulthood. We used Chi-square, T-tests and logistic regression while entering cognitive level, gender and age as covariates.

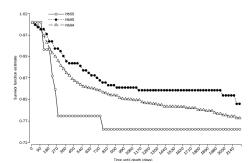
Results: The subgroup of 22q11.2DS patients with probable ASD during childhood did not show an increased risk for psychosis in adulthood. The average SRS scores were highly similar between those with and those with

Conclusions: ASD and schizophrenia associated with 22q11.2DS should be regarded as two unrelated, distinct phenotypic manifestations, consistent with true neuropsychiatric pleiotropy. 22q11.2DS can serve as a model to examine the mechanisms associated with neuropsychiatric pleiotropy associated with other CNVs.

### Protective effects of the sickle cell gene against malaria morbidity and mortality

Michael Aidoo, Dianne J Terlouw, Margarette S Kolczak, Peter D McElroy, Feiko O ter Kuile, Simon Kariuki, Bernard L Nahlen, Altaf A Lai, Venkatachalam Udhavakuma

Lancet 2002: 359: 1311-12



	Crude Incid	ience/1000 persoi	n-months	Adjusted relative r	Adjusted relative risk (95% CI)			
	HbAA	Hbas	HbSS	Hbas vs Hbaa	р	HbSS vs HbAA	р	
Severe malaria anaemia episodes	4-0	2-0	1.5	0-40 (0-30-0-60)	0.0001	0-29 (0-1-0-9)	0.04	
All severe anaemia episodes (Hb <6 g/dL plus any parasitaemia)	8-8	6-8	7.5	0-61 (0-46-0-80)	0-0006	0-63 (0-35-1-2)	0-15	
High density parasitaemia episodes	20	17-3	15.8	0-73 (0-65-0-84)	0.0001	0-52 (0-36-0-74)	0.0002	

moglobin. HbSS was associated with lower parasite incidence than HbAA haemoglobin levels and parasitaemia were determined using routine monthly fingerprick blood samples and samples collected any time the children were reported ill. All data points collected monthly for the entire time children participated in the study were used in data analyses unless indicated otherwise. Only birthweight among the various covariates considered (same as for survival analysis) was controlled

### Pleiotropy in gene mapping

- Mapping a single genotype to multiple phenotypes has the potential to uncover novel links between traits or diseases
- It can also offer insights into the mechanistic underpinnings of known comorbidities
- It can increase power to detect novel associations with one or more phenotypes

# A practitioners' guide for studying pleiotropy in genetic epi studies

Am J Epidemiol. 2017 Aug 11. doi: 10.1093/aje/kwx296. [Epub ahead of print]

Statistical Analysis of Multiple Phenotypes in Genetic Epidemiological Studies:From Cross-Phenotype Associations to Pleiotropy.

Salinas YD, Wang Z, DeWan AT

### Abstra

In the context of genetics, pleiotropy refers to the phenomenon in which a single genetic locus affects more than one trait or disease. Genetic epidemiological studies have identified loci associated with multiple phenotypes, and these cross-phenotype associations are often incorrectly interpreted as examples of pleiotropy. Pleiotropy is only one possible explanation for cross-phenotype associations. Cross-phenotype associations may also arise due to issues related to study design, confounder bias, or non-genetic causal links between the phenotypes under analysis. Therefore, it is necessary to dissect cross-phenotype associations over true pleiotropic loci. In this review, we describe statistical methods that can be used to identify robust statistical evidence of pleiotropy. First, we provide an overview of univariate and multivariate methods for discovery of cross-phenotype associations and highlight important considerations for choosing among available methods. Then, we describe now to dissect cross-phenotype associations by using mediation analysis. Pleiotropic loci provide insights into the mechanistic underpinnings of disease comorbidity, and may serve as novel targets for interventions that simultaneously treat multiple diseases. Discerning between different types of cross-phenotype associations is necessary to realize the public health potential of pleiotropic loci.

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KEYWORDS: genetic epidemiology; mediation analysis; pleiotropy

# Guidelines for generating robust statistical evidence of pleiotropy

**Discover** CP associations



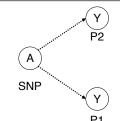
Dissect CP associations



Classify them as examples of biological, mediated, or spurious pleiotropy

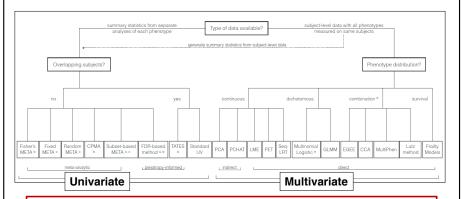
### Cross-phenotype (CP) associations

Statistical associations between a **single genetic locus** – a single gene or a single variant within a gene – and **multiple phenotypes** 



Note that the dashed lines denote uncertainty about whether the SNP has a direct effect on the phenotypes.

# Analytic options for discovery of CP associations



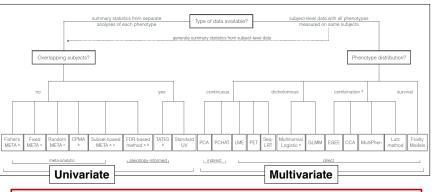
### Key distinction:

- Univariate methods examine the association between a given SNP and each trait separately
- Multivariate methods examine the association between a given SNP and each trait by modeling the traits *jointly*

# Univariate methods are by far the most commonly used to detect CP associations

- Univariate methods include (but are not limited to) the methods you've discussed in class so far:
  - · allelic Chi-Square test
  - genotypic Chi-Square test
  - · regression-based methods
- The overall approach is to:
  - obtain univariate association p-values for each phenotype
  - declare CP associations at genetic loci that are statistically significantly associated with each phenotype

## Analytic options for discovery of CP associations



Choice between univariate and multivariate approaches depends on:

- Types of data available on our phenotypes of interest
  - · Summary statistics vs. individual-level data?
  - Are the phenotypes measured on the same subjects?
- Distribution of the phenotypes (e.g., quantitative or disease trait)

# Hypothetical example: Discovery of CP associations for hypertension and heart disease by using logistic regression

### Step 1. Fit two univariate regression models within PLINK

 $E[hypertension] = \beta_0 + \beta_1 * SNP$ 

 $E[heart\ disease] = \beta_0 + \beta_1 * SNP$ 

Word of caution: The univariate tests of association should be marginal tests (conducted irrespectively of the second phenotype) NOT conditional tests (conducted on a subset defined based on absence/presence of the second phenotype). In this example, what that means is that the regression for hypertension should be fit on all subjects irrespectively of their heart disease status; and the regression for heart disease should be fit on all subjects irrespectively of their hypertension status. More on this later!

EVIDENCE to deciate a OF association at this OIVI

# Hypothetical example: Discovery of CP associations for hypertension and heart disease by using logistic regression

### Step 1. Fit two univariate regression models within PLINK

```
E[hypertension] = \beta_0 + \beta_1 * SNP

E[heart\ disease] = \beta_0 + \beta_1 * SNP
```

Step 2. For a given SNP, examine p-values for  $\beta_1$  from <u>each</u> model.

- P-value for  $\beta_1$  in hypertension model = 1.03 x 10<sup>-12</sup>
- P-value for  $\beta_1$  in heart disease model = 6.02 x 10<sup>-9</sup>

Step 3. Declare CP associations at a given SNP, if the p-values for  $\beta_1$  in each model surpass the study significance threshold.

Assuming the standard GWAS significance threshold (alpha=5 x10-8), there is a statistically significant association with both hypertension and heart disease at this particular SNP. Therefore, we have sufficient statistical evidence to declare a CP association at this SNP.

Using multivariate methods to increase the power to detect cross-phenotype associations

# A comparison of univariate and multivariate GWAS methods for analysis of multiple dichotomous phenotypes

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Genet. Epidemiol. 41 (7), 689-689

### Statistical power of multi-trait methods

- For *quantitative* trait methods, it has been shown that:
  - Multivariate analyses achieve greater power than univariate analyses both in the presence (Allison 1998) and absence of cross-trait genetic correlation or pleiotropy (Galesloot 2014)
- Therefore, joint analysis of *quantitative* phenotypes has the potential to enhance the statistical power of genetic studies.

### Statistical power of multi-trait methods

- With this potential for greater statistical power, multivariate methods could contribute to the investigation of the 'missing heritability' of complex diseases.
- However, it is unknown whether the trends observed for quantitative traits also hold for methods that can analyze multiple disease (case-control) phenotypes.
- Understanding the performance of these methods is essential to their successful application to real data.

### Objective

 To evaluate the relative statistical power of methods for analysis of two disease (case/control) phenotypes in the presence and absence of pleiotropy using simulated genotype and phenotype data.

### **Data Simulation**

- Genotypes were simulated for a bi-allelic SNP with MAF =
   0.20 by sampling two alleles independently from a binomial distribution.
- Genotypes (coded as 0/1/2) are the sum of the two alleles.

### Simulation scenarios

# traits associated	h <sub>i</sub> <sup>2</sup>	r <sub>Y1,Y2</sub>	P <sub>j</sub>
1	h <sub>1</sub> <sup>2</sup> =0.1%,h <sub>2</sub> <sup>2</sup> =0%	[-0.9,0.9]	P1 = P2 = 10%
			P1 = P2 = 20%
			P1 = 10%, P2 = 20%
			P1 = 20%, P2 = 10%
2	$h_1^2 = h_2^2 = 0.1\%$	[-0.9,0.9]	P1 = P2 = 10%
			P1 = P2 = 20%
			P1 = 10%, P2 = 20%
			P1 = 20%, P2 = 10%
2	$h_1^2 = 0.1\%, h_2^2 = 0.05\%$	[-0.9,0.9]	P1 = P2 = 10%
			P1 = P2 = 20%
			P1 = 10%, P2 = 20%
			P1 = 20%, P2 = 10%

### Methods evaluated

### 1. Standard univariate approach

· models fitted

logit[E(Y<sub>i1</sub>)] = 
$$\beta_0 + \beta_1 X_i$$
  
logit[E(Y<sub>i2</sub>)] =  $\beta_0 + \beta_1 X_i$ 

- · p-value extracted
  - the minimum of the two univariate p-values

### 2. Reversed ordinal logistic regression (MultiPhen)

· model fitted

logit[E(
$$X_i \le c$$
] =  $\alpha_c$  +  $\beta_1 Y_{i1}$  +  $\beta_2 Y_{i2}$ , for  $c$  = 1, 2, or 3 genotype categories

- · p-value extracted
  - the p-value for a Likelihood Ratio Test for model fit, evaluating the null hypothesis that  $\beta_1 = \beta_2 = 0$

### 3. Generalized estimating equations (GEEs)

· model fitted

$$logit[E(Y_{ij})] = \beta_0 + \beta_1 j_i + \beta_2 X_i + \beta_{12} X_i j_i$$

- · p-value extracted
- the p-value for the test of the hypothesis that  $\beta_2 = \beta_{12} = 0$

### 4. Generalized linear mixed models (GLMMs)

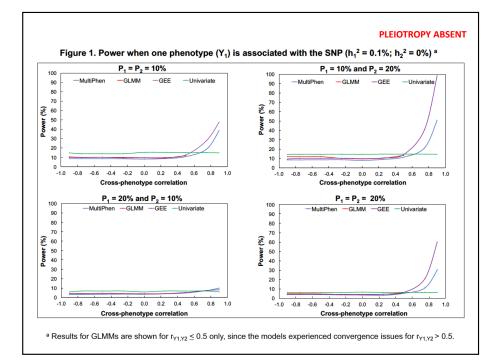
· model fitted

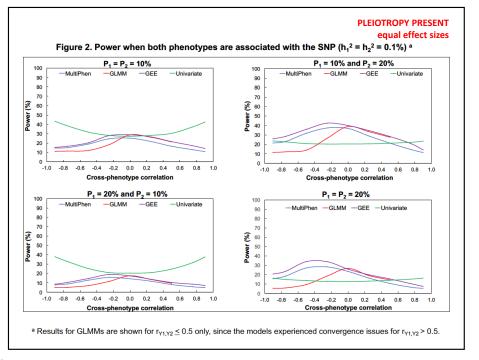
$$logit[E(Y_{ii})] = \beta_0 + \beta_1 j_i + \beta_2 X_i + \beta_{12} X_i j_i + b_{ii}$$

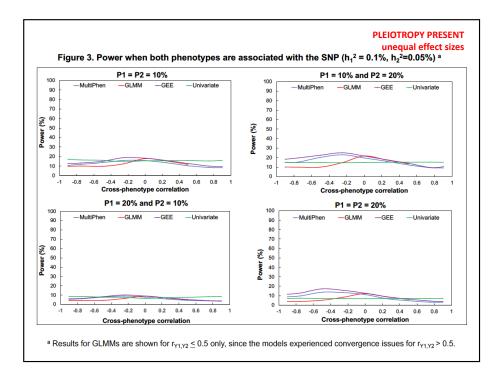
- · p-value extracted
  - the p-value for the test of the hypothesis that  $\beta_2 = \beta_{12} = 0$
- \* Y<sub>ij</sub> represent the case/control status of the i<sup>th</sup> subject, measured for phenotypes j = 1 or 2; X<sub>i</sub> are the individual genotypes; b<sub>ij</sub> are the random effects correlated within the i<sup>th</sup> subject; and j<sub>i</sub> is an indicator variable for the phenotypes (coded as 0/1).

### Power

 We defined power as the percentage of the 10,000 replicates for which the extracted p-value for a given scenario was smaller than a genome-wide significance level of 5x10<sup>-8</sup>.



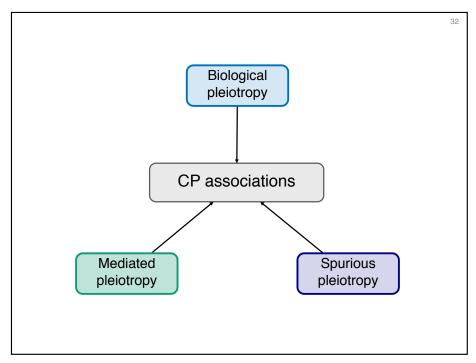




### Conclusions

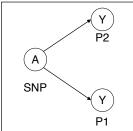
- The performance of the univariate approach appeared to complement that of multivariate methods, with notable patterns:
  - in the absence of pleiotropy, multivariate methods had better performance for r<sub>Y1,Y2</sub> > 0.5 while univariate methods had better performance for r<sub>Y1,Y2</sub> < 0.5</li>
  - in the presence of pleiotropy (positive genetic correlation), the multivariate approach lost power for r<sub>Y1,Y2</sub> > 0, while the univariate approach gained power across this range of values
- Thus, to improve GWAS discovery, it may be beneficial to use univariate and multivariate approaches in parallel.

Problem: CP associations need not be indicative of pleiotropy



### Biological pleiotropy

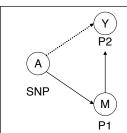
Independent associations between a genetic locus (A) and multiple phenotypic outcomes (Y)



The SNP has a direct effect on each phenotype. (Note that direct or causal effects are depicted with solid lines).

### Mediated pleiotropy

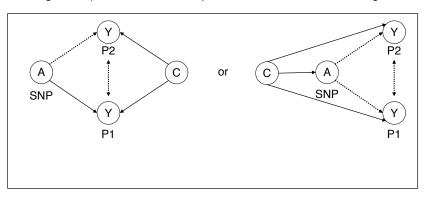
Association between a genetic locus (A) and an intermediate phenotype (M) that causes a second phenotypic outcome (Y)



A non-genetic causal link between M and Y induces an association between A and Y, even in the absence of a direct effect of A on Y.

Spurious pleiotropy

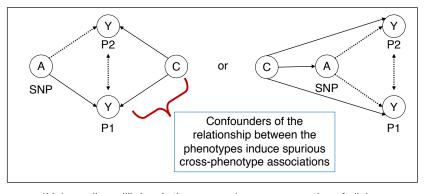
Artifactual associations with multiple phenotypes due to issues related to study design, confounding, or associations with markers in strong linkage disequilibrium\* with multiple causal variants in different genes



\*Linkage disequilibrium is the non-random co-segregation of alleles.

### Spurious pleiotropy

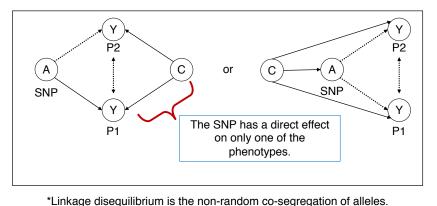
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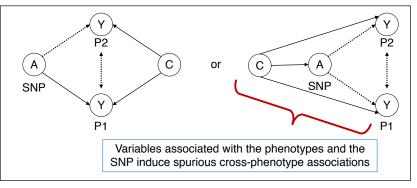
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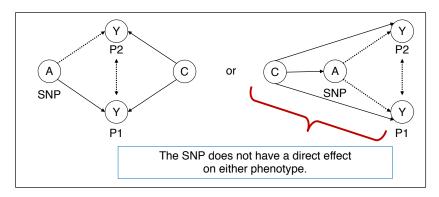
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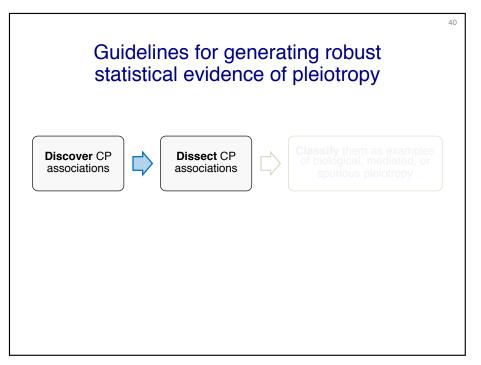
\*Linkage disequilibrium is the non-random co-segregation of alleles.

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Artifactual associations with multiple phenotypes due to issues related to study design, confounding, or associations with markers in strong linkage disequilibrium\* with multiple causal variants in different genes

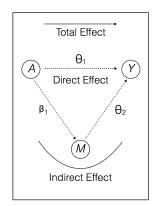


\*Linkage disequilibrium is the non-random co-segregation of alleles.



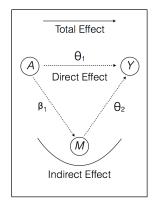
Mediation analysis provides a tool for dissecting CP associations

- Mediation analysis decomposes the total effect of the SNP (A) on a phenotypic outcome (Y) into:
  - Direct effect: effect of A on Y that occurs independently of an intermediate phenotype (M)
  - Indirect effect: effect of A on Y that occurs through the intermediate phenotype M



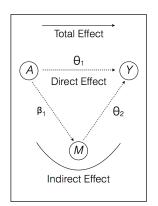
### Mediation analysis: Data requirements

- All phenotypes must be measured on the same subjects
- Temporality must be ascertained
  - The occurrence of the intermediate variable *M* must precede that of the phenotypic outcome variable *Y*



Mediation analysis: Assumptions

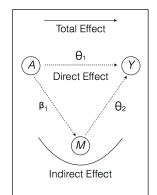
- There must be no unmeasured:
  - confounders of the total effect
  - confounders of the relationship between SNP A and the mediator M
  - confounders of the relationship between mediator M and phenotypic outcome Y



### Mediation analysis: Assumptions

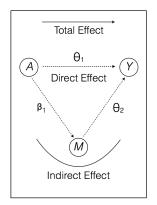
Typically met in genetic epi studies!

- There must be no unmeasured:
  - confounders of the total effect
  - confounders of the relationship between SNP A and the mediator M
  - confounders of the relationship between mediator M and phenotypic outcome Y



### Mediation analysis: Assumptions

- There must be no unmeasured:
  - confounders of the total effect
  - confounders of the relationship between SNP A and the mediator M
  - confounders of the relationship between mediator M and phenotypic outcome Y



Requires adjustment for <u>known</u> confounders to prevent bias (<u>Note</u>: this effectively restricts the use of mediation analyses to datasets in which data on such variables have been collected)

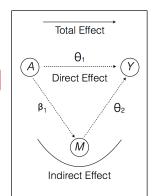
### Mediation analysis: Regression-based approach

 Requires fitting two regression models, one for mediator M and one for phenotypic outcome Y:

• 
$$E[M \mid a, c] = \beta_0 + \beta_1 a + \beta_2' c$$

• 
$$E[Y | a, m, c] = \theta_0 + \theta_1 a + \theta_2 m + \theta_4' c$$

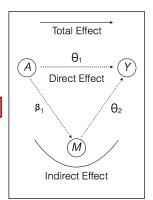
Assesses the effect of A on M, while controlling for measured confounders (C)



### Mediation analysis: Regression-based approach

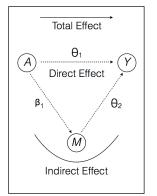
- Requires fitting two regression models, one for mediator M and one for phenotypic outcome Y:
  - $E[M | a, c] = \beta_0 + \beta_1 a + \beta_2' c$
  - $E[Y | a, m, c] = \theta_0 + \theta_1 a + \theta_2 m + \theta_4' c$

Assesses the effect of A on Y, while controlling for both M and C



### Mediation analysis: Regression-based approach

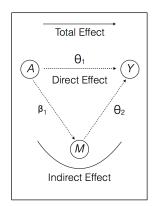
- Requires fitting two regression models, one for mediator M and one for phenotypic outcome Y:
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  - $E[Y | a, m, c] = \theta_0 + \theta_1 a + \theta_2 m + \theta'_4 c$
- The parameter estimates from these models (namely  $\beta_1$ ,  $\theta_1$ , and  $\theta_2$ ) are used to estimate the direct and indirect effects



# Guidelines for generating robust statistical evidence of pleiotropy Discover CP associations Dissect CP associations Classify them as examples of biological, mediated, or spurious pleiotropy

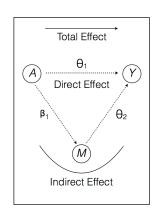
### Mediation analysis: Interpretation

**Biological pleiotropy:** SNP A is associated with mediator M, and the total effect of SNP A on phenotypic outcome Y is equal to its direct effect (i.e., the indirect effect is equal to 0)



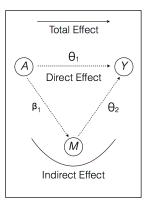
### Mediation analysis: Interpretation

- Mediated pleiotropy
- Complete mediation:
- SNP A is associated with mediator M and the total effect of A on phenotypic outcome Y is equal to its indirect effect (i.e., the direct effect is equal to 0).
- Incomplete mediation:
- SNP A is associated with mediator M and A has both direct and indirect effects on phenotypic outcome Y (i.e., the total effect is equal to the sum of the direct and indirect effects)



### Mediation analysis: Interpretation

- Spurious pleiotropy
- SNP A is not associated with mediator M after controlling for measured confounders



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### mediation R package

- > med.fit<-qlm(W1~rs1 2, data=combined, family=binomial("logit"))
- > out.fit<-glm(W2~W1+rs1\_2, data=combined, family=binomial("logit"))
- > med.out<-mediate(med.fit,out.fit, treat="rs1\_2", mediator="W1", boot=TRUE, boot.ci.type="bca", sims=1000)
- > summary(med.out)

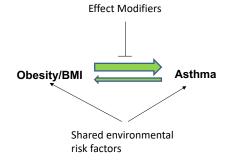
Causal Mediation Analysis

Nonparametric Bootstrap Confidence Intervals with the BCa Method

	Estimate 9	95% CI Lowe	r 95% CI U	lpper p-value
ACME (control)	0.02152	0.01823	0.03	<2e-16 ***
ACME (treated)	0.02199	0.01868	0.03	<2e-16 ***
ADE (control)	0.00723	0.00415	0.01	<2e-16 ***
ADE (treated)	0.00771	0.00443	0.01	<2e-16 ***
Total Effect	0.02922	0.02461	0.03	<2e-16 ***
Prop. Mediated (control)	0.73634	0.65429	0.84	<2e-16 ***
Prop. Mediated (treated)	0.75247	0.67272	0.85	<2e-16 ***
ACME (average)	0.02175	0.01847	0.03	<2e-16 ***
ADE (average)	0.00747	0.00426	0.01	<2e-16 ***
Prop. Mediated (average)	0 74441	0.66254	0.84	<2e-16 ***

### Empirical searches for pleiotropic loci for asthma and obesity

### Asthma-obesity comorbidity



Ford ES. The epidemiology of obesity and asthma. J Allergy Clin Immunol. 2005;115(5):897-909; quiz 10.

Studies DR. Obestay and asthmat: The Chicken or the egg? J Allergy Clin Immunol. 2004.

Kim SH, Obstay BD. Obestay and asthmat: The Chicken or the egg? J Allergy Clin Immunol. 2014.

Kim SH, Sutherland ER, Gelfand EW. Is there a link between obesity and asthma? Allergy Asthma Immunol Res. 2014;6(3):189-95.

Egan KB, Ettinger AS, DeWan AT, Holford TR, Holmen TL, Bracken MB. Longitudinal associations between asthma and general and abdominal weight status among Norwegian adole: the HNIY Study. Pediatric obesity. 2014.

Am J Hum Genet. 2009 Jul;85(1):87-96. doi: 10.1016/j.ajhg.2009.06.011. Epub 2009 Jul 2.

PRKCA: a positional candidate gene for body mass index and asthma.

Murphy A1, Tantisira KG, Soto-Quirós ME, Avila L, Klanderman BJ, Lake S, Weiss ST, Celedón JC.

### Study design

- Two phases:
  - genome-wide linkage analysis of BMI
  - follow-up family-based candidate-gene association study of BMI and asthma
- Strategy for candidate-gene study:
  - Authors focused on a single gene (PRKCA) within the BMI linkage peak because:
    - animal models suggest role of PRKCA in obesity; and
    - published association studies of other genes within the linkage peak had found no association with BMI.

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### Study population

- Costa Rica study
  - N = 415 asthmatic children + parents
- · Childhood Asthma Management Program
  - N = 493 non-Hispanic White asthmatic children + parents

Note that ALL children in both study populations are asthmatic

### Phenotype definitions

- Body mass index (BMI)
  - · calculated from objective measures of height and weight
- Asthma
  - physician-diagnosed asthma + one of the following:
    - · 2 respiratory symptoms or asthma attacks in prior year
    - increased airway responsiveness or bronchodilator response

Statistical methods

- Univariate family-based association tests (FBATs) were used to test PRKCA SNPs for association with BMI and asthma separately
  - Note: The FBAT statistic takes into account the phenotype of the offspring only
- Significance threshold used by study authors:  $\alpha = 9.5 \times 10^{-5}$

Results for BMI Table 3. Evidence for Association of PRKCA with BMI in Costa Rica and CAMP mber of Informative offspring with 0/1 **Effect Size** Joint p Value (CR. CAMP  $(1.0 \times 10^{-4})$  $9.5 \times 10^{-5}$ 61868473 C 0.26 0.33 83 (60/23) 113 (83/39) 2.27 1.60 +0.0019+0.0039 (+0.0077) 120 (86/34) 136 (98/47) 1.69 1.21 Two BMI-associated variants

### Results for asthma

			Allele I	Frequency	Number of Info Families <sup>b</sup> (num with 0/1 recod	ber of offspring			
	Location (BP) <sup>a</sup>	Minor Allele	CR	САМР	CR	САМР	Costa Rica p Value <sup>c,d</sup>	CAMP Replication p Value <sup>c,d</sup> (two-sided)	Joint p Value <sup>c</sup> (CR, CAMP two-sided)
rs732191	61779673	G	0.46	0.35	168 (117/51)	141 113/43	-0.0194	-0.0214 (-0.0428)	0.0036 (0.0067)
rs9895580	61789701	С	0.47	0.35	168 (117/51)	141 114/43	-0.0171	-0.0160 (-0.0320)	0.0025 (0.0047)
rs4411531	61793662	A	0.29	0.12	88 (70/18)	25 (24/1)	-0.0058	-0.0058 (-0.0117)	0.0004 (0.0007)
rs8080771	61824330	G	0.46	0.35	164 (116/48)	108 (90/29)	-0.0161	-0.0070 (-0.0140)	0.0011 (0.0021)
rs11652956	61839798	G	0.29	0.12	83 (65/18)	23 (22/1)	-0.0101	-0.0111 (-0.0222)	0.0011 (0.0021)
rs7221968	61848731	С	0.27	0.11	79 (63/16)	18 (17/1)	-0.0122	-0.0216 (-0.0432)	0.0024 (0.0045)
rs7405806	61862056	A	0.49	0.31	164 (109/55)	90 (77/20)	-0.0309	-0.0009 (-0.0018)	0.0003 (0.0006)
rs11079657	61862528	A	0.38	0.23	129 (94/35)	60 (56/8)	-0.0092	-0.0002 (-0.0004)	$2.6 \times 10^{-5}$ ** (5.0 × $10^{-5}$ **)

One asthma-associated variant

### **Conclusions**

- Authors' conclusion: PRKCA displays pleiotropy for asthma and BMI (pleiotropy at gene level)
  - Two variants (rs228883 and rs1005651) displayed statistically significant associations with body mass index
  - A different variant (rs11079657) displayed a statistically significant association with asthma.

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### **Conclusions**

- Our conclusion: PRKCA is associated with asthma and with BMI among asthmatics (no true CP association!)
  - There is insufficient evidence to declare a CP association at PRKCA because the test of association with BMI was not a marginal test
    - FBAT test for BMI only took into account the phenotype of the offspring – which were ALL asthmatic
  - Thus, it remains to be seen whether the association with BMI is also present among non-asthmatics subjects
  - Without that information, we would not be able to assess whether asthma is a mediator or a moderator of the relationship between PRKCA and BMI.

A GWAS study: Salinas et al. (In Press)

Discovery and mediation analysis of cross-phenotype associations with asthma and body mass index in 12q13.2  $\,$ 

Salinas YD, Wang Z, and DeWan AT

### Study design

- Two parts:
  - Genome-wide search for cross-phenotype associations with asthma and body mass index
  - Follow-up mediation analysis to dissect genome-wide significant CP associations

### Study population

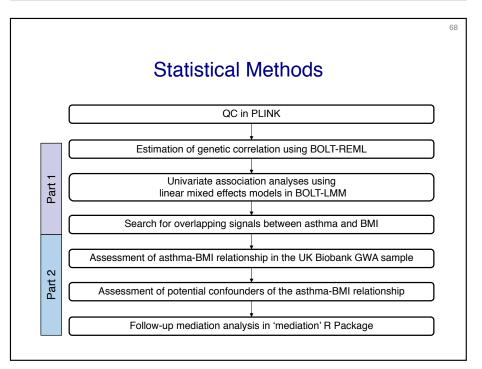
 N = 305,945 White, British subjects from the UK Biobank (a population-based prospective cohort study of > 500,000 subjects, aged 40-69 years at baseline)

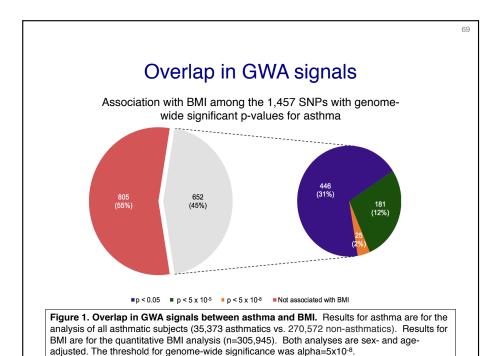


### Phenotype definitions

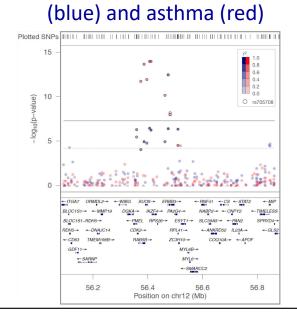
- BMI at baseline (kg/m²):
  - calculated based on height and weight measurements collected by trained UK Biobank staff at the recruitment sites
- Asthma diagnosed prior to baseline (yes/no):
  - ascertained via the question "Has a doctor ever told you that you had asthma?"
  - <u>Note</u>: In mediation analyses, two subgroups were created based on age-at-diagnosis

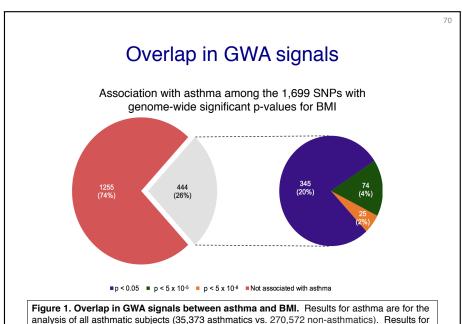






# Regional plot around rs705708 for BMI





### Cross-phenotype associations in 12q13.2

BMI are for the quantitative BMI analysis (n=305,945). Both analyses are sex- and age-

adjusted. The threshold for genome-wide significance was alpha=5x10-8.

Table 2. Cross-phenotype associations in 12q13.2 a

					Asthma		BMI <sup>c</sup>	
SNP	Gene	BP	Effect/reference allele	EAF	OR (95% CI)	Pc	beta (95% CI)	$\mathbf{P}^{\mathrm{d}}$
rs2069408	CDK2	56,364,321	G/A	0.3388	1.04 (1.02, 1.06)	3.30x10 <sup>-6</sup>	-0.06 (-0.08, -0.04)	5.40x10 <sup>-7</sup>
rs1873914	RAB5	56,379,427	C/G	0.4237	1.06 (1.04, 1.08)	2.40x10 <sup>-12</sup>	-0.05 (-0.07, -0.02)	7.90x10 <sup>-5</sup>
rs705702 b	SUOX	56,390,636	G/A	0.3376	1.07 (1.05, 1.09)	3.10x10 <sup>-14</sup>	-0.05 (-0.08, -0.03)	1.10x10 <sup>-5</sup>
rs10876864 b	SUOX	56,401,085	G/A	0.4279	1.06 (1.04, 1.08)	1.50x10 <sup>-12</sup>	-0.05 (-0.07, -0.03)	1.60x10 <sup>-5</sup>
rs1701704	IKZF4	56,412,487	G/T	0.3433	1.07 (1.05, 1.09)	1.50x10 <sup>-14</sup>	-0.06 (-0.09, -0.04)	3.70x10 <sup>-7</sup>
rs2456973	IKZF4	56,416,928	C/A	0.3432	1.07 (1.05, 1.09)	1.50x10 <sup>-14</sup>	-0.06 (-0.08, -0.04)	6.00x10 <sup>-7</sup>
rs11171739 b	ERBB3	56,470,625	C/T	0.4337	1.06 (1.04, 1.07)	8.80x10 <sup>-11</sup>	-0.05 (-0.07, -0.03)	1.10x10 <sup>-5</sup>
rs2292239	ERBB3	56,482,180	T/G	0.3470	1.07 (1.05, 1.08)	4.50x10 <sup>-13</sup>	-0.06 (-0.08, -0.04)	4.20x10 <sup>-7</sup>
rs705708	ERBB3	56,488,913	A/G	0.4712	1.05 (1.03, 1.07)	7.20x10 <sup>-9</sup>	-0.06 (-0.09, -0.04)	1.30x10 <sup>-8</sup>
rs11171747b	ESYT1	56518408	T/G	0.6180	1.04 (1.02, 1.05)	2.90x10 <sup>-5</sup>	-0.06 (-0.08, -0.04)	4.50x10 <sup>-7</sup>

Abbreviations: BP = base-pair; BMI = body mass index; CI = confidence interval; EAF = effect allele frequency; OR = odds ratio; SNP = single-nucleotide

- Results shown for SNPs with  $p \le 5x10^{-8}$  for asthma and  $p \le 0.05$  for BMI.
- For intergenic SNPs, the nearest gene is listed, with priority given to genes directly downstream of variant.
- P-value from BOLT-LMM, derived using the standard "infinitesimal" mixed model. P-value from BOLT-LMM, derived using the Gaussian mixture model.

Decomposing the effect of rs705708 on BMI via mediation analysis

Among childhood asthmatics Adult asthmatics (n=16.801) and (n=4,817) and common set of noncommon set of non-asthmatics asthmatics (n=181.304) (n=181.304) total effect = -0.0656total effect = -0.0560direct effect = -0.0655 direct effect = -0.0582 rs705708 BMI rs705708 varies by sex asthma asthma indirect effect = -0.00013 indirect effect = 0.0022 **Population Average Population Average** 

**Note**: Effect estimates shown are adjusted for common determinants of asthma and BMI: age, sex, breast-feeding status, exposure to maternal smoking, and smoking status at asthma diagnosis (adult analyses only). Unless otherwise noted by an asterisk(\*), all paths are significant at the 0.05 level.

Conclusions

- rs705708 has a positive direct effect on asthma
  - · Stronger in magnitude for childhood asthma
- rs705708 has a negative direct effect on BMI
  - Consistent in magnitude and direction in analyses including childhood vs. adult asthmatics
- This suggests that locus 12q13.2, tagged by rs705708, has pleiotropic effects on asthma and BMI.

**Conclusions** 

- 12q13.2 is multigenic and our CP associations span genes CDK2, RAB5, SUOX, IZK4, RPS26, ERBB3, and ESYT1.
  - rs705708 is the top regional BMI signal and resides in ERBB3.
  - The top regional asthma signal, rs2456973, resides in IZKF4.
  - While rs705708 and rs2456973 could be in LD with the same causative variant in either ERBB3 or IKZF4 or another gene in 12q13.2, it is also possible that each variant could tag a distinct, trait-specific causative variant in different genes.
- Therefore, locus 12q13.2 displays pleiotropic effects on asthma and BMI, but this may not be an example of pleiotropy at the gene level (biological pleiotropy).

### Intro to population genetics

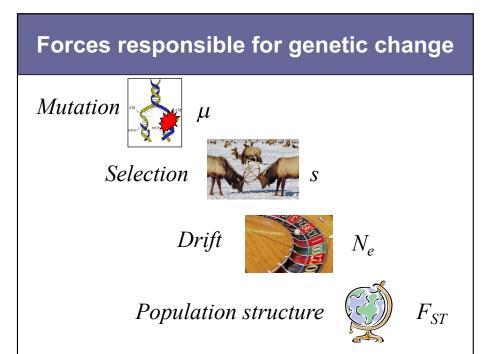
Shamil Sunyaev



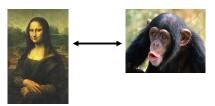


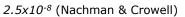
Broad Institute of M.I.T. and Harvard

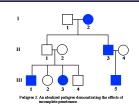
### **Mutations**



### Mutation rate in humans and flies







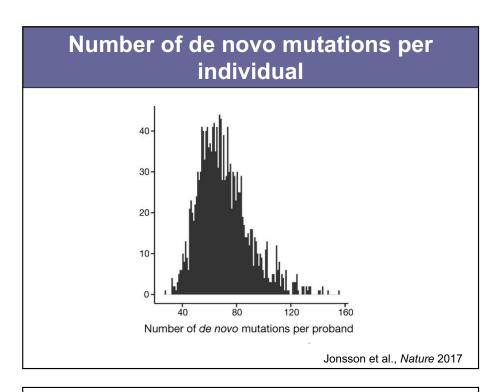
1.8x10<sup>-8</sup> (Kondrashov)

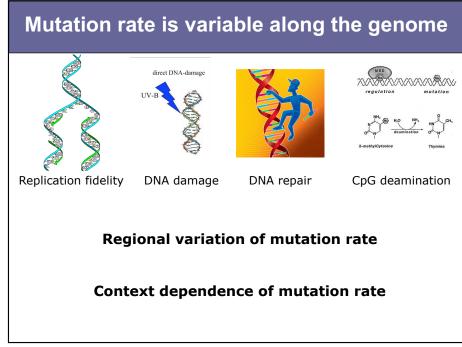
NGS estimates  $\sim 1.2 \times 10^{-8}$  per nt changes genome

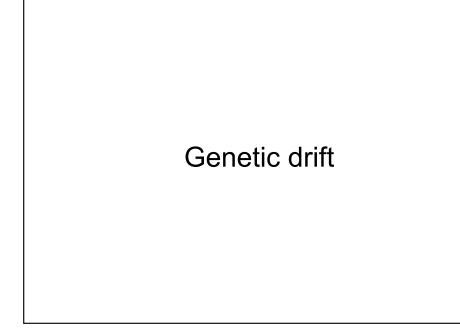
~70 per nt changes genome

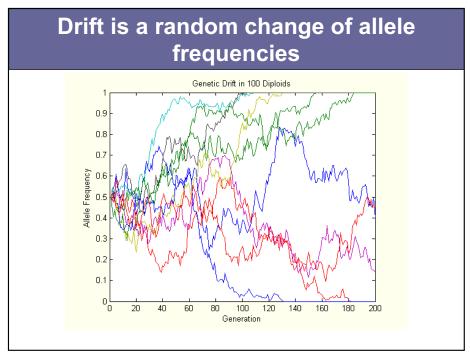
Other events: indels (10-9)

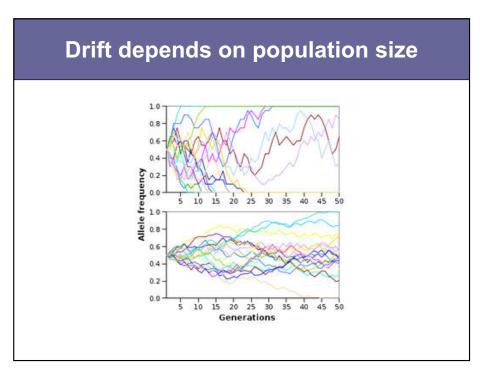
repeat extensions/contractions (10<sup>-5</sup>)



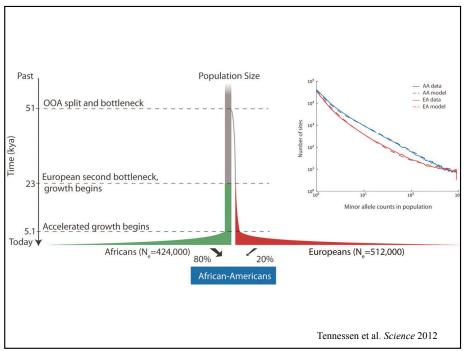








### Demographic history





# Selective effect of mutation Deleterious Neutral Advantageous

Selection indicates functional mutations, whether or not the tested trait is under selection

mutation

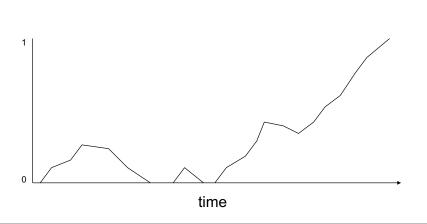
Nonfunctional

13

# Methods of mathematical population genetics

### **Dynamic of allelic substitution**

Mathematically, allele frequency change in a population follows a one-dimensional random walk



### **Diffusion approximation**

Random walk that does not jump long distances can be approximated by a diffusion process

$$\frac{\partial \phi(x, p, t)}{\partial t} = -\frac{\partial M\phi(x, p, t)}{\partial x} + \frac{1}{2} \frac{\partial^2 V\phi(x, p, t)}{\partial x^2}$$

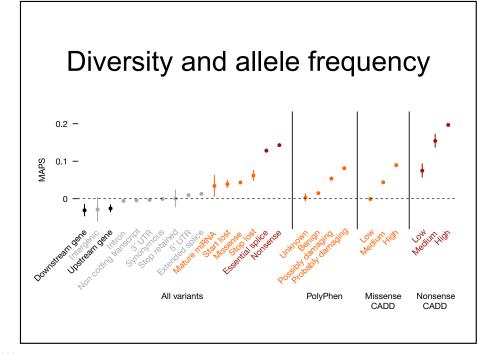
# Instead of modeling a population, we can model our sample Time goes backwards!

Natural selection in protein coding regions

### **Signatures of purifying selection**

Reduced variation

Excess of rare alleles

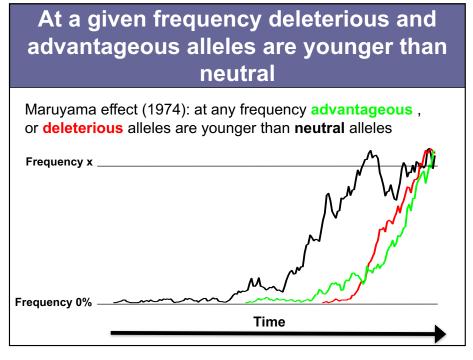


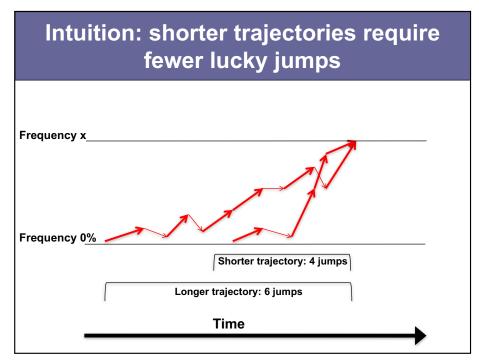
Am J Hum Genet 26:669-673, 1974

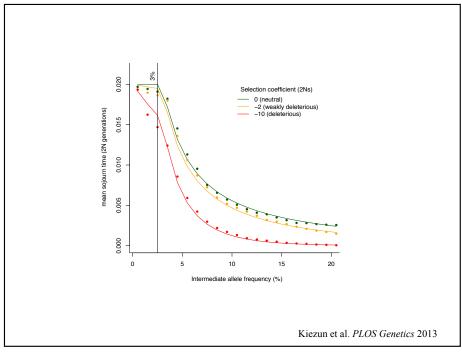
MAHLON V. R. FREEMAN, M.D.

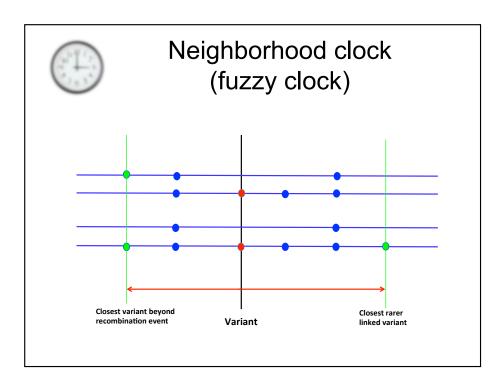
The Age of a Rare Mutant Gene in a Large Population

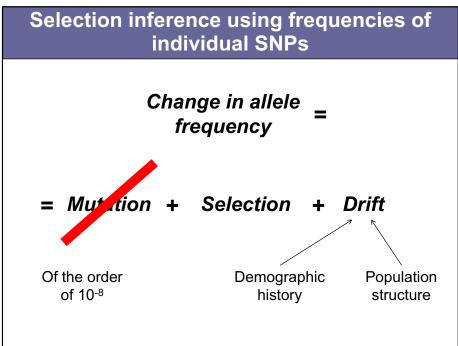
Takeo Maruyama<sup>1</sup>











### Focusing on rare deleterious PTVs

PTV – protein truncating variant (a.k.a. nonsense)

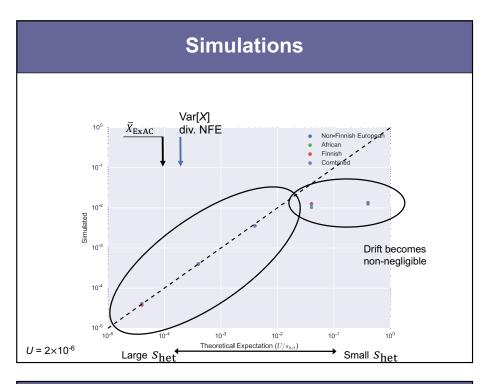
Combine all PTVs per gene – we assume that they have identical effects

Consider each gene as a bi-allelic locus – PTV / no PTV

# Selection inference using combined frequency of PTVs

Change in allele = frequency

Assuming string selection and a very large population, combined frequency of rare deleterious PTVs is expected to be Poisson distributed with  $\lambda$ =U/hs

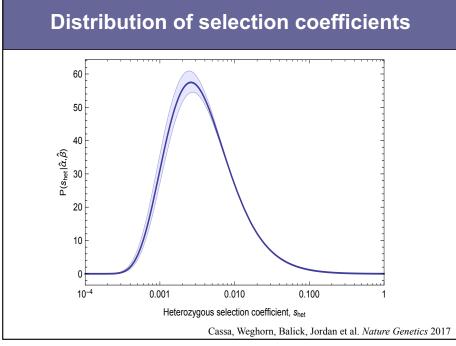


### The model

PTV counts in each gene are Poisson distributed but we lack sufficient data to estimate selection coefficients

We can treat selection coefficients as random variables with a distribution to be estimated

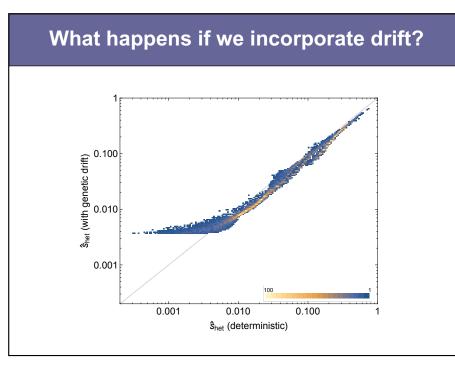
$$P(n|\alpha,\beta;\nu) = \int P(n|s_{\text{het}};\nu) P(s_{\text{het}};\alpha,\beta) \, ds_{\text{het}}$$



### **Estimates for each gene**

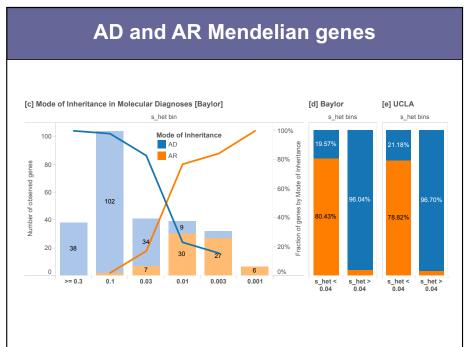
The estimated distribution over selection coefficients can be now used as a prior, and per gene estimates from posteriors

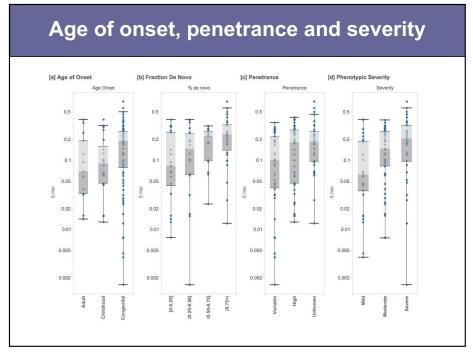
$$P(s_{\text{het},i}|n_i;\nu_i) = \frac{P(n_i|s_{\text{het},i};\nu_i)P(s_{\text{het},i};\widehat{\alpha}_t,\widehat{\beta}_t)}{\int P(n_i|s;\nu_i)P(s;\widehat{\alpha}_t,\widehat{\beta}_t) \,ds}$$

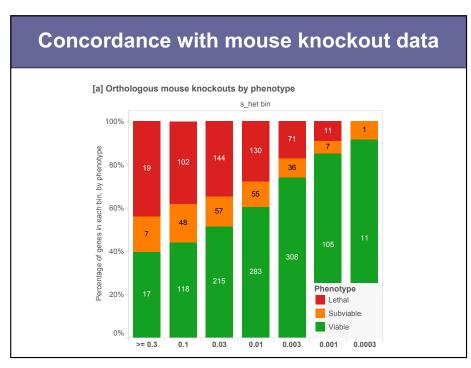


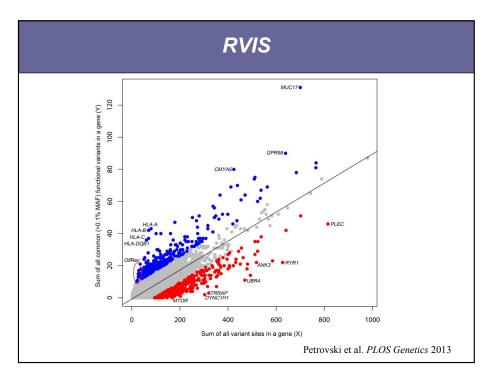
### What happens if we incorporate drift?

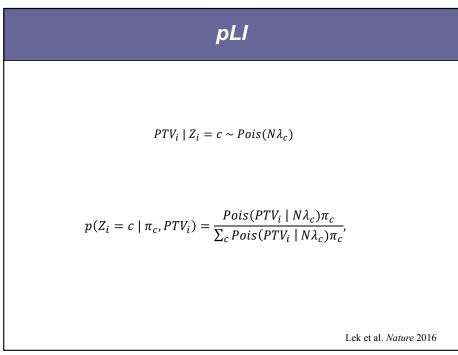
- 1) The approach fails if selection is weak
- 2) The approach fails if mutational target is small
- 3) These considerations are important for regional constraint scores
- 4) Overall, the approach is non-informative in case of recessivity

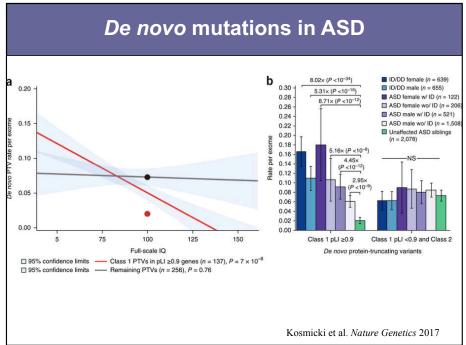


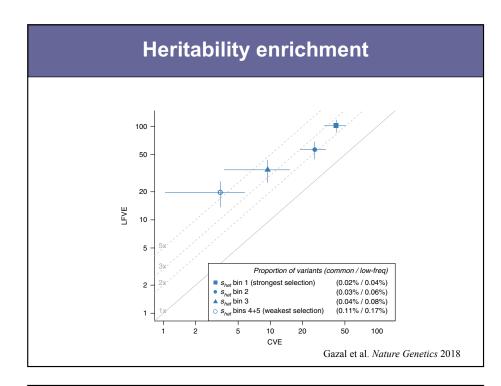




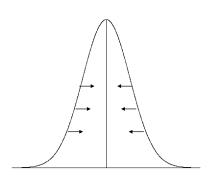








# Stabilizing selection is the most common type of selection on a quantitative trait



selection
Selection may be related or unrelated to the trait

Stabilizing

# Technically, non-neutral genetic variation should not exist!

Forces to maintain variation:

Selection

Mutation

### Why does a common genetic disease exist?

From evolutionary perspective common genetic disease should not exist: natural selection should remove disease-causing alleles from the population

**Theory 1:** 

MEDICALLY detrimental polymorphisms are not EVOLUTIONARY deleterious

- Disease late onset (after the reproductive age)
- Changed environment and lifestyle (Selection direction reversal)
- Compensatory positive effect

**Balancing selection** 

Frequency dependent selection

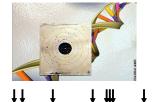
Antagonistic pleiotropy (Trade Off)

**Examples:**  $APO\overline{E}$  (Alzheimer's disease), AGT (Hypertension), CYP3A (Hypertension)

### Mutation/selection balance

### **Theory 2:**

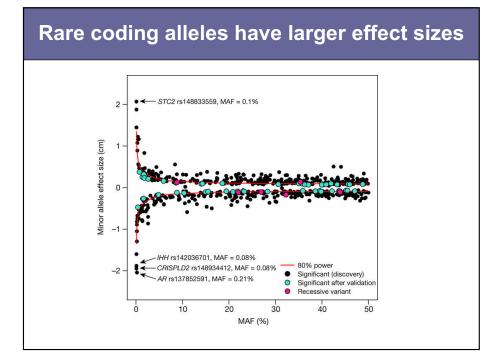
Common diseases are due to multiple deleterious alleles in mutation-selection balance



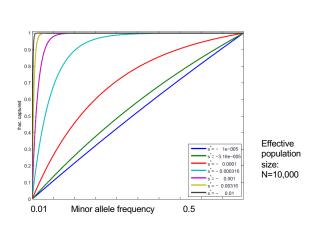
- Weak selection
- High mutation rate

### **CURRENT ESTIMATE:**

- ~70 new mutations per genome
- ~1 new coding mutation per genome

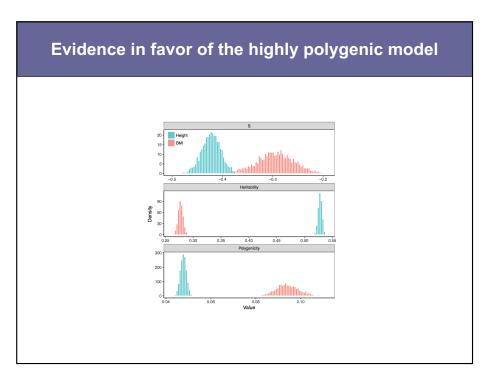


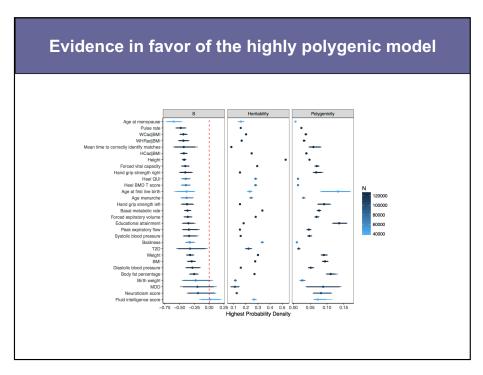
# Heritability by allele frequency

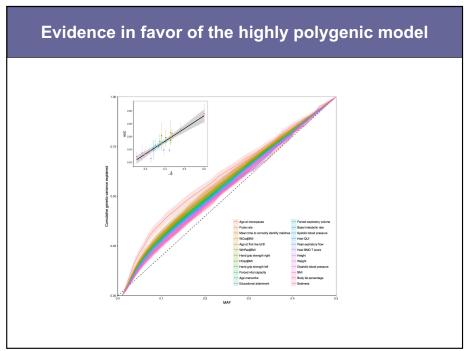


### Evidence in favor of the highly polygenic model

$$\beta_j \sim N\left(0, \left[2p_j(1-p_j)\right]^S \sigma_\beta^2\right) \pi + \phi(1-\pi)$$







# **Evolution, maintenance and allelic architecture of complex traits**

Shamil Sunyaev



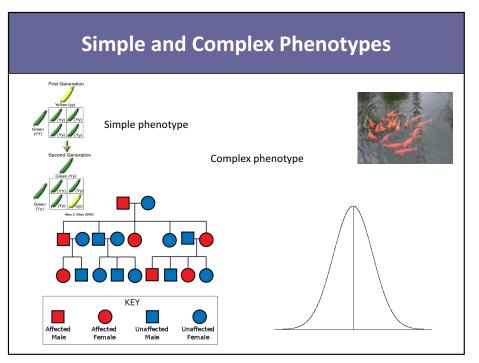


Broad Institute of M.I.T. and Harvard

# GENOTYPE GENOTYPE Functional Biology

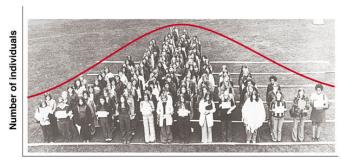
### The role of statistics

- Genetics for statistics is what physics is for mathematics
- Genetics is a leading motivation for development of new basic statistics
- Statistics is the main formal instrument (although not the only one)



### Complex traits are heritable but not in Mendelian fashion

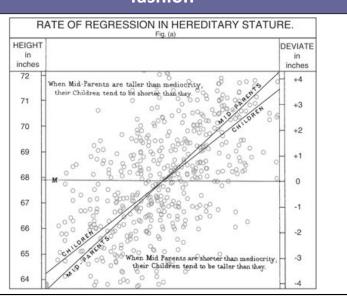
Tobin/Dusheck, Asking About Life, 2/e



Height in inches

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### Complex traits are heritable but not in Mendelian fashion



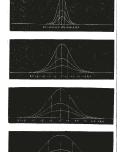
### Infinitesimal model

NATURE

[April 5, 1877

lies with r towards ne hinder ; are fully cs on the TYPICAL LAWS OF HEREDITY1

WE are far too apt to regard common events as matters of course, and to accept many things as obvious truths which are not obvious truths at all, but present problems of much interest. The problem to extremi- which I am about to direct attention is one of these.

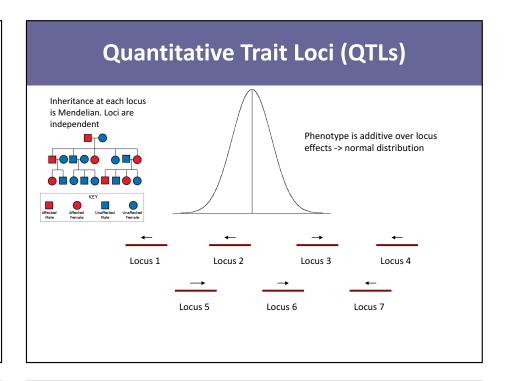


distribution in pedigrees The pedigree defines the covariance matrix

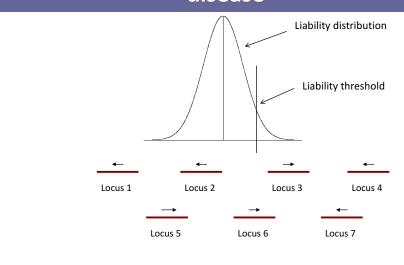
Infinitesimal model: multivariate normal

XV.—The Correlation between Relatives on the Supposition of Mendelian Inheritance. By R. A. Fisher, B.A. Communicated by Professor J. ARTHUR THOMSON. (With Four Figures in Text.)

(MS. received June 15, 1918. Read July 8, 1918. Issued separately October 1, 1918.)



# Dichotomous complex traits such as disease

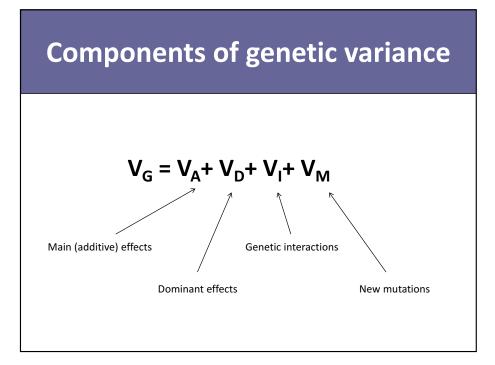


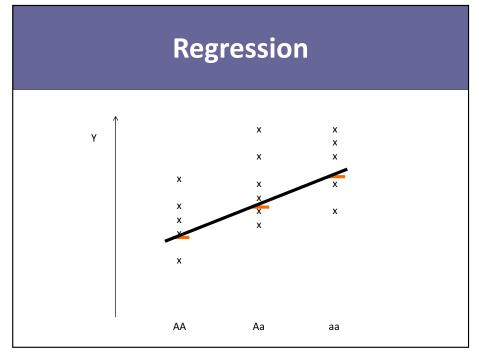
# Population variation is fully described by variance

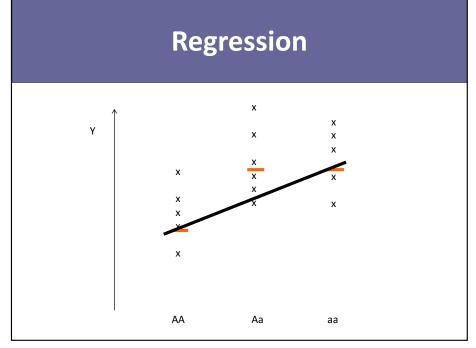
$$V = V_G + V_E$$

Genetic contribution Everything else

# 







### **Additive variance**

Additive variance V<sub>A</sub> is variance explained by the model

$$Y_j = \sum_i \beta_i X_{ij} + \varepsilon$$

$$V_A = 2\sum_i \beta_i^2 x_i (1 - x_i)$$

# Variance components due to dominance and epistasis

Dominance variance V<sub>D</sub> is variance explained by the residuals of the model additive over loci

Epistatic variance  $V_1$  is genetic variance that is not captured by the model additive over loci (presumably due to interactions)

Additive by additive pairwise epistasis

$$Y_j = \sum_{i} \beta_i X_{ij} + \sum_{lk} \beta_{lk} X_{lj} X_{kj} + \varepsilon$$

### Other variance components

Epistasis can be additive by dominant and dominant by dominant

Epistasis can be due to higher order interactions

Mutational variance V<sub>M</sub> – additional variance due to *de novo* mutations

### Heritability

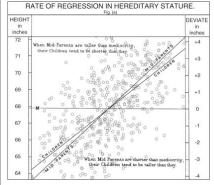
Broad sense

$$H^2 = \frac{V_G}{V}$$

Narrow sense

$$h^2 = \frac{V_A}{V}$$

### **Estimating heritability**

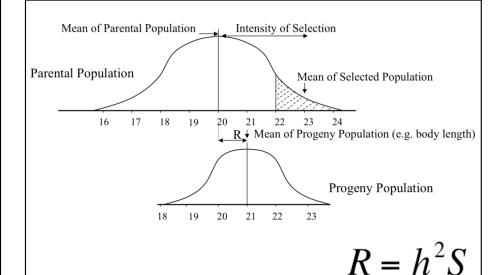


$$Cov(MP, O) = \frac{1}{2}V_A + \frac{1}{4}V_I$$

Narrow sense heritability

$$h^2 = \frac{V_A}{V} \approx \frac{Cov(MP, O)}{V(MP)}$$

### **Breeder's equation**



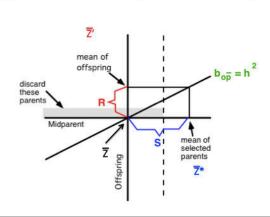
### **Breeder's equation**

Response to Selection = heritability \* Selection Differential

R

$$= h^2$$





### With genotypic information in hand

Regress phenotype on genotype

$$Y_j = \sum_i \beta_i X_{ij} + \epsilon$$

$$Y_{j} = \sum_{i} \beta_{i} X_{ij} + \varepsilon \qquad V_{A} = 2 \sum_{i} \beta_{i}^{2} x_{i} (1 - x_{i})$$

Narrow sense heritability

$$h^2 = \frac{V_A}{V}$$

### In the Ideal World

Regress phenotype on genotype

$$Y_j = \sum_i \beta_i X_{ij} + \varepsilon$$

Identify significant and reproducible associations. Estimate effect sizes. Estimate additive variance.

$$\hat{V}_A = 2\sum_{i}^{known} \hat{\beta}_i^2 x_i (1 - x_i)$$

Reality: missing heritability

$$\hat{h}^{2} = \frac{\hat{V}_{A}}{V} << \frac{Cov(MP, O)}{V(MP)}$$

# Current GWAS explain a minor fraction of heritability



The case of the missing heritability

Height – 10%, Blood lipids – 12%

### Likely reasons for missing heritability

- 1. Common variants of weak effect
- 2. Rare variants of larger effect
  - 3. Epistatic interactions

$$Cov(MP, O) = \frac{1}{2}V + \frac{1}{4}V_{I}$$

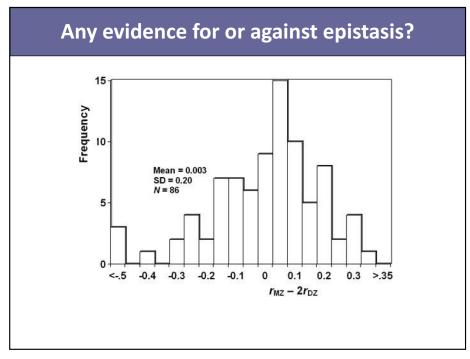
### Questions about allelic architecture

- How many loci are involved?
- Is variation underlying the trait rare or common?
- What is the distribution of effect sizes of variants involved in the trait?
- What is the role of epistasis and dominance?

### GxG interactions

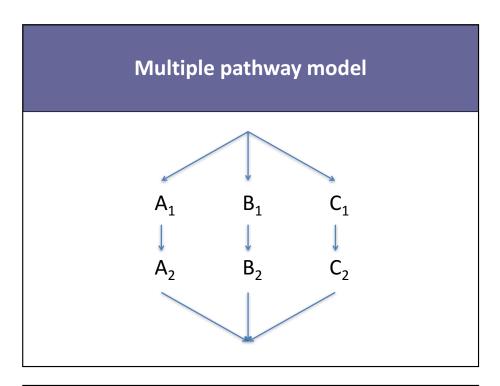
# Why is epistasic variance commonly disregarded?

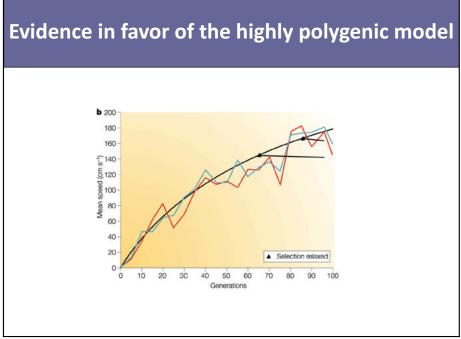
- In human genetics, epistatic interactions between common variants have not been observed.
- In a model with two (or several) loci, contribution of epistatic variance is relatively small.
- Long term response to selection in model organisms seems to contradict the importance of epistasis.

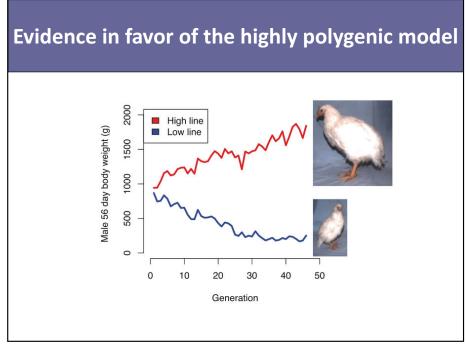


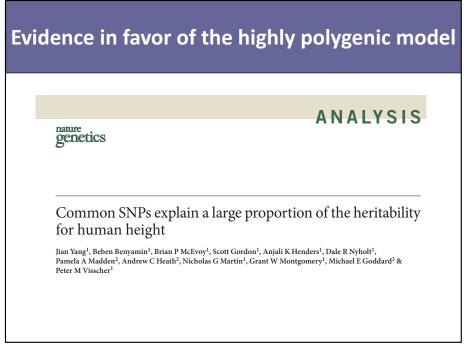
# Why is epistasic variance might be of importance?

- A non-linear model involving many loci would generate a large epistatic variance.
- Interactions would be statistically undetectable.
- The model would not generate significant deviations from the observations.
- As an example, we may consider a model with multiple pathways involved.









AA

Aa

aa

Genotypes

0

1

\_

Normalized genotypes

 $\frac{0 - E(X)}{\sqrt{Var(X)}}$ 

 $\frac{1 - E(X)}{\sqrt{Var(X)}}$ 

 $\frac{2 - E(X)}{\sqrt{Var(X)}}$ 

Normalized genotypes

 $\frac{-2q}{\sqrt{2pa}}$ 

 $\frac{p-q}{\sqrt{2na}}$ 

 $\frac{2p}{\sqrt{2n}}$ 

If SNP1 is causal and SNP2 is not, the apparent association of SNP2 is:

$$\hat{\boldsymbol{\beta}}_2 = \boldsymbol{\beta}_1 \cdot \boldsymbol{r}_{12}$$

In non-normalized genotypes

$$\hat{\beta}_2 = \beta_1 \cdot r_{12} \cdot \sqrt{\frac{Var(X_1)}{Var(X_2)}}$$

 $X_{ij}$  – Normalized genotype of individual i at SNP j

In the matrix form:

$$\overline{y} = X\overline{\beta} + \varepsilon$$

Two important matrices:

$$LD = \frac{1}{M}X^T X$$

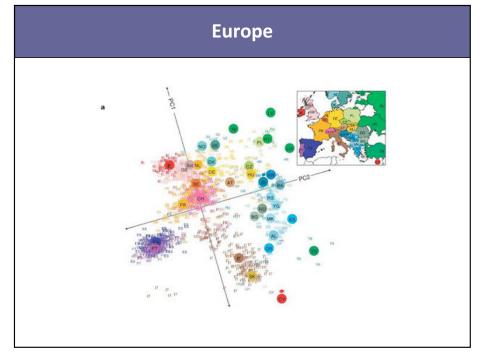
$$GRM = \frac{1}{N}XX^{T}$$

### Principle component analysis (PCA)

$$GRM = \frac{1}{N}XX^{T}$$

Principle component are eigenvectors

First principle component corresponds to the largest eigenvalue



### **Linear Mixed Models (LMM)**

- We can model effects of individual variants as random effects distributed as  $N(0, \sigma^2)$ .
- Random effect model is a model with error terms drawn from a multivariate normal distribution.
- In the infinitesimal model, co-variance matrix can be approximated using IBS (not IBD).

### **Linear Mixed Model (LMM)**

Our model

$$Y_i = \sum_j \beta_j X_{ij} + \varepsilon$$

We have to fit markers individually

$$Y_i = \beta_1 X_1 + \sum_{j=2} \beta_j X_{ij} + \varepsilon \sim \beta_1 X_1 + \varepsilon'$$

For each SNP we can fit the model

$$Y_i = \beta X_i + u_i + \varepsilon$$

$$\varepsilon \sim N(0, I\sigma^2)$$
  $u \sim MVN(0, GRM)$ 

### Remember from the Galton plot

Parent and offspring share 50% of DNA (IBD)

$$Cov(P,O) = \frac{1}{2}V_A$$

More generally, if fraction of the genome IBD is r

$$Cov(A,B) = \frac{1}{r}V_A$$

### If we assume that genetic effects are random

We assume that all SNPs have effects on the trait drawn from a normal distribution

$$Y_i = \mu_i + \mu_i + \varepsilon$$

$$Cov(u_i, u_k) = \frac{1}{N}\sigma^2 \sum_j X_{ij} X_{ik}$$

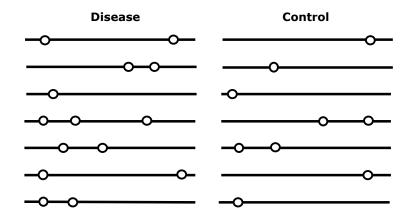
$$u \sim MVN(0,\sigma^2GRM)$$

### Challenges of the polygenic model

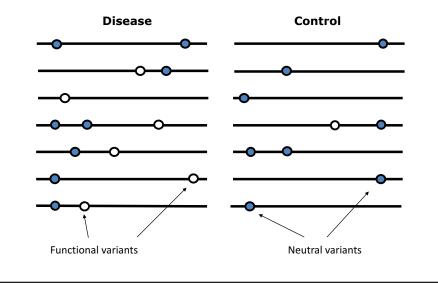
- 1) Need for a very large target size
- Natural selection is expected to rapidly eliminate variants and reduce allele frequency of remaining variants
- 3) Variants must be either very rare or of very small effect sizes

Rare variants

### This is a direct association!



## This is a direct association!



Hyperlipidemia in Coronary Heart Disease

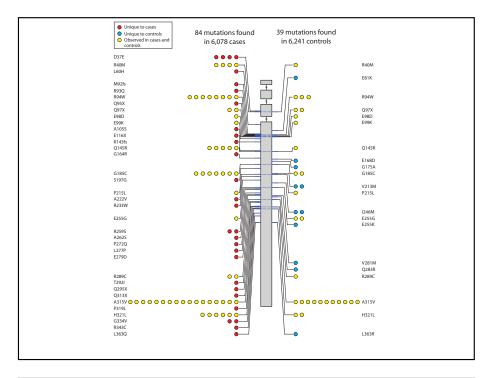
II. GENETIC ANALYSIS OF LIPID LEVELS IN 176 FAMILIES AND DELINEATION OF A NEW INHERITED DISORDER, COMBINED HYPERLIPIDEMIA

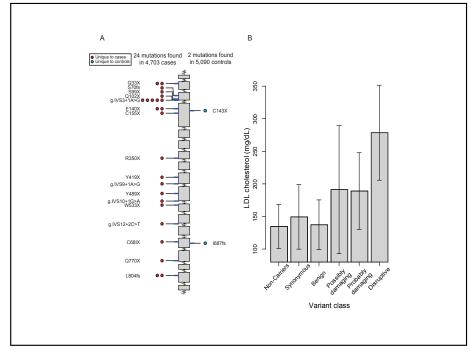
JOSEPH L. GOLDSTEIN, HELMUT G. SCHROTT, WILLIAM R. HAZZARD, EDWIN L. BIERMAN, and ARNO G. MOTULSKY with the technical assistance of Ellen D. Campbell and Mary Jo Levinski

From the Departments of Medicine (Division of Medical Genetics, University Hospital, and Division of Metabolism and Gerontology, Veterans Administration Hospital) and Genetics, University of Washington, Seattle, Washington 98195

TABLE XII
Frequency of Hyperlipidemia

Disorder	Survivors of myocardial infarction			
	< Age 60 (a)	≥ Age 60 (b)	Ratio a/b	General population*
	%	%		%
Monogenic hyperlipidemia				
Familial hypercholesterolemia	4.1	0.7	5.9	~0.1-0.2
Familial hypertriglyceridemia	5.2	2.7	1.9	~0.2-0.3
Combined hyperlipidemia	11.3	4.1	2.8	~0.3-0.5
Total	20.6	7.5		~0.6-1.0
Polygenic				
Hypercholesterolemia	5.5	5.5	1.0	_
Sporadic				
Hypertriglyceridemia	5.8	6.9	0.8	
				Goldstein et





Hyperlipidemia in Coronary Heart Disease

II. GENETIC ANALYSIS OF LIPID LEVELS IN 176 FAMILIES
AND DELINEATION OF A NEW INHERITED DISORDER,
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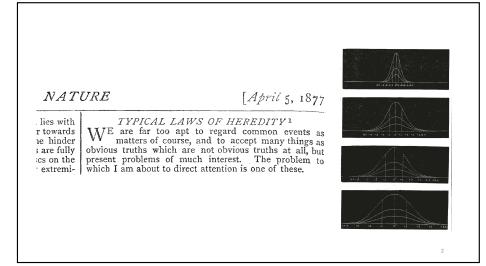
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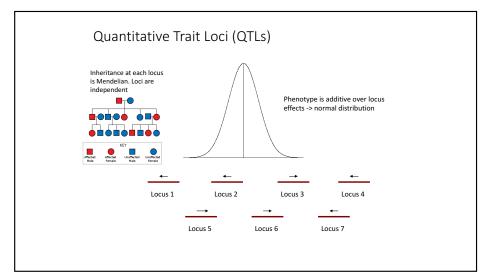
### Non-Parametric Polygenic Risk Prediction

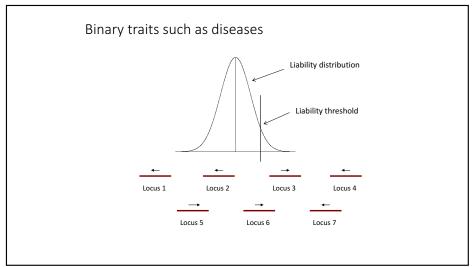
### Shamil Sunyaev

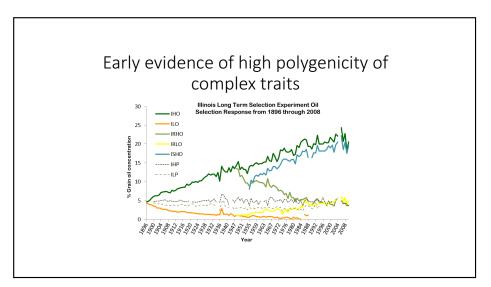


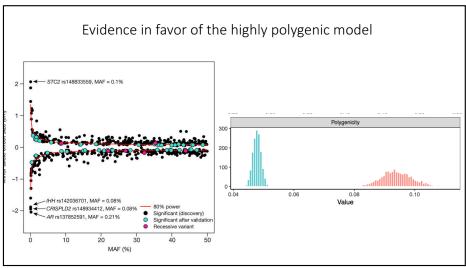






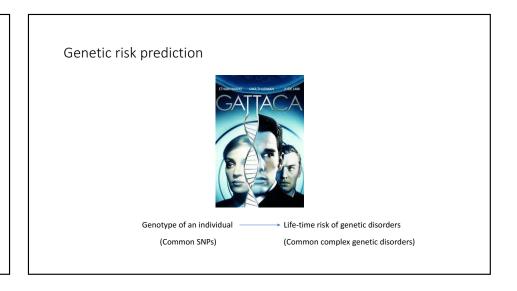






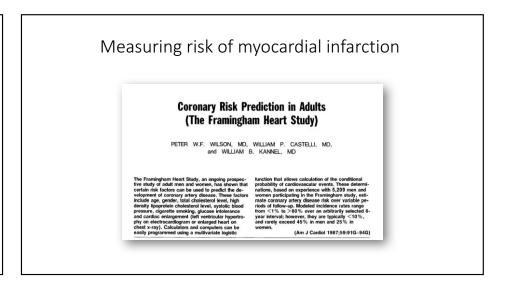
# Effect sizes of individual variants are very small

- Genotype at a single locus carries very little information about phenotype.
- It does not mean that one cannot predict phenotype from genotype.
- Accuracy  $(r^2)$  of an ideal genetic predictor equals heritability.

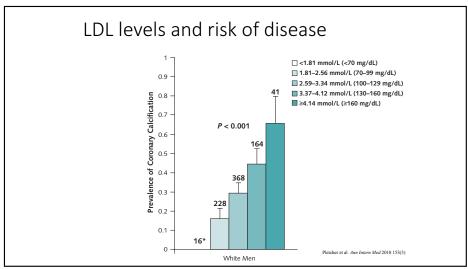


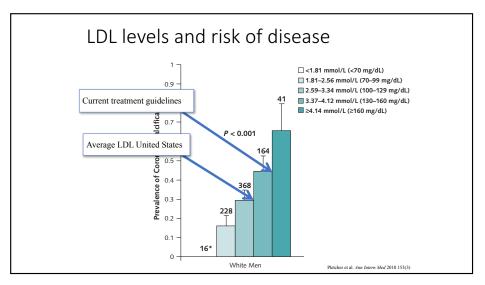
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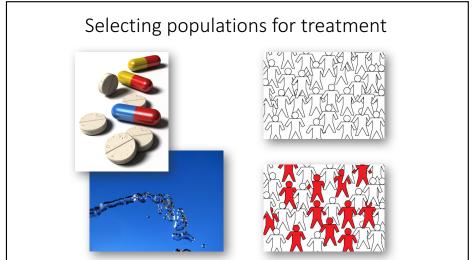
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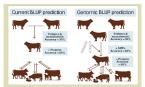
### Why estimate genetic risk?

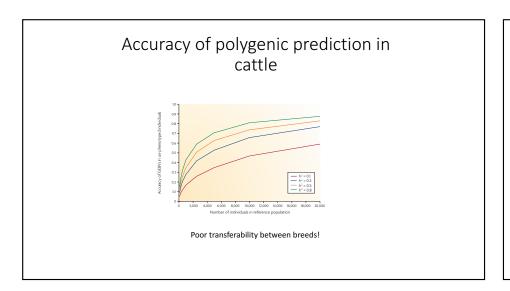
- An estimate of the long-term risk at birth
- Genetic risk can be combined together with biomarkers and clinical features
- Genetics explains about 50% of risk. One cannot predict risk any better than that but 50% is a non-trivial proportion of risk

## BLUP – Best Linear Unbiased Predictor



- Infinitesimal model
- Genetic effects are random
- Predict the expected genetic effect





### Applications in humans



Prediction of individual genetic risk to disease from genome-wide

Naomi R. Wray, Michael E. Goddard and Peter M. Visscher

Genome Res. 2007 17: 1520-1528; originally published online Sep 4, 2007 Access the most recent version at doi:10.1101/gr.6665407

LETTERS

Common polygenic variation contributes to risk of schizophrenia and bipolar disorder

- LD-prune
- Exclude SNPs of very small effect

# Extensions of BLUP – multiple variance scales and binary phenotypes

MultiBLUP: Speed and Balding. Genome Research 2014

Bayesian analysis: MacLeod et al. Genetics 2014

BSLMM: Zhou et al. PLOS Genetics 2013

GeRSI: Golan and Rossett. AJHG 2014

Methods that work with summary statistics

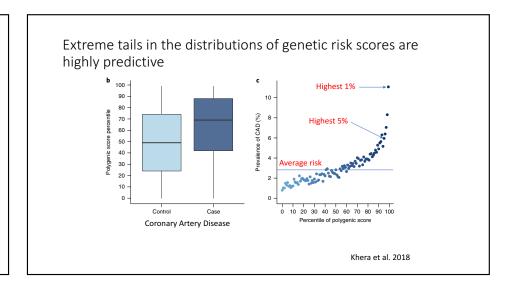
- Summary statistics are easily available
- Most methods require a separate small individual level dataset to tune parameters

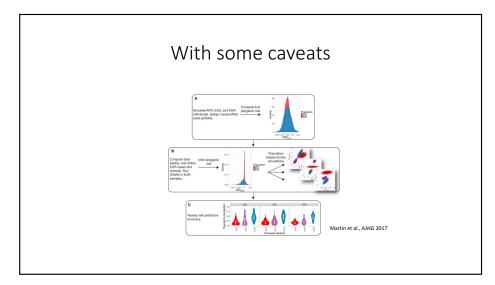
20

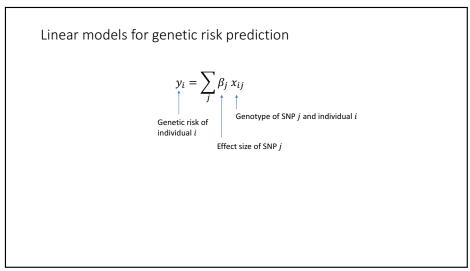
# LDPred – a Bayesian method using summary statistics

$$\beta_i \sim_{iid} \left\{ \begin{array}{ll} N\bigg(0, \frac{h_g^2}{Mp}\bigg) \text{with probability } p \\ \\ 0 \text{ with probability } (1-p), \end{array} \right.$$

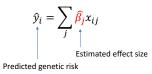
Also, check BayesR





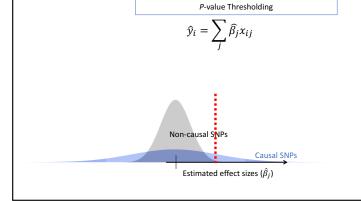


"Polygenic scores" can leverage summary statistics from a large GWAS study

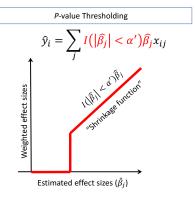


"Polygenic scores" can leverage summary statistics from a large GWAS study  $\hat{y}_i = \sum_j \hat{\beta}_j x_{ij}$ Estimated effect size Predicted genetic risk  $\frac{\text{Sampling error}}{\text{Non-causal SNPs}}$ Estimated effect sizes  $(\hat{\beta}_i)$ 

"Polygenic scores" can leverage summary statistics from a large GWAS study

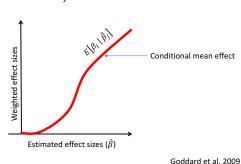


*P*-value thresholding can be reformulated as "shrinking" estimated effect sizes



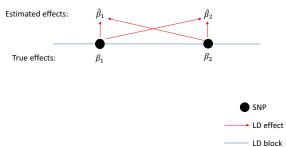
The optimal polygenic score can be constructed with "conditional mean effects"

$$\hat{y}_i = \sum_j E[\beta_j \mid \hat{\beta}_j] x_{ij}$$



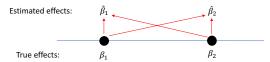
Accounting for LD in summary data is a major challenge

• Correlation between apparent true genetic effects

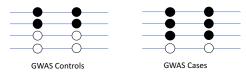


Accounting for LD in summary data is a major challenge

• Correlation between apparent true genetic effects



• Correlation between sampling errors



Our approach ("Non-Parametric Shrinkage" or NPS)

- No explicit specification of genetic architecture prior, thus "non-parametric"
- Learn conditional mean effects directly from training data
- Fully account for correlation in summary statistics

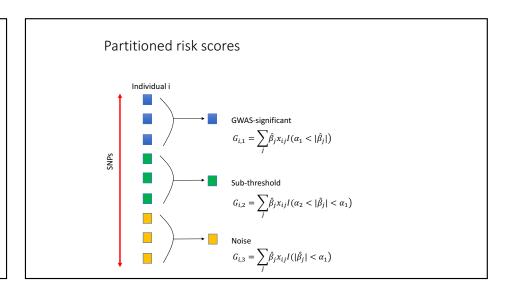
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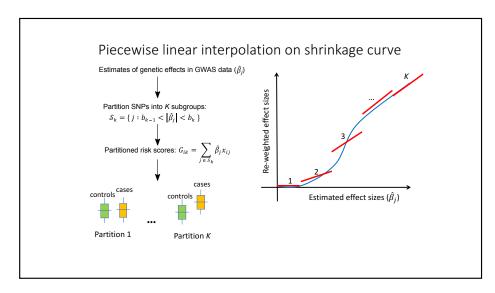
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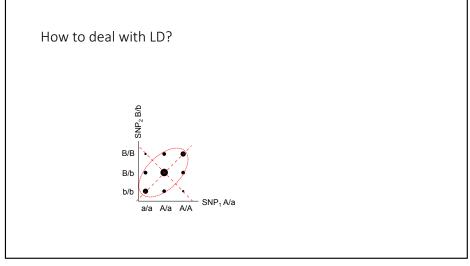
• Learn conditional mean effects directly from training data

1. How to estimate  $E[\beta_j \mid \hat{\beta}_j]$  without a Bayesian prior on  $\beta$ • Fully account for correlation in summary statistics

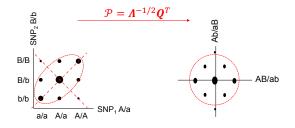
2. How to deal with LD



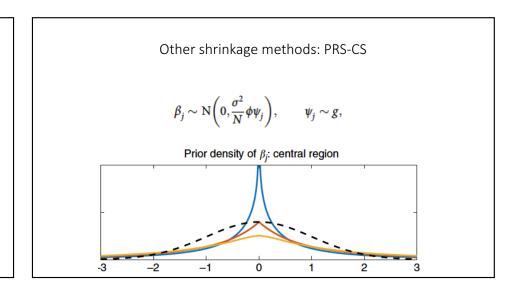




### Decorrelating linear projection ${\mathcal P}$

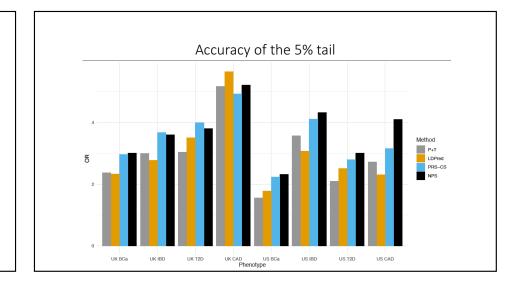


 $\Sigma$  is a local LD matrix and  $\Sigma=Q~\Lambda~Q^T$  by eigenvalue decomposition  $\Sigma^{-1}=Q~\Lambda^{-1}~Q^T=(Q~\Lambda^{-1/2})(\Lambda^{-1/2}Q^T)$ 



Other shrinkage methods: PRS-CS

Lassosum – extension of LASSO



### Summary on the method

- NPS accounts for the correlation of sampling errors in GWAS summary statistics.
- NPS provides an extensible framework to estimate the shrinkage curve from training data.
- NPS is best-suited to take advantage of the high density of markers and imputation accuracy in latest GWAS datasets.

The preprint is available in BioRxiv:
Chun et al. "Non-parametric polygenic risk
prediction using partitioned GWAS summary statistics."
Software is available at: https://github.com/sgchun/nps

Is an extreme presentation with a family history Mendelian?

- It is often assumed that an extreme phenotypic presentation is due to a large effect Mendelian mutation.
- Apparently Mendelian family history is assumed to support a highly penetrant Mendelian mutation.
- Could these cases be polygenic (or, at least, not monogenic)?

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# Annotating gene sequence variation

Shamil Sunyaev

Department of Biomedical Informatics
Harvard Medical School



Broad Institute of M.I.T. and Harvard

# Identifying functionally significant causal variants in Segregation data Frequency in Controls Interpretation Bioinformatics

### Map variants on genomic annotation

Watch for multiple transcripts!

Watch for conflicting annotations!

### Nonsense variants

One of most significant types of variants usually leading to the complete loss of function.

Nonsense variants are enriched in sequencing artifacts

Important considerations: i) location along the gene, ii) does the variant cause NMD? iii) is the variant in a commonly skipped exon?

**Tool: LOFTEE** 

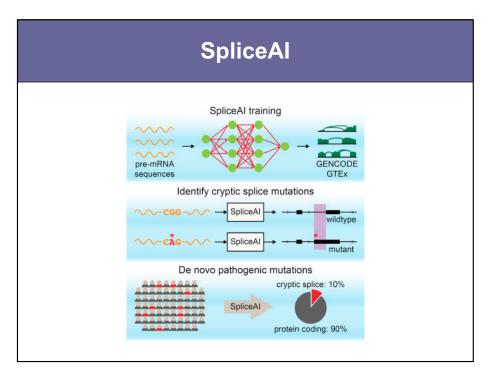
### Variants involved in splicing

Variants in canonic splicing sites

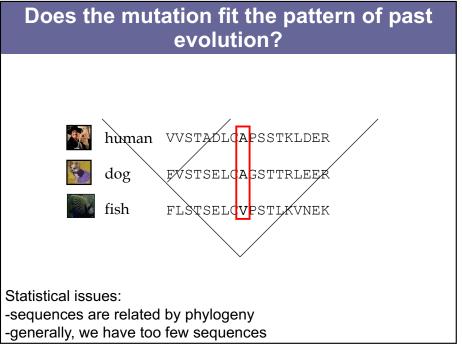
Variants in exonic or intronic splicing enhancers

Gain of splicing variants

**PREDICTION** 



# Missense variants: computational predictions His66Arg P23946: Chymase precursor ...IVTSNCPSKPCGCFLIRNFVLTAA H CAGRSITVTLGAHNITEEEDTWQKL... Sequence alignment LASCGGFLIRNFVLTAA H CAGRFIMVTLGAHNIQKK. LASCGGFLIRNFVLTAA H CAGRFIMVTLGAHNIQKK. LASCGGFLIRNFVLTAA H CAGRFIMVTLGAHNIQKK. LASCGGFLIRNFVLTAA H CAGRFIMVTLGAHNIQKK. QVACGGFLIRNFVLTAA H CAGRFIMVTLGAHNIQKK. Feature annotation Key Begin End Description ACT SITE 100 110 Charge relay system. ACT SITE 203 203 Charge relay system.



# Does the mutation fit the pattern of past evolution?

- We assume a constant fitness landscape: what is good for fish is good for human!
- We can estimate whether the mutation fits the pattern of amino acid changes.
- We can also estimate rate of evolution at the amino acid site

### **Continuous time Markov model**

 $GLY \longrightarrow VAL \longrightarrow ALA \longrightarrow GLY \longrightarrow ALA$ 

### **Continuous time Markov model**

P - matrix of transition probabilities

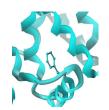
$$P(t) = e^{Qt}$$

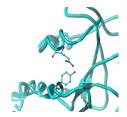
 $\pi$  – stationary distribution

$$Q\bar{\pi}=0$$

### **Protein structure view**





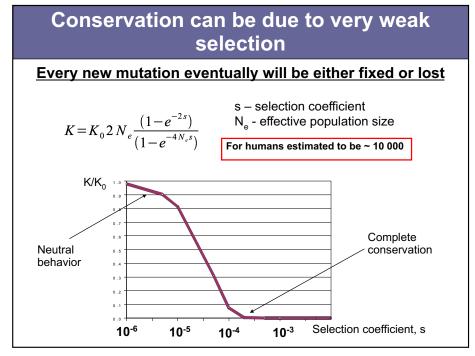


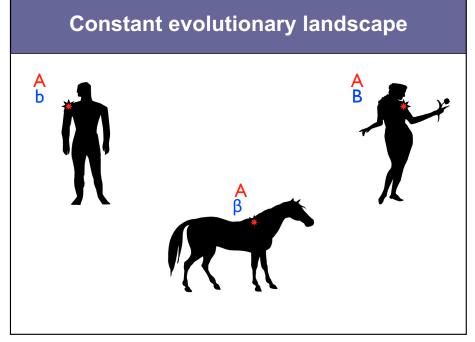
- Most of pathogenic mutations are important for stability (good news?).
- $\Delta\Delta G$  is difficult to estimate.
- Unfolded protein response pathway has to be taken into account.
- · Heuristic structural parameters help but less than comparative genomics.

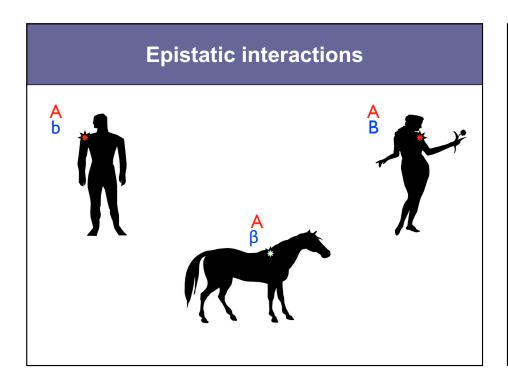
### PolyPhen2 Prediction Analysis Interpretation Sequence MSA creation profile based scores homology search MSA Alignment full-length alignment identity based scores protein domain CpG transition ROC confidence nonsynonymous SNP Probabilistic Classifier Structure 3D visualization essible surface area Annotation www.genetics.bwh.harvard.edu/pph2 Adzhubei, et al. Nature Methods 2010

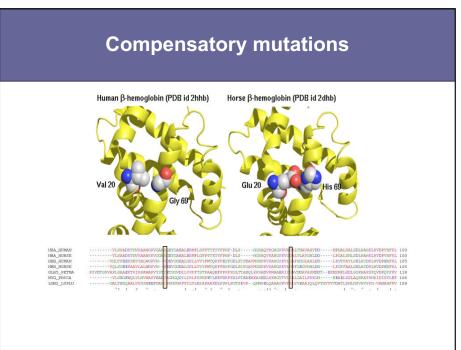
### Weakly deleterious mutations

- Multiple independent lines of evidence suggest abundance of weakly deleterious alleles in humans
- Weakly deleterious variants may occur in highly conserved positions
- Weakly deleterious alleles probably contribute to complex phenotypes but not to simple Mendelian phenotypes



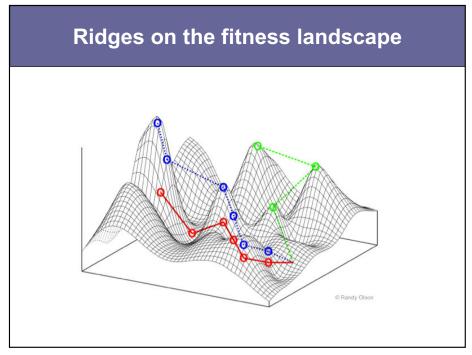




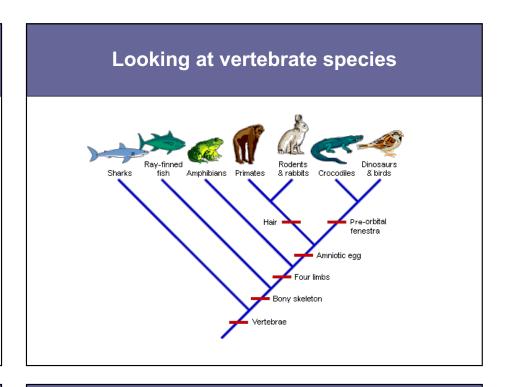


# The phenomenon of compensatory mutations in different fields

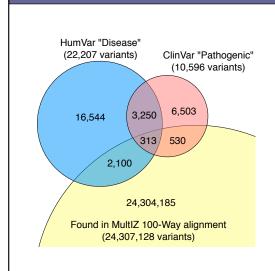
- Biochemistry protein stability, allosteric effects
- Genetics incomplete penetrance
- Evolutionary biology speciation, epistatic models of evolution



## 



## Many human disease mutations are found in vertebrates



5.5-6.5% of presumably pathogenic human mutations are detected in mammals

### How complex genetic suppression can be?

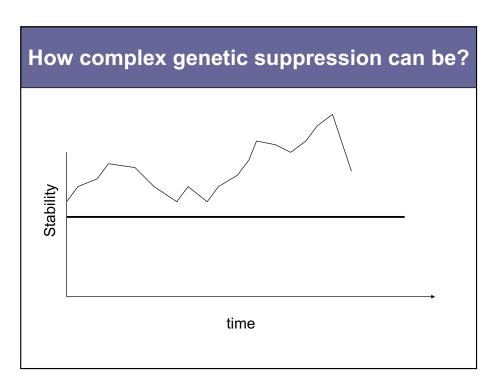
### LETTER

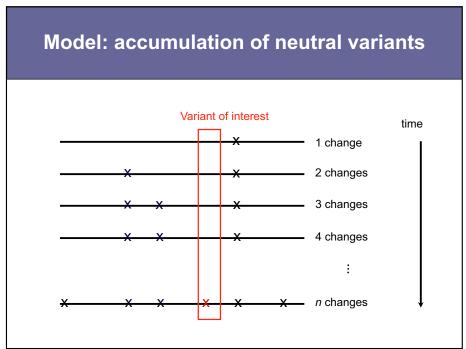
doi:10.1038/nature12678

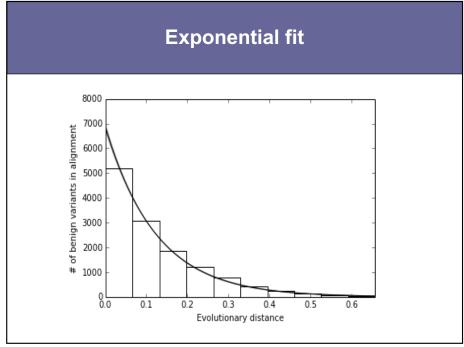
### Genetic incompatibilities are widespread within species

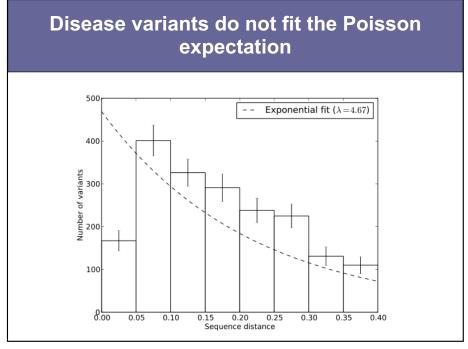
 $Russell\ B.\ Corbett-Detig^1, Jun\ Zhou^1,\ Andrew\ G.\ Clark^{2,3},\ Daniel\ L.\ Hartl^1\ \&\ Julien\ F.\ Ayroles^{1,2,4}$ 

Numerous Dobzhansky-Muller incompatibilities in fly population



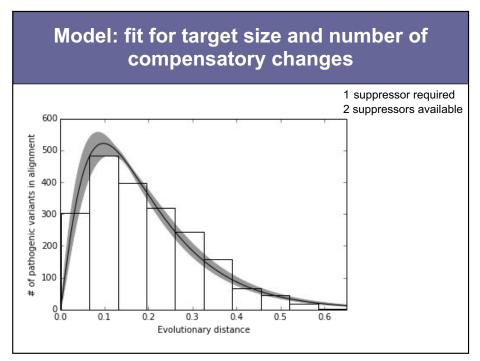


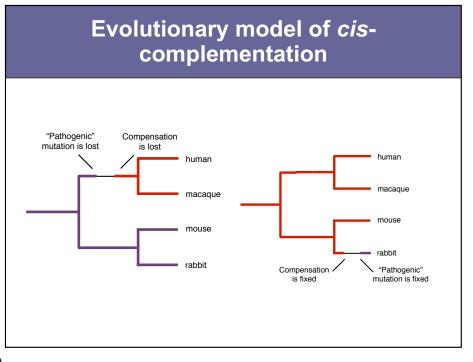




# Suppressors target size m Disease variant 1 change 2 changes 3 changes 4 changes i. k out of m required for suppression

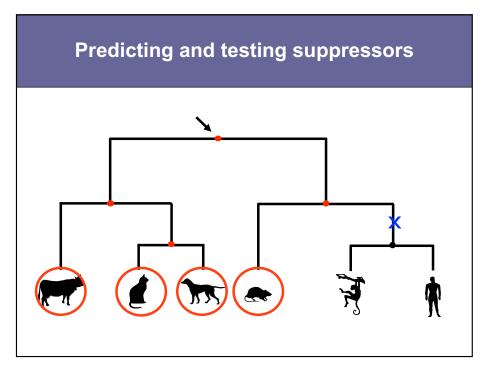
## Model: Erlang distribution $L(k,t,\lambda) = \frac{\lambda^k t^{k-1} e^{-\lambda t}}{(k-1)!}$



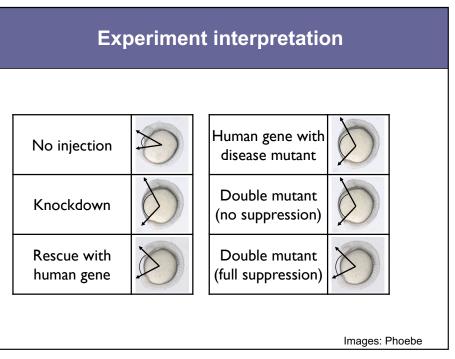


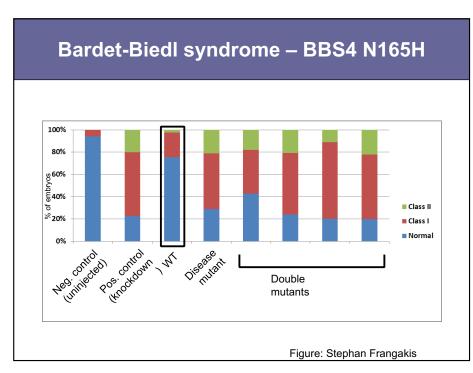
### **Model Summary**

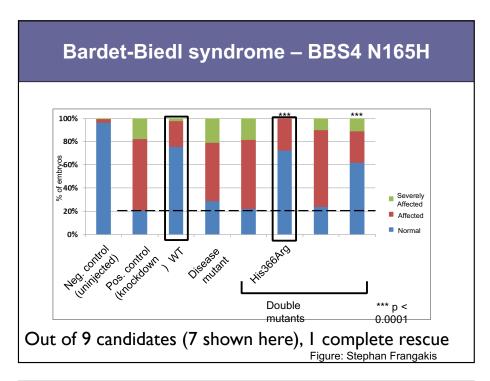
- ~5-6% of human disease mutations have potential suppressors (i.e. are present in another mammalian species)
- In most cases, one large-effect suppressor is sufficient, out of only 1-2 available
- These values allow simple experiment to identify suppressors

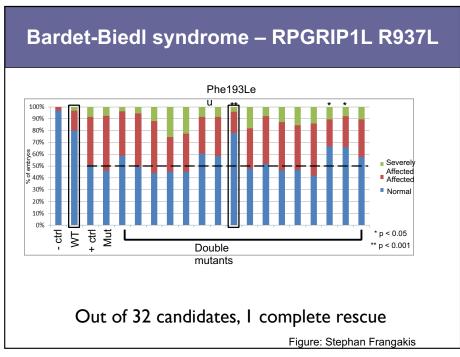


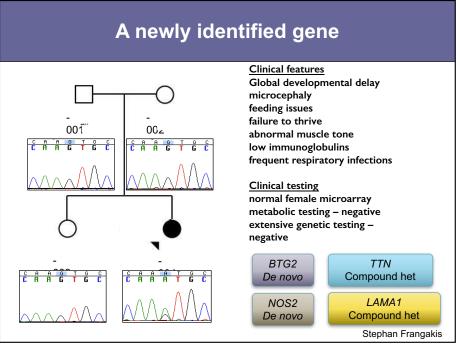
## Model of Bardet-Biedl Syndrome (obesity, renal failure, vision loss) Caused by defects in primary cilium Embryonic convergence / extension phenotype in zebrafish Easily scorable phenotype Class I Class II Images: Phoebe

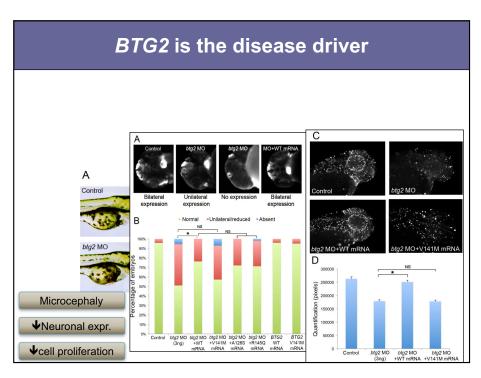


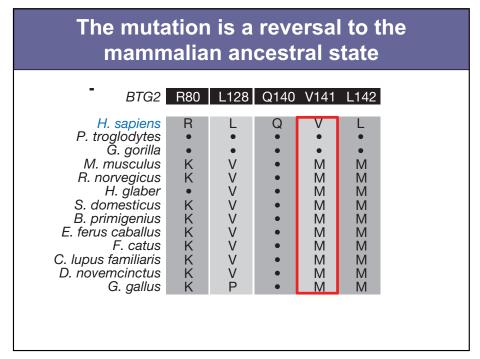


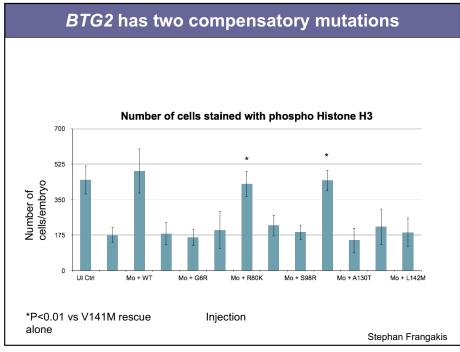


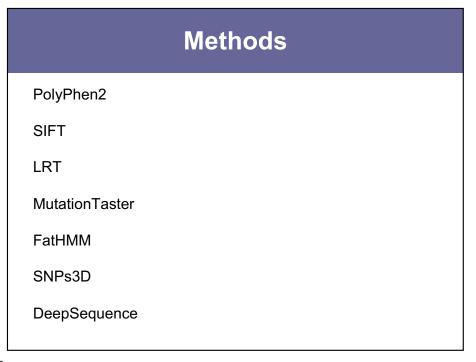












### **Umbrella** methods

Condel

REVEL

**CADD** 

M-CAP

### **Incorporating regional constraint**

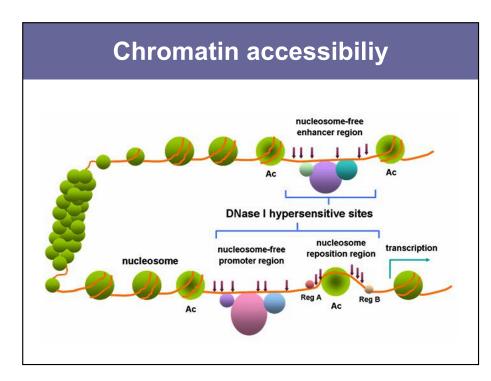
**CCR** 

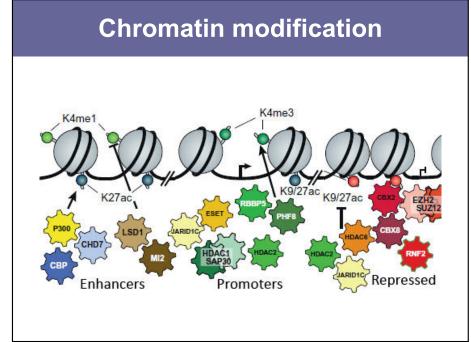
M-CAP

**PrimateAl** 

### Non-coding variants

## Regulatory variants • Regulation: variants in promoters, enhancers, silencers, insulators chromatin modifiers chromatin remodelers proximal promoter core promoter





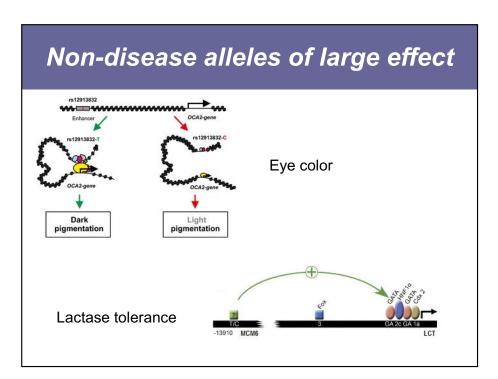
## EPIGENETIC MECHANISMS are afforded by these factors and processors - Development in view, childrood - Development of index childrood - Aging - Duel OHROMOSOME DINA methylation Methyl group in regisement leafor found in some datalesy sourcest can tag DNA and activate or regress genes. Histories are preferre around which DNA can wind for correction and grow regulation. CNA inaccessibility, gene inactive Indicate with the availability of genes in the DNA to be activated.

## Why do we think that non-coding variation is of importance?

Regions and individual nucleotides conserved along phylogeny show signals of purifying selection in humans

Epigenetic studies report many well-localized regulatory marks

GWAS signals are predominantly located in non-coding regions



### **Ultraconserved elements**

OPEN d ACCESS Freely available online

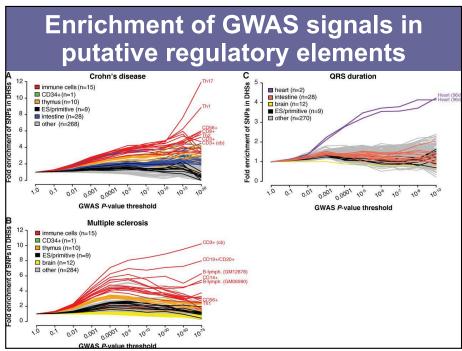
PLOS BIOLOGY

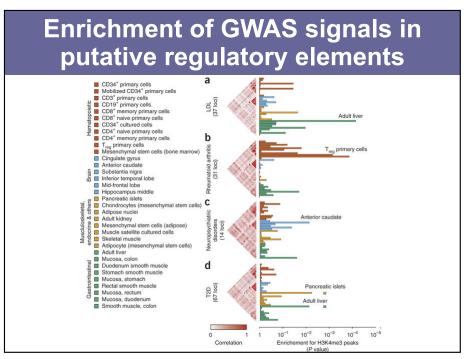
### Deletion of Ultraconserved Elements Yields Viable Mice

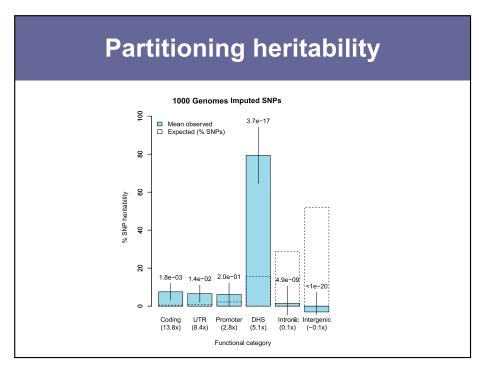
Nadav Ahituv<sup>1,2"</sup>, Yiwen Zhu<sup>1</sup>, Axel Visel<sup>1</sup>, Amy Holt<sup>1</sup>, Veena Afzal<sup>1</sup>, Len A. Pennacchio<sup>1,2</sup>, Edward M. Rubin<sup>1,2"</sup>

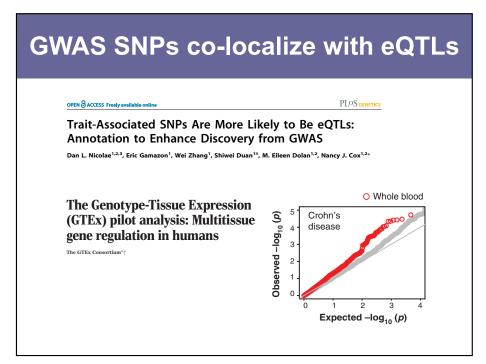
1 Genomics Division, Lawrence Berkeley National Laboratory, Berkeley, California, United States of America, 2 United States Department of Energy Joint Genome Institute
Walnut Creek California, United States of America

Ultraconserved elements have been suggested to retain extended perfect sequence identity between the human, mouse, and rat genomes due to essential functional properties. To investigate the necessities of these elements in vivo, we removed four noncoding ultraconserved elements (ranging in length from 222 to 731 base pairs) from the mouse genome. To maximize the likelihood of observing a phenotype, we chose to delete elements that function as enhancers in a mouse transgenic assay and that are near genes that exhibit marked phenotypes both when completely inactivated in the mouse and when their expression is altered due to other genomic modifications. Remarkably, all four resulting lines of mice lacking these ultraconserved elements were viable and fertile, and failed to reval any critical abnormalities when assayed for a variety of phenotypes including growth, longevity, pathology, and metabolism, addition, more targeted screens, informed by the abnormalities observed in mice in which genes in proximity to the investigated elements had been altered, also failed to reveal notable abnormalities. These results, while not inclusive of all the possible phenotypic impact of the deleted sequences, indicate that extreme sequence constraint does not necessarily reflect crucial functions required for viability.

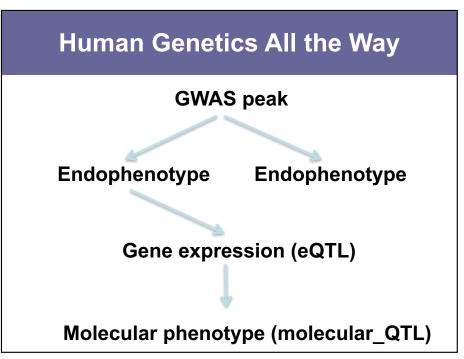




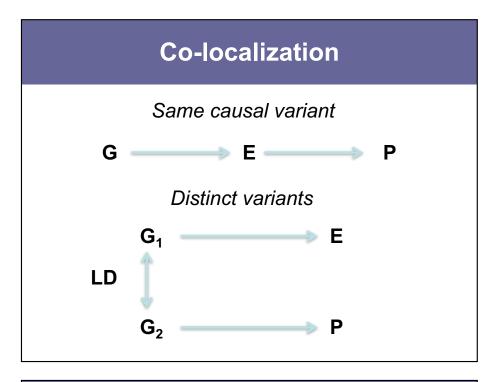




## Translating GWAS findings into mechanistic models GWAS peak Controlled model system Biochemistry



## Causality Mediation G E P Independent effects E G P Reverse causation G P E



### Methods

Coloc

**eCAVIAR** 

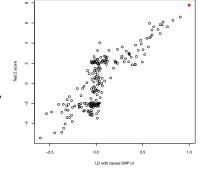
JLIM

### PAINTOR's fine mapping model

 If a SNP is causal, then r<sup>2</sup> should predict association of other SNPs in the area:

$$Z_2 \sim N(r_{12}\lambda_1, 1)$$

 Correlation between test statistics Z are approximated by MVN given local pairwise LD structure.



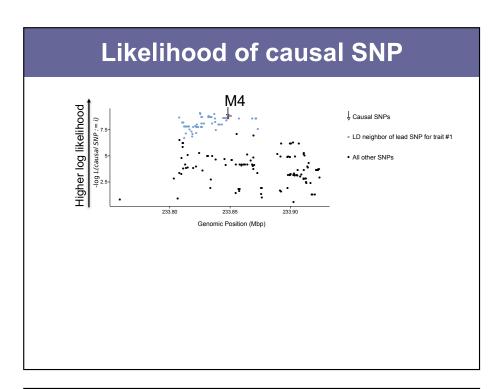
$$L(\mathbf{Z}|C = \{m\}; \lambda_m) = N(\mathbf{Z}; \Sigma(\lambda \circ C), \Sigma)$$

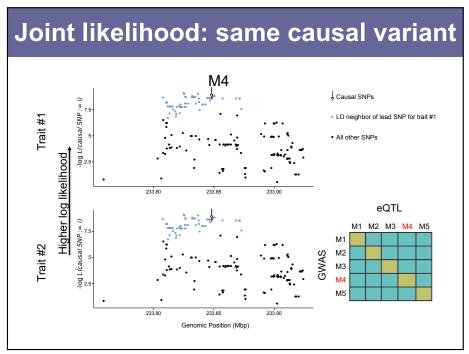
 $\propto e^{-\frac{1}{2}(\mathbf{Z}^T \Sigma^{-1} \mathbf{Z} - z_m^2)}$ 

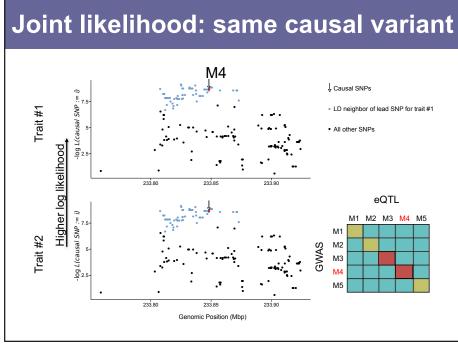
Parameters

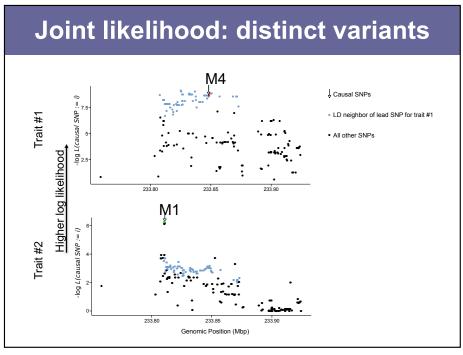
z: standardized effect sizez: association statisticc: indicator of causalitym: SNP considered

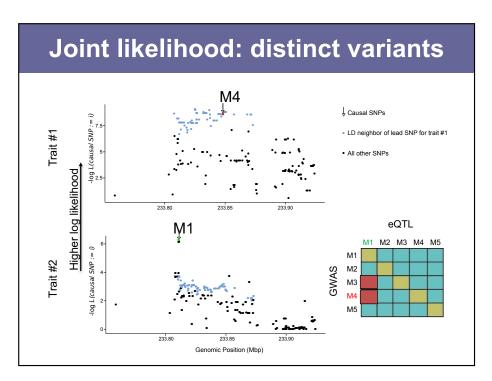
Kichaev et al. PLoS Genet. 2014; Chen et al. Genetics. 2015

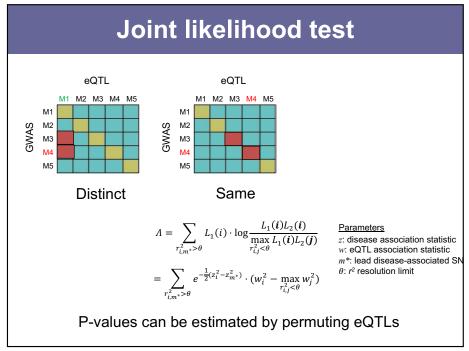


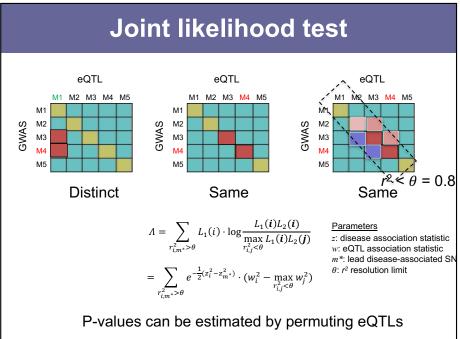












## Real data: autoimmune/inflammatory diseases

- · Highly successful GWAS
- · ImmunoChip: custom fine-mapping array
- Free availability of summary statistics on ImmunoBase
- Accessibility of disease relevant cell types and eQTLs data

	Densely			
Disease	genotyped a			
MS	59			
IBD	69			
Crohn	19			
UC	10			
T1D	47			
RA	34			
CEL	34			
Overall	272			

		Number of loc				
	Densely	eQTL present <sup>b</sup>				
Disease	genotyped <sup>a</sup>	CD4 <sup>+</sup>	CD14 <sup>+</sup>	LCL	Total	
MS	59					
IBD	69					
Crohn	19					
UC	10					
T1D	47					
RA	34					
CEL	34					
Overall	272	<del></del> '				

 $^{\circ\circ\circ}$  CD4/CD14+ (n=211/213) from Raj et al. Science 2014; LCL (n=278) from Lappalainen et al. Nature 2013

		Number of lo				
	Densely	eQTL present b				
Disease	genotyped <sup>a</sup>	CD4 <sup>+</sup>	CD14 <sup>†</sup>	LCL	Total	
MS	59					
IBD	69					
Crohn	19					
UC	10					
T1D	47					
RA	34					
CEL	34					
Overall	272	_				

<100 kb

lead disease SNP

nominal eQTL SNP (assoc. P < 0.05)

<1 Mb

eQTL gene

\*\*\*\* CD4/CD14\* (n=211/213) from Raj et al. Science 2014; LCL (n=278) from Lappalainen et al. Nature 2013

		Number of lo					
	Densely	eQTL present <sup>b</sup>					
Disease	genotyped <sup>a</sup>	CD4 <sup>+</sup>	CD14 <sup>+</sup>	LCL	Total		
MS	59	54	55	55	56		
IBD	69	69	69	68	69		
Crohn	19	18	18	18	18		
UC	10	10	9	10	10		
T1D	47	39	40	36	40		
RA	34	34	34	34	34		
CEL	34	34	34	34	34		
Overall	272	258	259	255	261		

<100 kb

lead disease SNP

nominal eQTL SNP (assoc. P < 0.05)

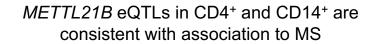
<1 Mb

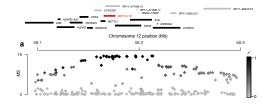
eQTL gene

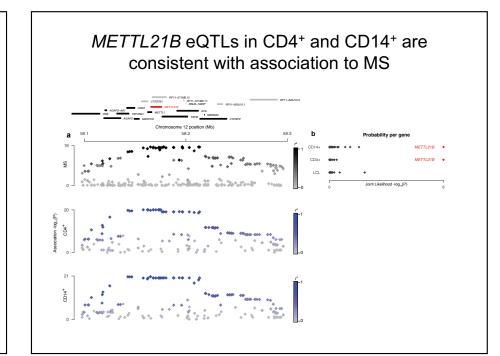
 $^{\circ\circ\circ}$  CD4/CD14+ (n=211/213) from Raj et al. Science 2014; LCL (n=278) from Lappalainen et al. Nature 2013

<sup>\*</sup> Excluding conditional hits

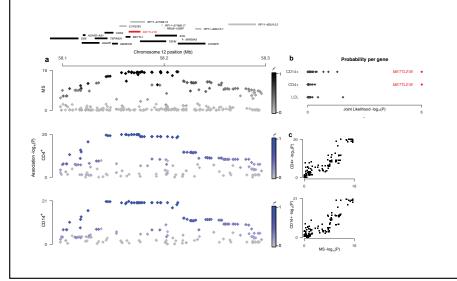
\*\* Defined by ImmunoChip's densely genotyped finemapping intervals. Excluding MHC



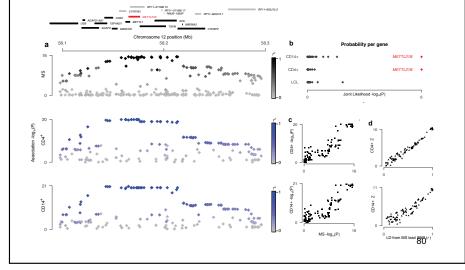


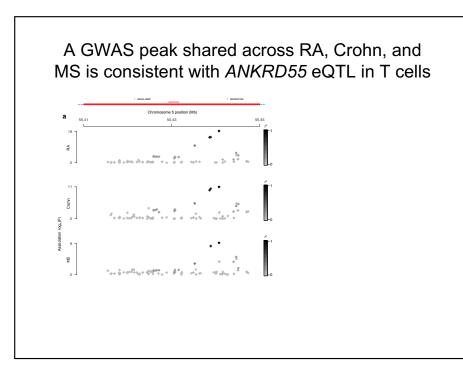


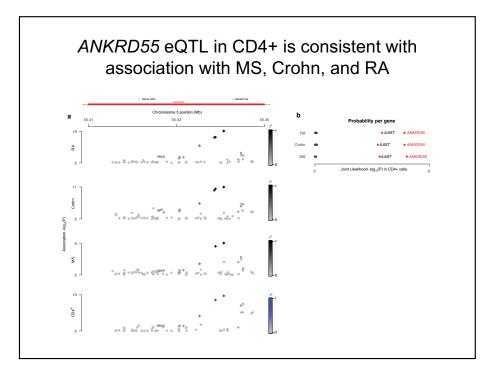
## METTL21B eQTLs in CD4+ and CD14+ are consistent with association to MS

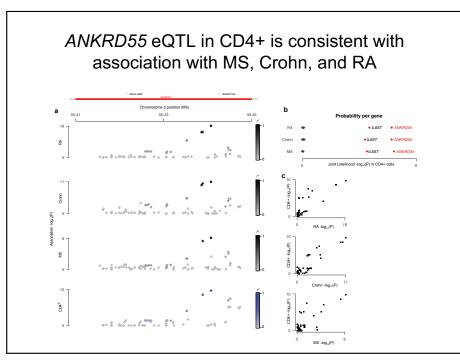


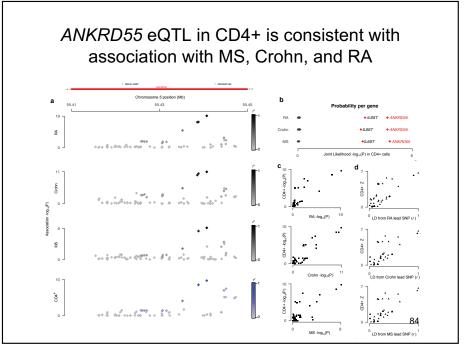
## METTL21B eQTLs in CD4+ and CD14+ are consistent with association to MS







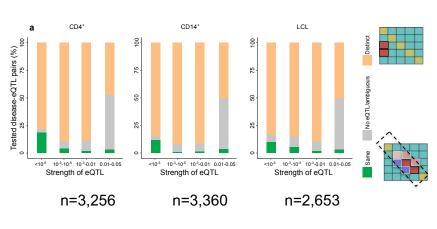




## 15% of disease loci have eQTL driven by the same variant (FDR 5%)

	Number of loci								
	Densely	eQTL present b			Driven by same effect c				
Disease	genotyped a	CD4 <sup>+</sup>	CD14 <sup>+</sup>	LCL	Total	CD4 <sup>+</sup>	CD14 <sup>+</sup>	LCL	Total
MS	59	54	55	55	56	8	3	6	12
IBD	69	69	69	68	69	6	9	1	12
Crohn	19	18	18	18	18	2	1	0	3
UC	10	10	9	10	10	2	1	3	4
T1D	47	39	40	36	40	2	0	0	2
RA	34	34	34	34	34	2	0	1	3
CEL	34	34	34	34	34	3	2	0	5
Overall	272	258	259	255	261	25	16	11	41

## ~75% of tests disease eQTL pairs are driven by distinct variants



### **Summary on eQTLs**

- ~15% of GWAS loci were mapped to eQTL genes.
- ~25% of GWAS loci are driven by the eQTLs of same effect.
- JLIM software

### Methods

**GWAVA** (supervised)

CADD (predicts loss of genetic variation)

INSIGHT / LINSIGHT (population genetics)

Eigen (eigenvector in the annotation space)

PINES (phenotype-specific)

<sup>\* 75%</sup> of hits pass Bonferroni threshold as well.

## Supervised Learning Unsupervised Learning x<sub>2</sub> x<sub>2</sub> x<sub>1</sub> x<sub>1</sub>

### **PINES**

- Take all annotations and create an uncorrelated space
- Upweight axes corresponding to relevant cell/tissue types
- The score is based on the angle with the direction of the maximal possible annotation

